



SPX LLRF R&D

ANL: Tim Berenc, Hengjie Ma, Ned Arnold, Frank Lenkszus, Tom Fors, Bill Yoder

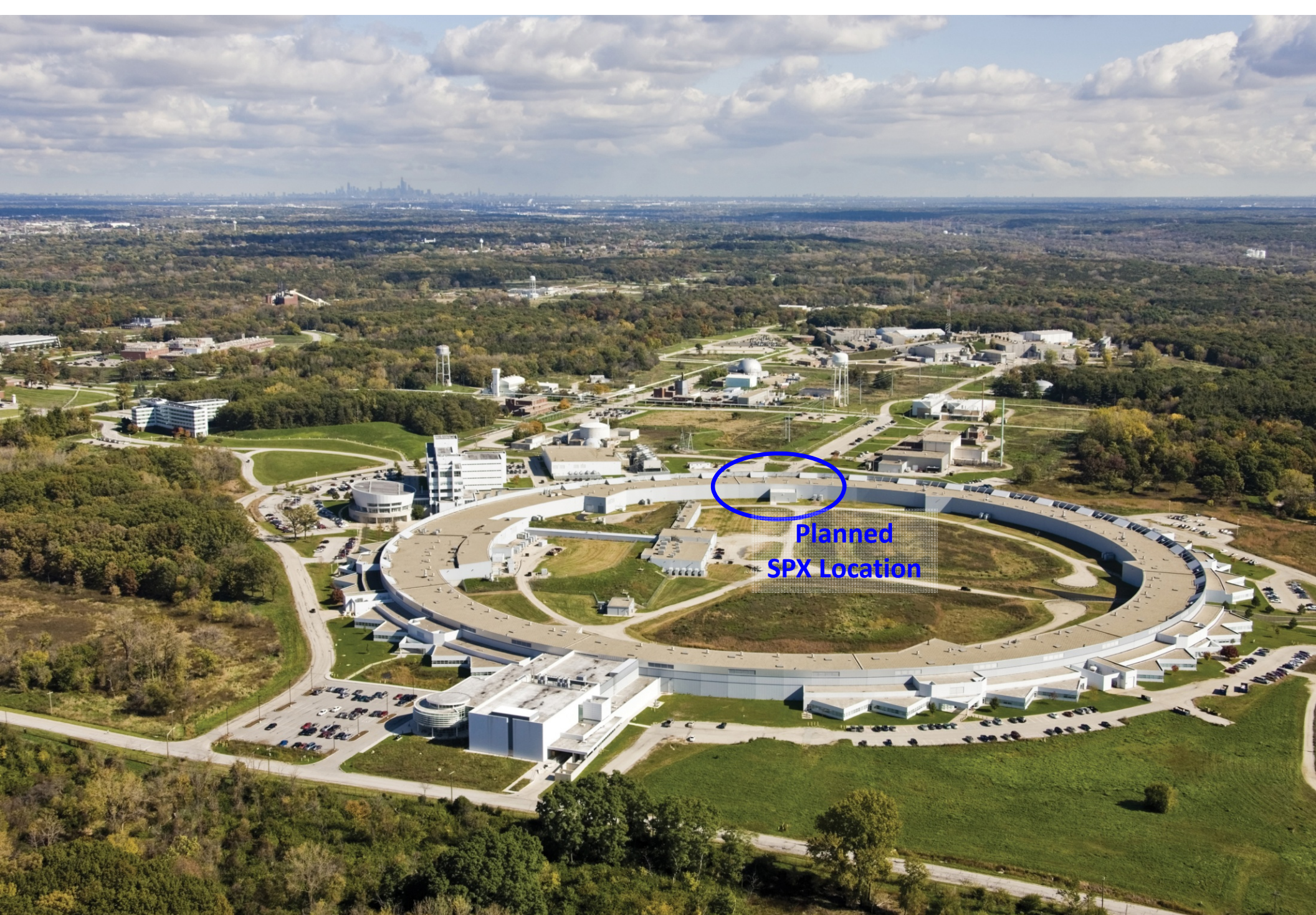
LBNL: Larry Doolittle, Gang Huang, John Byrd, Jim Greer, Kerri Campbell

Feb. 6, 2012
ASD Seminar

Outline

- Intro
- LLRF Receiver (prototype results)
- Deflecting Cavity Behavior (static and dynamic)
- LLRF Controller (benchtop performance tests)
- Storage Ring RF modification plans
- Summary



