



## Prelude to Discussion on Error Budgets

July 18, 2011 T. Berenc

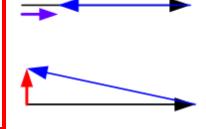


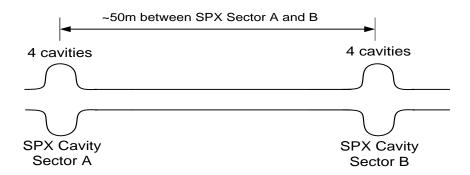
## **Performance Requirements**

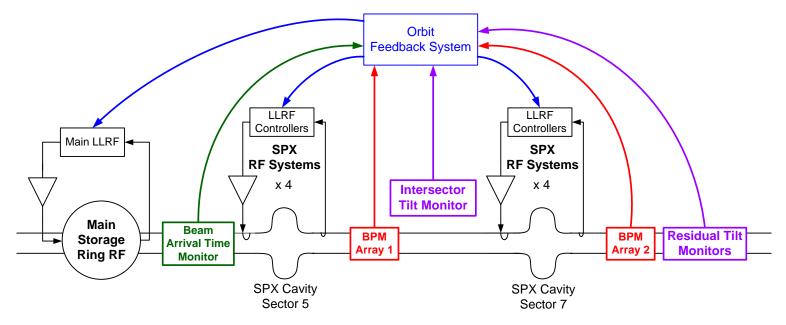
# Common Mode

# Differential Mode

Specification name	Rms Value	Driving requirement
Common-mode voltage	< 1%	Keep intensity and pulse
variation		length variation under
		1% rms
Common-mode phase	$< 4.0^{\circ}$	Keep intensity variation
variation		under 1% rms
Voltage mismatch	< 1.1%	Keep rms emittance
between sectors		variation under 10% of
		nominal 40 pm
Phase error between	$< 0.18^{\circ}$	Keep rms beam motion
sectors		under 10% of beam
		size/divergence