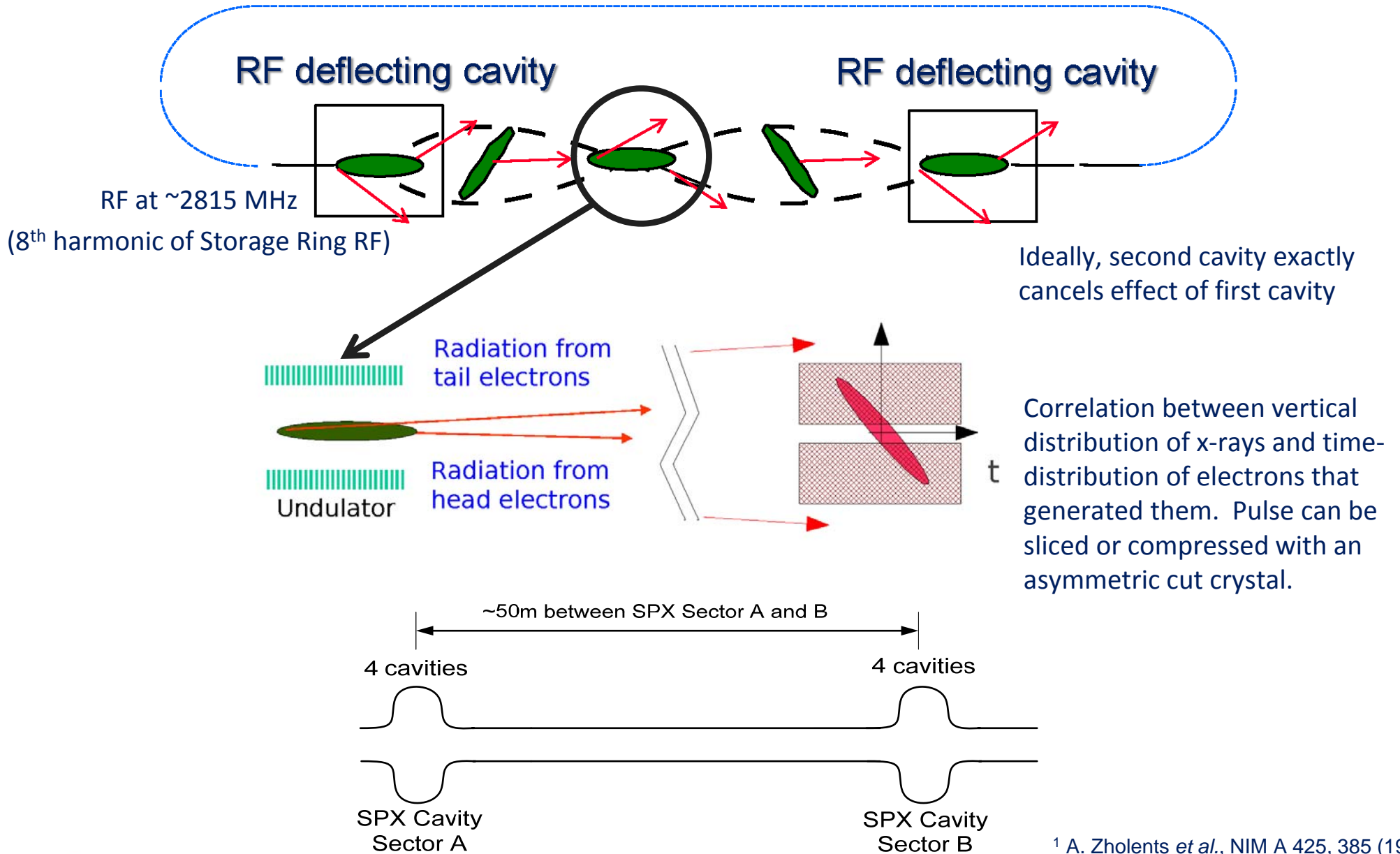


Planned
SPX Location



APS-U SPX System - Zholents' Transverse RF Chirp Concept¹

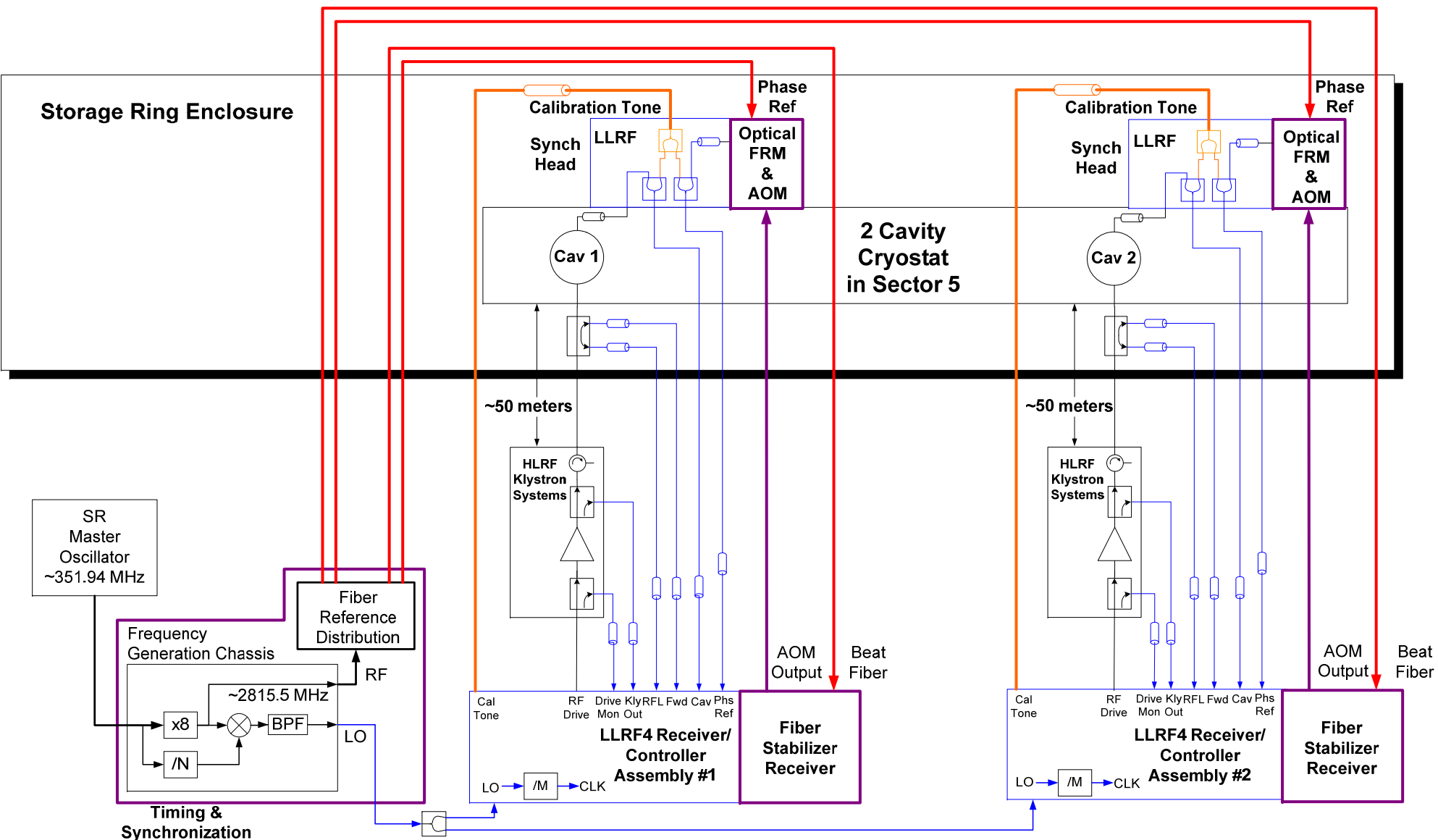
Goal: provide ~2 psec (presently 50-100 psec) X-ray pulses at 6.5 MHz rep. rate for time-resolved studies



¹ A. Zholents *et al.*, NIM A 425, 385 (1999)

SPX0 = R&D System Proof of Principle (1 Sector, 2 cavities)

- Cavities counter-phased (180deg) to demonstrate tolerance requirements
- Cavities run in-phase to create a chirped beam around entire ring to have a look at short pulse x-rays

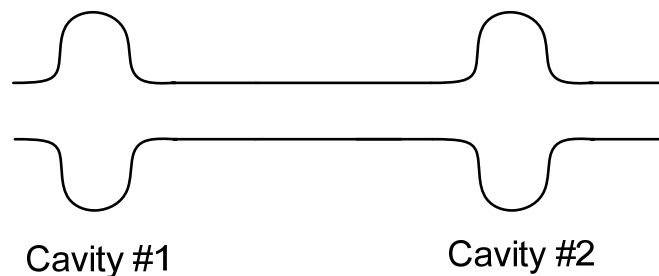
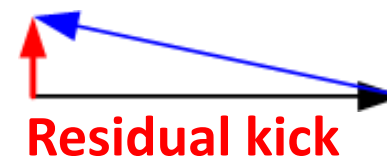


SPX0 System Performance Requirements ³

Specification name	Rms Value	Bandwidth	Driving requirement
Common-mode voltage amplitude variation	< 7%	0.1Hz – 271kHz	Keep beam emittance variation distinguishable from the differential voltage effect for SPX0
Common-mode phase variation	< 1.0 deg	0.1Hz – 1kHz	Keep global orbit motion distinguishable from differential phase for SPX0
	< 3.6 deg	1kHz – 271kHz	Keep rms emittance variation distinguishable from differential phase for SPX0
Differential mode voltage variation	< 1%	0.1Hz – 1kHz	Keep rms emittance variation outside of SPX under 10 % of nominal 35 pm
	< 0.77%	1kHz – 271kHz	Effective emittance growth under 1.5 pm for SPX
Differential mode phase variation	< 0.077 deg	0.1Hz – 1kHz	Keep global rms orbit motion under 10% of the beam size/divergence for SPX
	< 0.28 deg	1kHz – 271kHz	Keep emittance growth outside of SPX under 10 % of nominal 35 pm

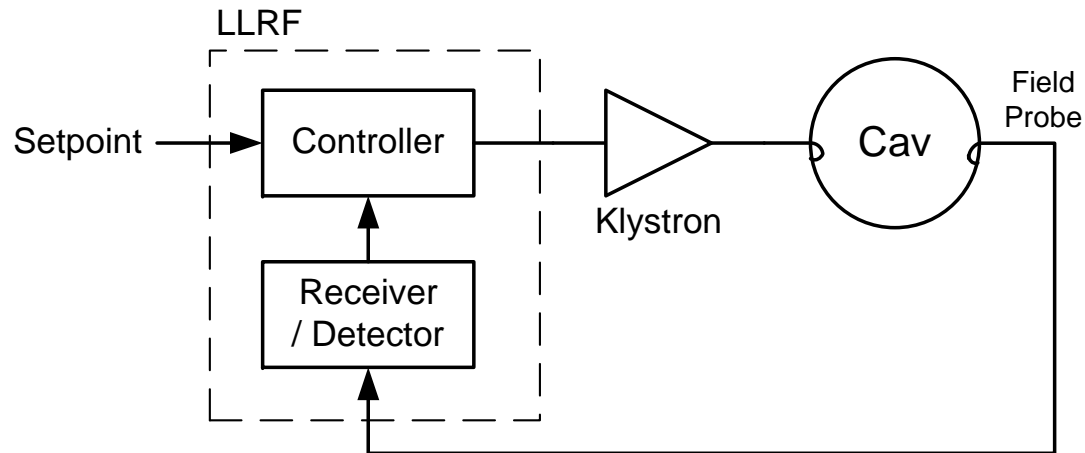
Common Mode

Differential



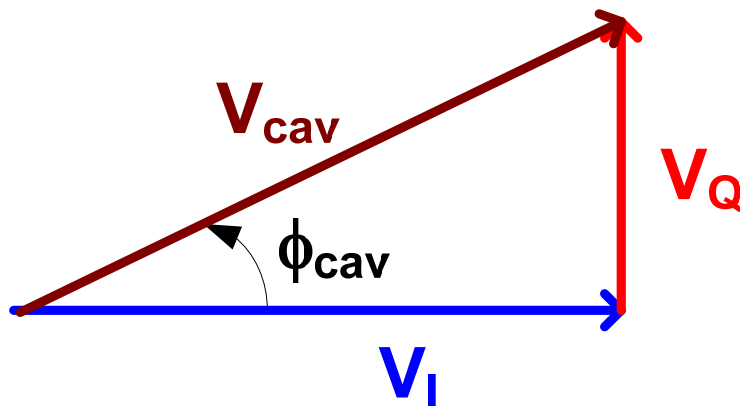
Low Level Radio Frequency (LLRF) System

Primary responsibility is to regulate the cavity field



Polar Coordinates

$$V_{cav} \cos(\omega_{RF} t + \phi_{cav})$$