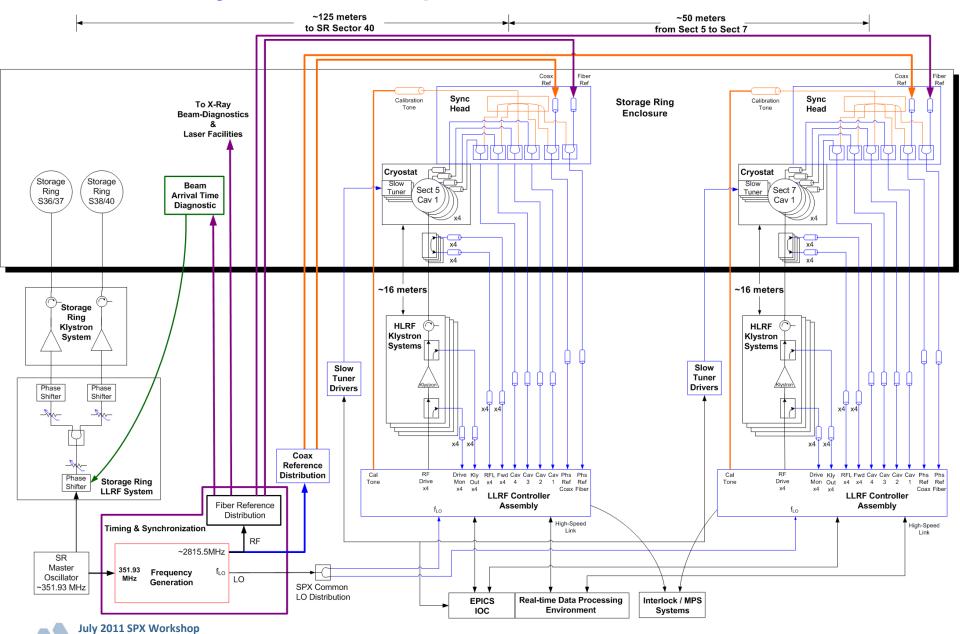


BPM Array 1: sets phase of Sector 5
BPM Array 2: sets phase of Sector 7

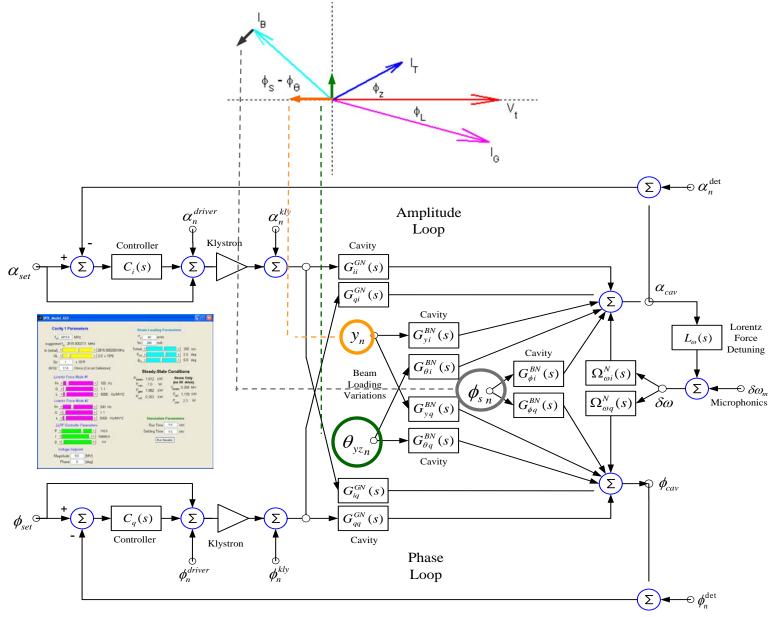
Intersector Tilt Monitor: sets amplitude of Sector 5
Residual Tilt Monitors: sets amplitude of Sector 7

Beam Arrival Time Monitor: sets phase of Main Storage Ring RF

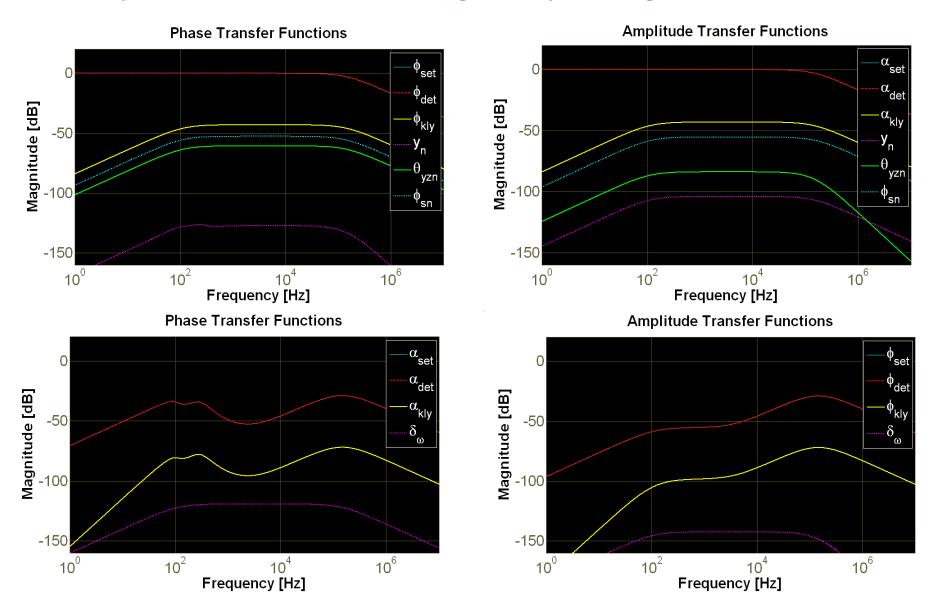
## Production System Concept (2 Sectors, 4 cav/sector)