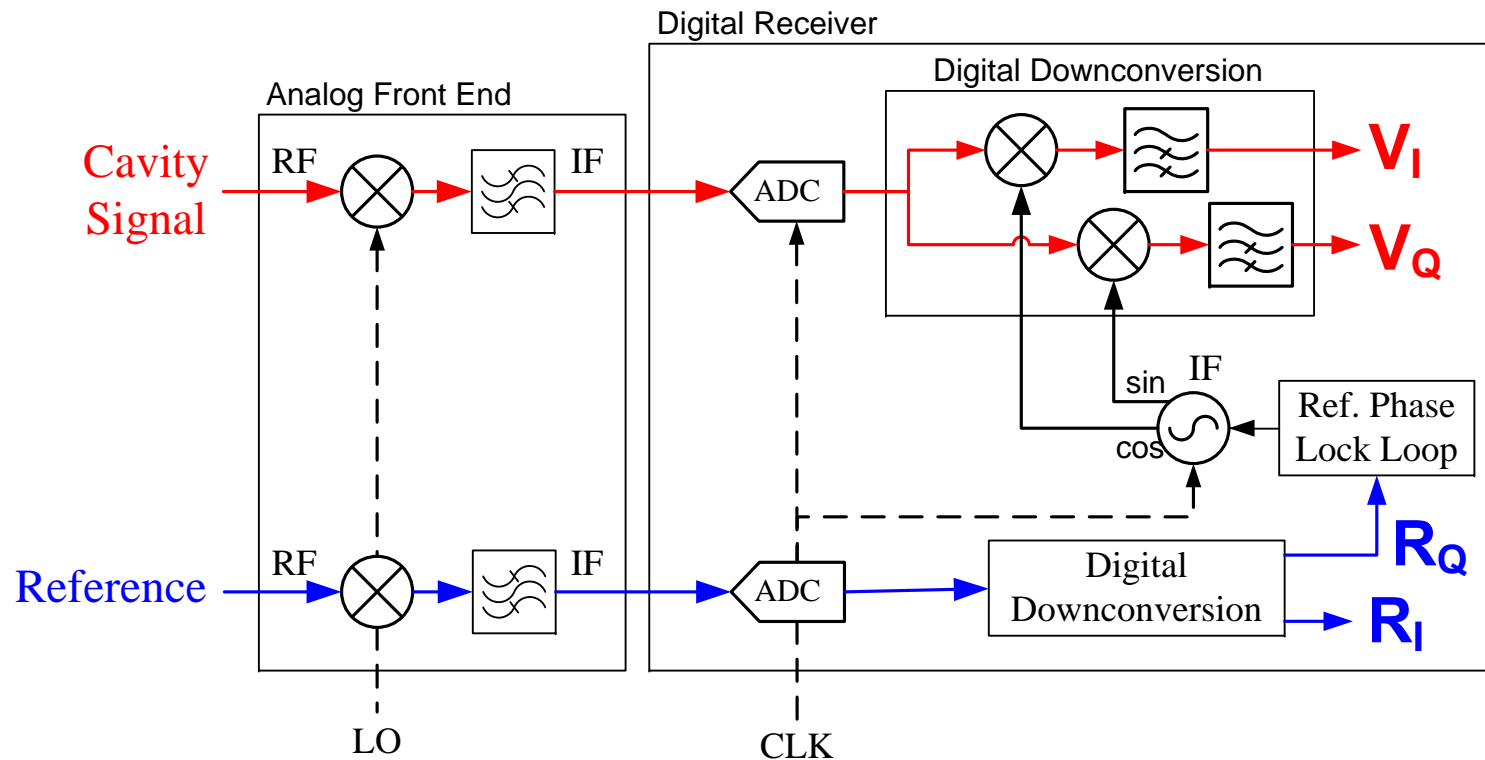
Cartesian Coordinates

$$V_I \cos \omega_{RF} t - V_Q \sin \omega_{RF} t$$

$$V_{cav} = \sqrt{V_I^2 + V_Q^2}$$

$$\phi_{cav} = \arg(V_I + jV_Q)$$

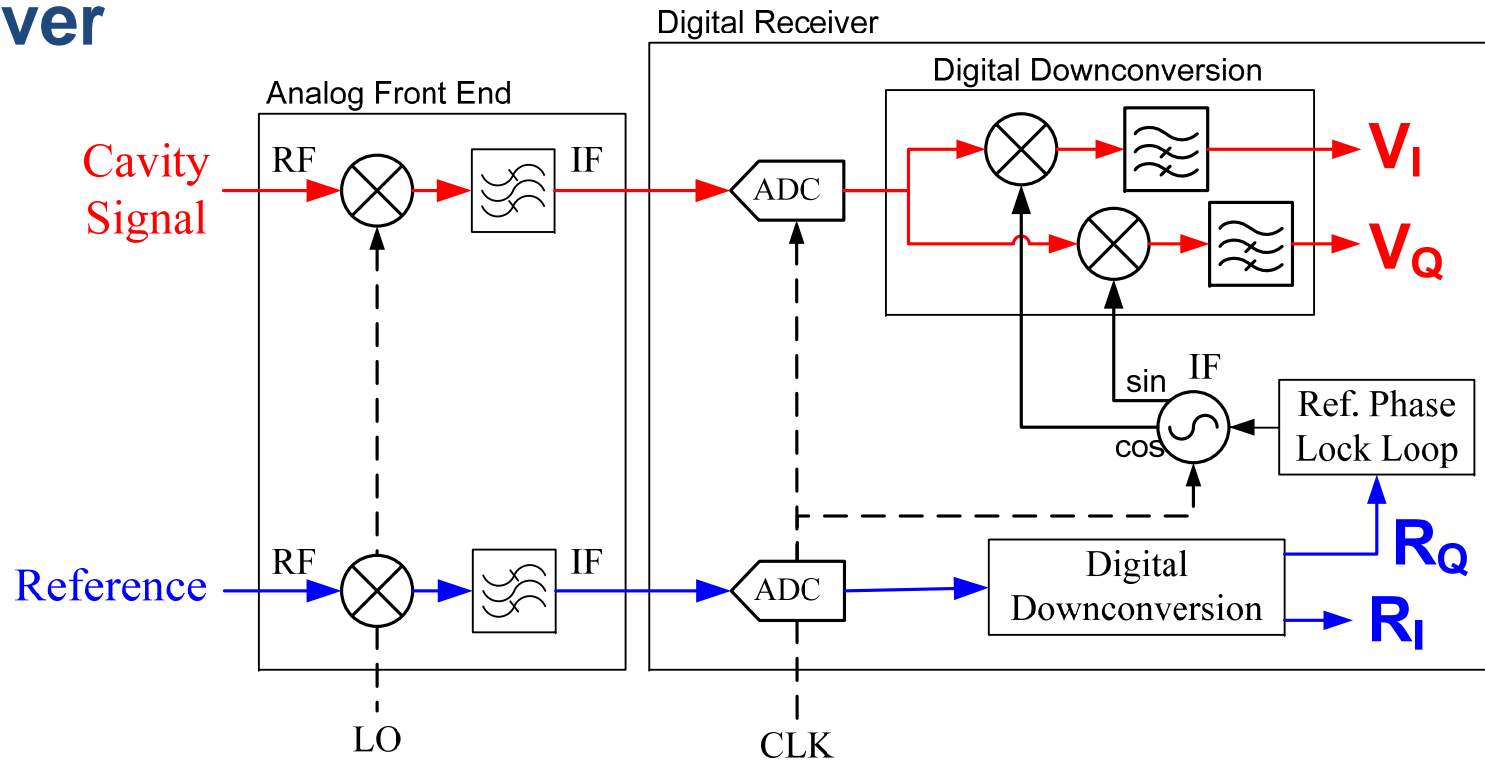
Receiver You can't regulate any better than your receiver