#### Dynamic small signal model for individual crab cavity

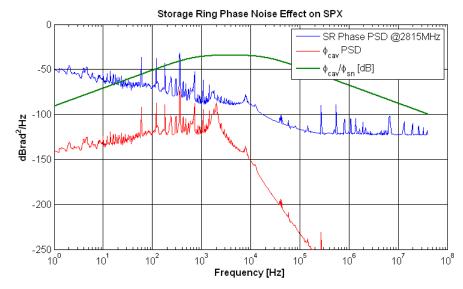


#### Example Transfer Functions from single cavity small signal model





## Motivation for Cavity Electrical Alignment Adjust



Beam Loading is proportional to offset

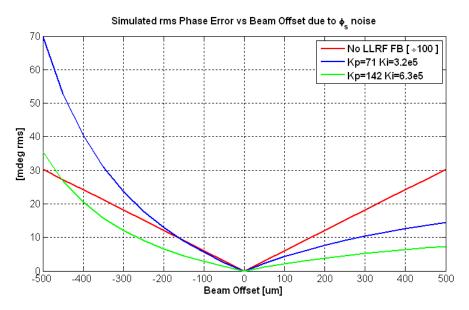
Cavity-to-cavity alignment errors cause

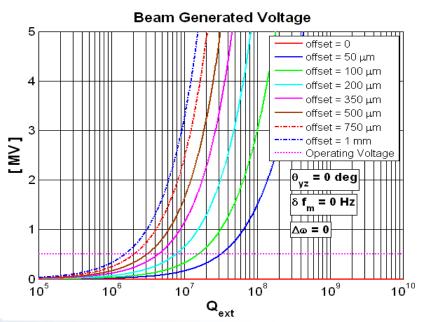
differential beam-loading that will lead to

differential phase noise

Standard cavity-to-cavity alignment = 500um
Beyond APS-U, 4MV => 0.07deg spec
Need measurements of beam jitter at 150mA
Means to reduce effect:

improve cavity alignment, go to lower QL, reduce Storage Ring AM & PM noise





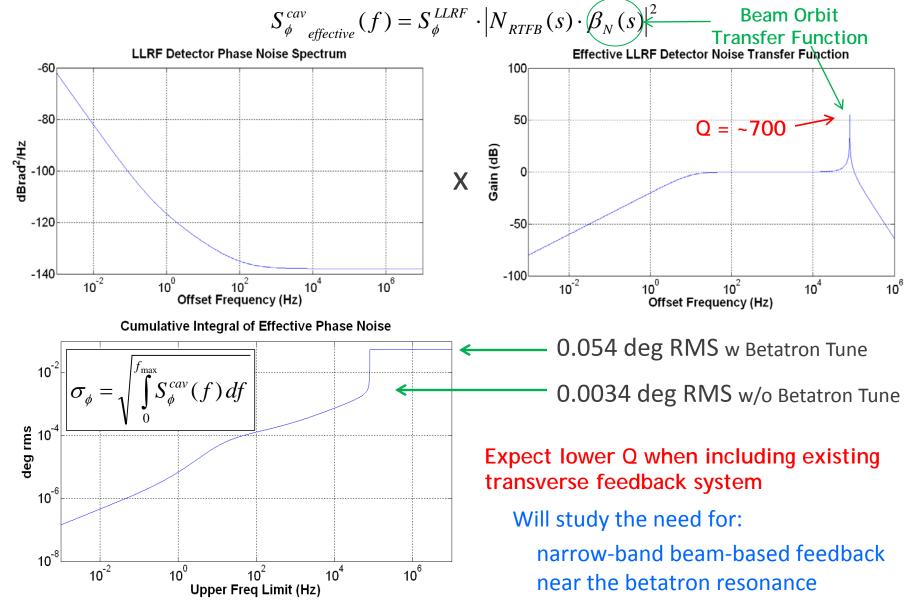
### **Initial Error Budgeting**

$$\sigma_{tot} = \sqrt{\sigma_1^2 + \sigma_2^2 + \dots}$$

$$\sigma_n^2 = \int_{f_{\min}}^{f^{\max}} S_n(f) |H_n(f)|^2 df$$

			PHASE				AMPLITUDE				
		Common M	Common Mode [deg rms] Differential			Common N	/lode [ % rms]	Differential [% rms]			
	Total Budget	4		0.18		1		1.1			
		2.31	3.27	0.10	0.15	0.58	0.82	0.64	0.90		
	Error/Noise Source [4]	< 10Hz [deg rms]	[10Hz-200kHz] [deg rms]	< 10Hz [deg rms]	[10Hz-200kHz] [deg rms]	< 10Hz [% rms]	[10Hz-200kHz] [% rms]	< 10Hz [% rms]	[10Hz-200kHz] [% rms]		
1	SPX Frequency Generation Chassis		0.5097		0.039		0.226		0.249		
2	Phase Ref. Distribution		0.5097		0.039						
3	LO Distribution		0.5097		0.039		0.226		0.249		
4	LLRF Controller		0.5097		0.040		0.226		0.249		
5	Cavity Field Probe Cabling		0.5097		0.039		0.226		0.249		
6	Klystron + Driver Amp		0.5097		0.040		0.226		0.249		
7	Microphonics		0.5097		0.039		0.226		0.249		
8	Beam-Loading Offset Noise		0.5097		0.039		0.226		0.249		
9	Beam-Loading Tilt Noise		0.5097		0.039		0.226		0.249		
10	Storage Ring Beam Jitter		2.7		0.039		0.226		0.249		
	Beam-Loading Synchronous Phase Noise (other than										
11	Storage Ring beam jitter ??)		0.5097		0.039		0.226		0.249		
12	Beam Arrival Time Feedback Process		0.5097		0.039		0.226		0.249		
13	AM-to-PM Cross Modulation		0.5097		0.039						
14	PM-to-AM Cross Modulation	N/A.					0.226		0.249		
15	Orbit Feedback Process [outside SPX zone] (differential phase correction)	N/A			0.039						
16	Orbit Feedback Process [inside SPX zone] (common mode phase correction)		0.5097								
17	Residual Tilt Feedback [outside SPX zone] long-term differential amplitude correction	N/A							0.249		
18	Intersector Tilt Feedback Process [inside SPX zone] common mode amplitude set-point	N/A:					0.226				
	# of processes	14		14		13		13			

### **Example Calculation for a Single Line Item**



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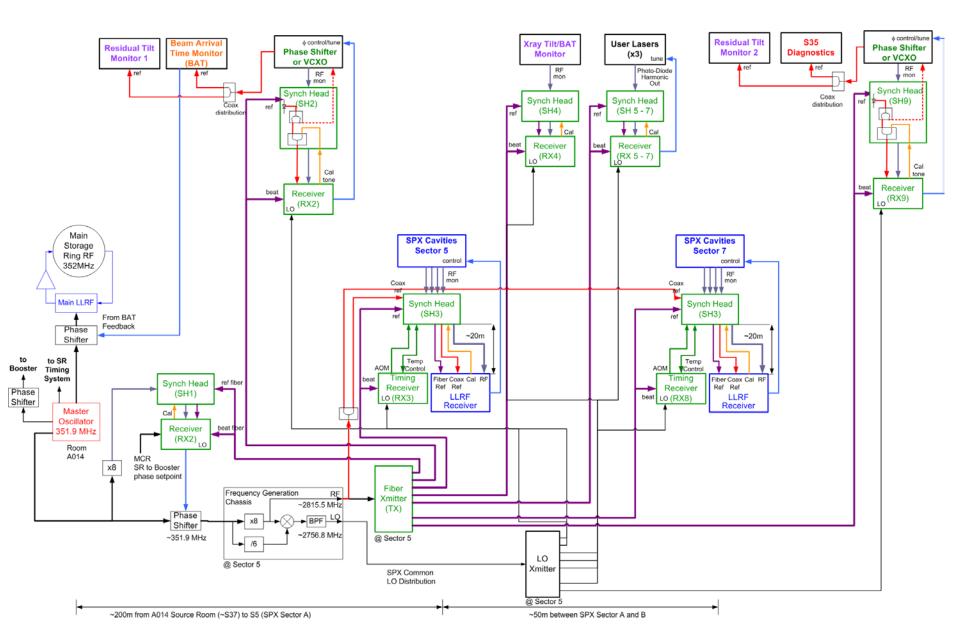
#### Potential Topics To Discuss...