Regulate to a Designated Phase Reference

- Don't let the LO assume the role of the phase reference
- Phase is a Differential Measurement
- Mixers preserve phase information, x's and ÷'s preserve timing
- In theory, common mode LO and clock noise cancels

Receiver



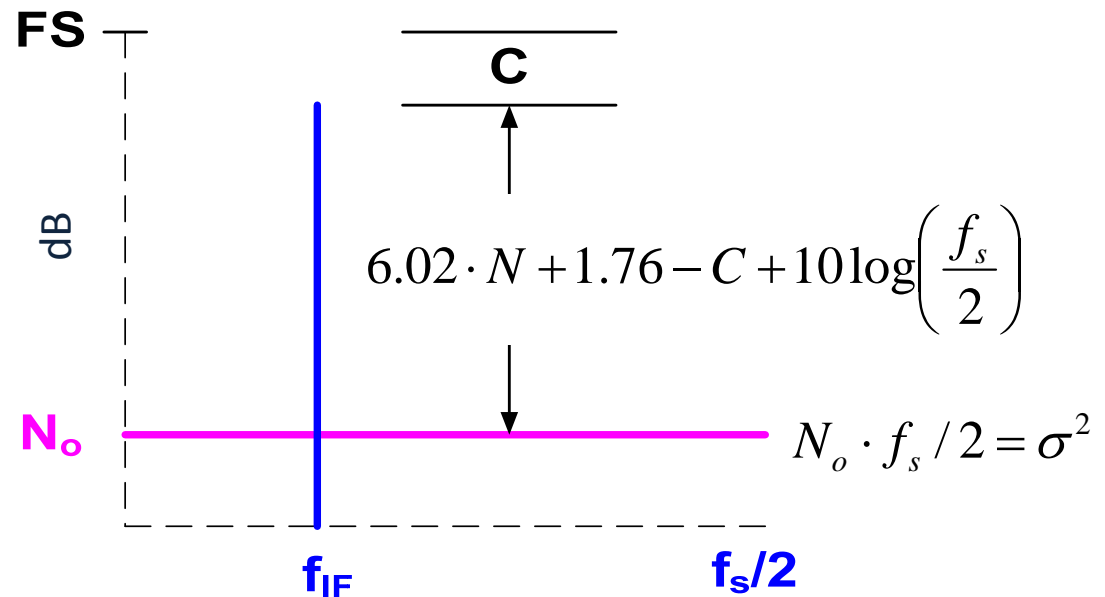
ADC Quantization Noise

Variance $\sigma^2 = \frac{q^2}{12} = \frac{1}{2^{2N} \cdot 12}$

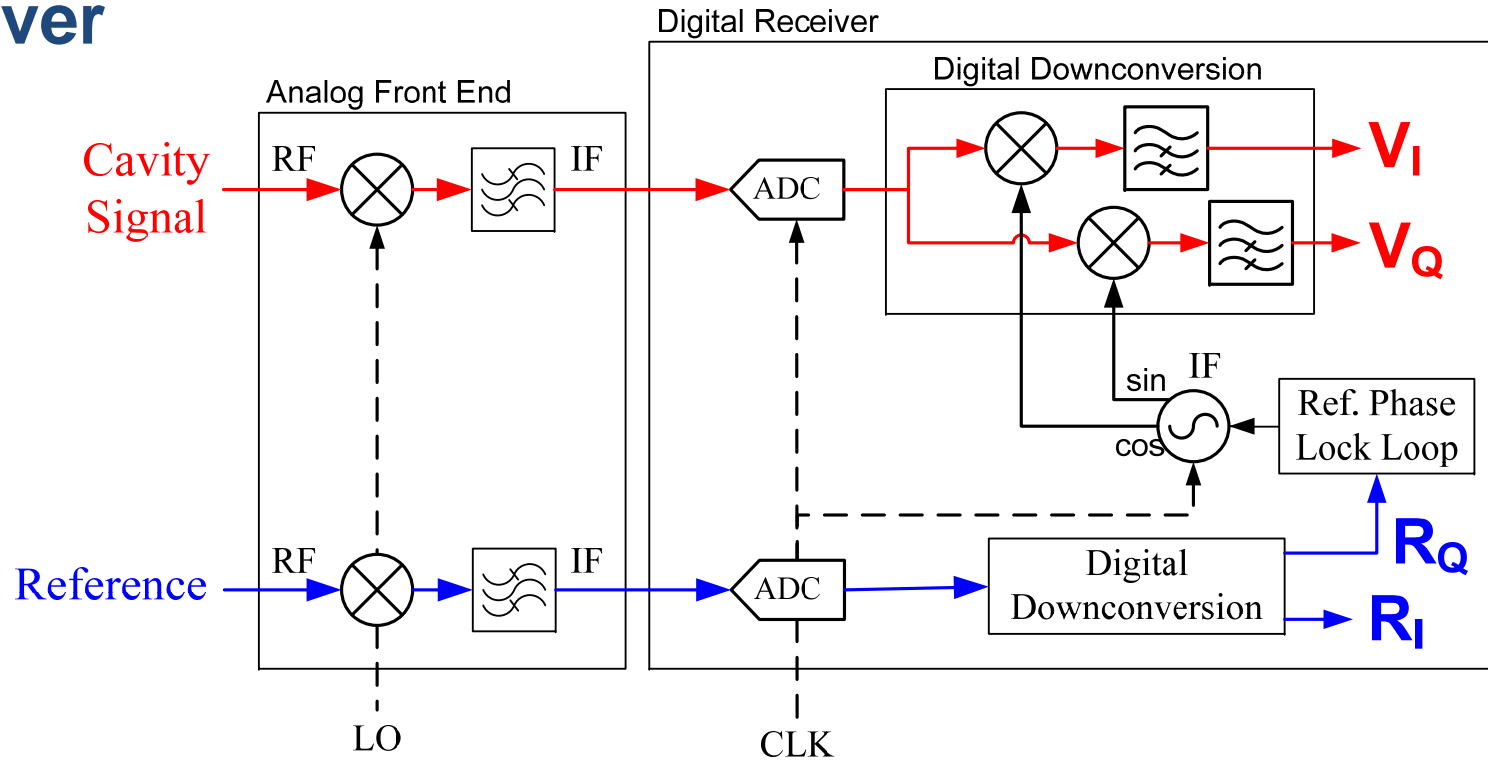
$SNR = 6.02 \cdot N + 1.76 - C$ [dB]