- Identify additional processes and noise sources
- Ways to a practical allocation of error budgets across frequency bands and systems
- Cavity alignment tolerance
- Interaction with orbit feedback and influence of bunch by bunch feedback on betatron tune Q

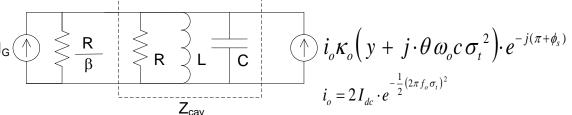
#### **Blank Worksheet**

			PHASE			AMPLITUDE				
		Common Mode [deg rms]		Differential [deg rms]		Common Mode [ % rms]		Differential [% rms]		
	Total Budget		4		0.18		1		1.1	
	101	< 10Hz	[10Hz-200kHz]	< 10Hz	[10Hz-200kHz]	< 10Hz	[10Hz-200kHz]	< 10Hz	[10Hz-200kHz]	
	Error/Noise Source [4]	[deg rms]	[deg rms]	[deg rms]	[deg rms]	[% rms]	[% rms]	[% rms]	[% rms]	
1	SPX Frequency Generation Chassis									
2	Phase Ref. Distribution									
3	LO Distribution									
4	LLRF Controller									
5	Cavity Field Probe Cabling									
6	Klystron + Driver Amp									
7	Microphonics									
8	Beam-Loading Offset Noise									
9	Beam-Loading Tilt Noise									
10	Storage Ring Beam Jitter									
	Beam-Loading Synchronous Phase Noise (other than									
11	Storage Ring beam jitter ??)									
12	Beam Arrival Time Feedback Process									
13	AM-to-PM Cross Modulation					N/A	N/A	N/A	N/A	
14	PM-to-AM Cross Modulation	N/A		WA						
15	Orbit Feedback Process [outside SPX zone] (differential phase correction)	N/A				N/A	N/A			
	Orbit Feedback Process [inside SPX zone]				+					
16	(common mode phase correction)									
17	Residual Tilt Feedback [outside SPX zone] long-term differential amplitude correction	N/A								
18	Intersector Tilt Feedback Process [inside SPX zone] common mode amplitude set-point	N/A								
	# of processes		14		<u> </u> 14	ļ.	13		<u> </u> .3	

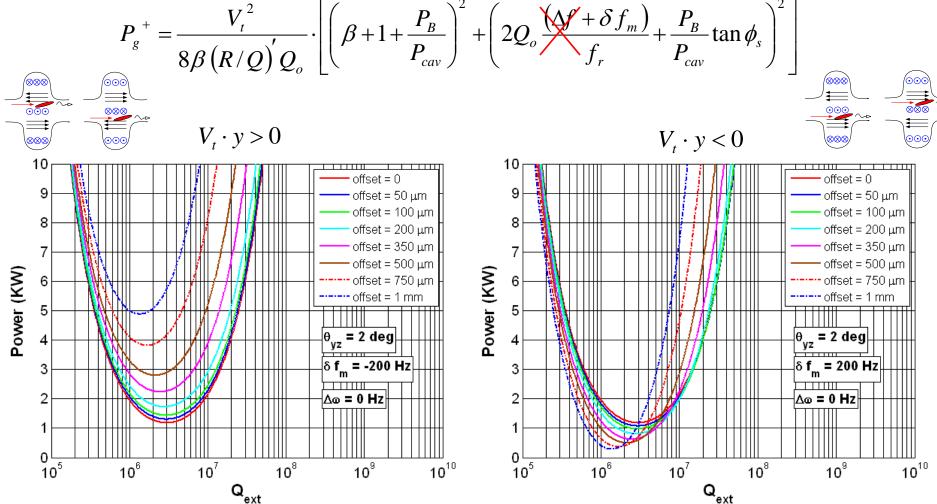
## **Backup Slides**



### **Deflecting Cavity Beam Loading**

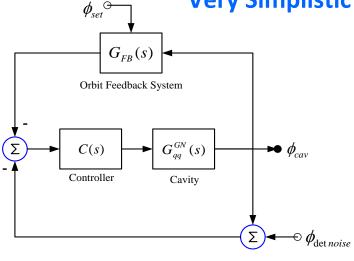


$$P_g^+ = \frac{V_t^2}{8\beta (R/Q)'Q_o} \cdot \left[ \left(\beta + 1 + \frac{P_B}{P_{cav}}\right)^2 + \left(2Q_o \frac{(M + \delta f_m)}{f_r} + \frac{P_B}{P_{cav}} \tan \phi_s\right)^2 \right]$$





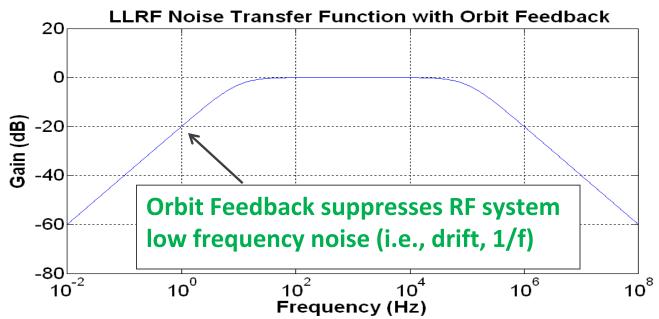
#### **Very Simplistic First Order Orbit Feedback concept**



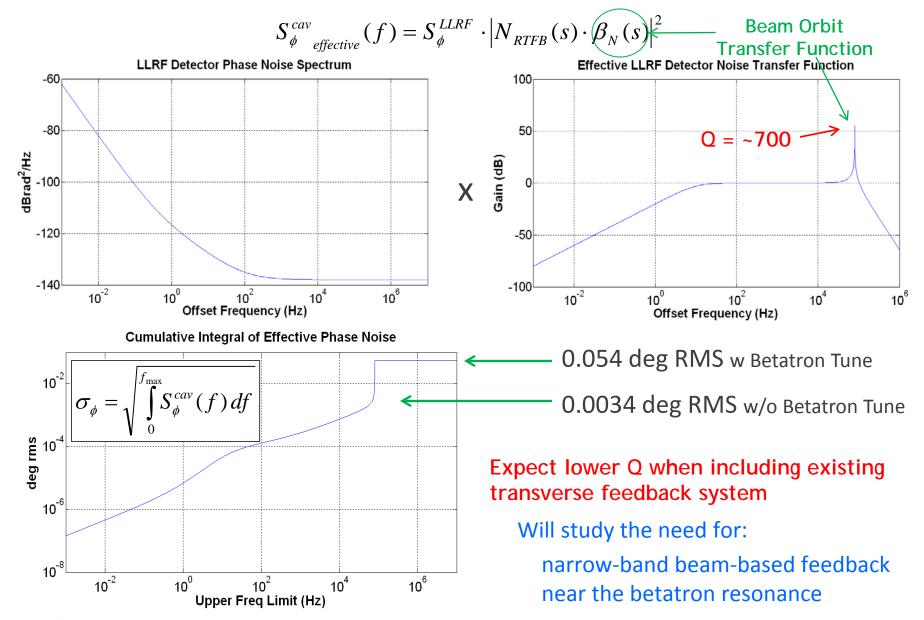
Assume: 
$$G_{FB}(s) = \frac{K_p^{RTFB} \sigma_{RTFB}}{s}$$

$$N_{FB}(s) = \frac{\phi_{cav}(s)}{\phi_{\text{det noise}}(s)} = \frac{C(s)G_{qq}^{GN}(s)}{1 + C(s)G_{qq}^{GN}(s)[1 + G_{FB}(s)]}$$

$$= \frac{K_p \sigma_{cav} s}{s^2 + K_p \sigma_{cav} s + K_p^{RTFB} K_p \sigma_{RTFB} \sigma_{cav}}$$



#### How to achieve 0.18° rms Differential Phase ??



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