N = # of ADC bits

C = dB carrier is below full scale



Receiver



ADC Quantization Noise

phase noise variance

$$\sigma_{\phi}^2 = \int_0^{f_{\max}} S_{\phi}(f) df$$

14 bit ADC

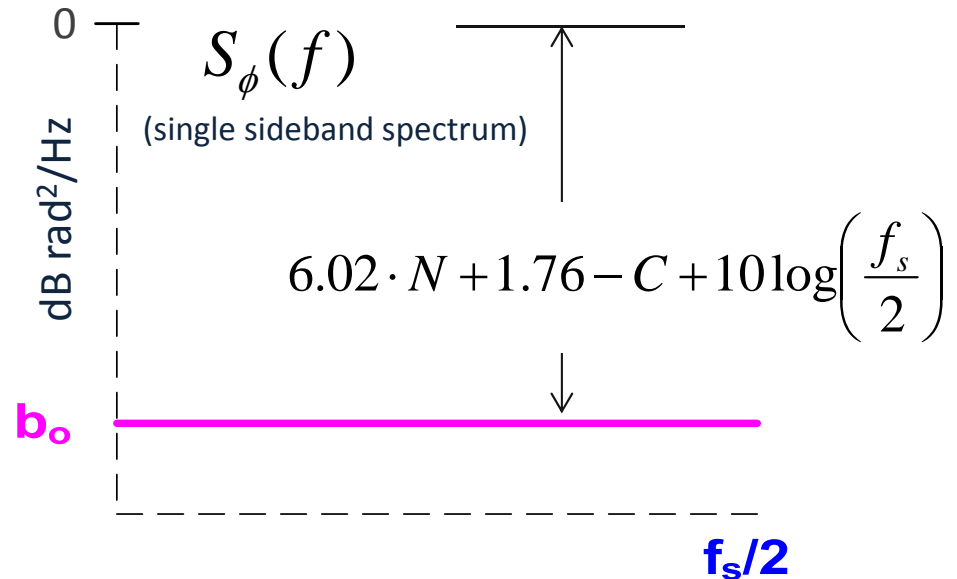
16 bit ADC

$$\sigma_{\phi}^2 = -85 \text{ dB rad}^2$$

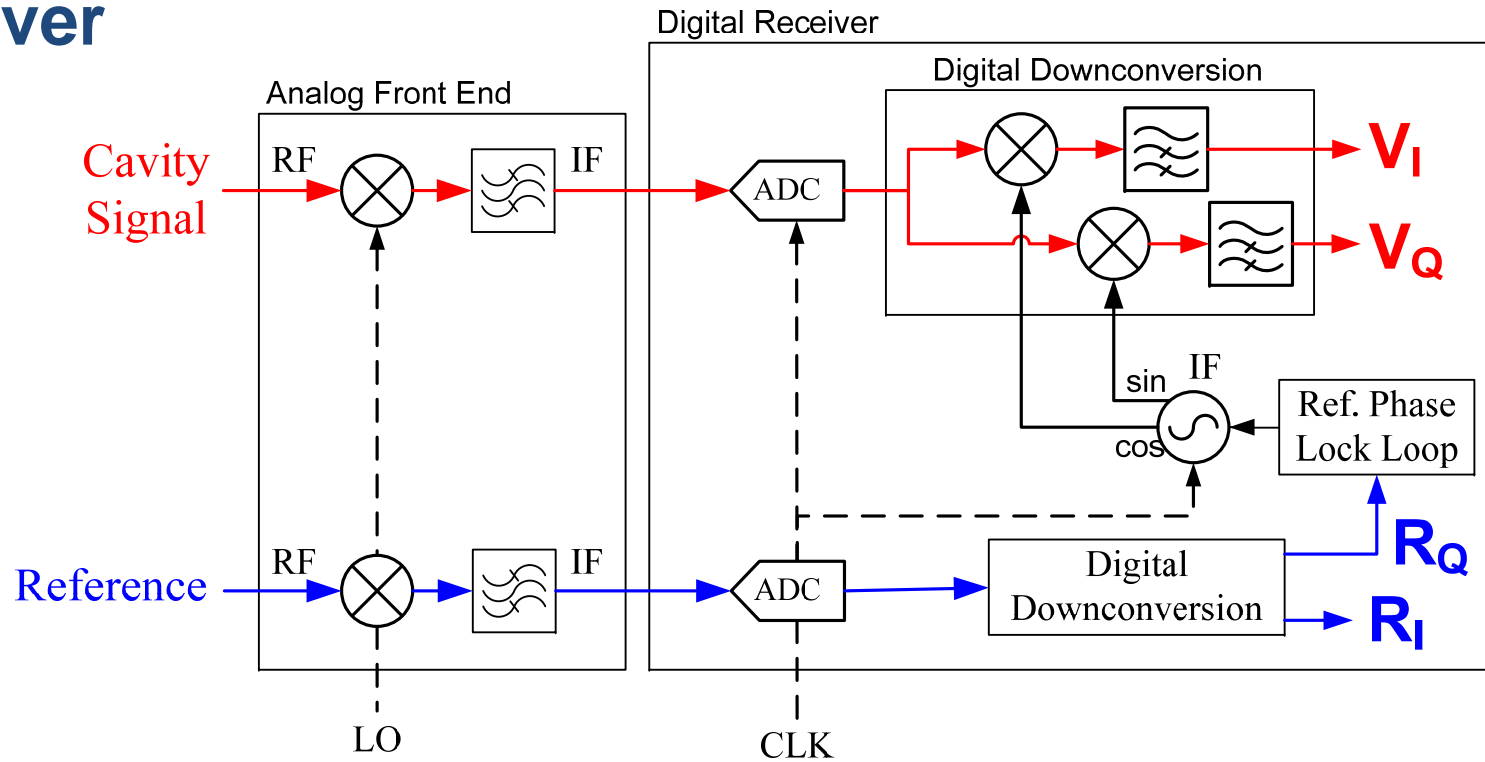
$$\sigma_{\phi}^2 = -97 \text{ dB rad}^2$$

$$\sigma_{\phi} = 0.0032 \text{ deg rms}$$

$$\sigma_{\phi} = 0.0008 \text{ deg rms}$$



Receiver



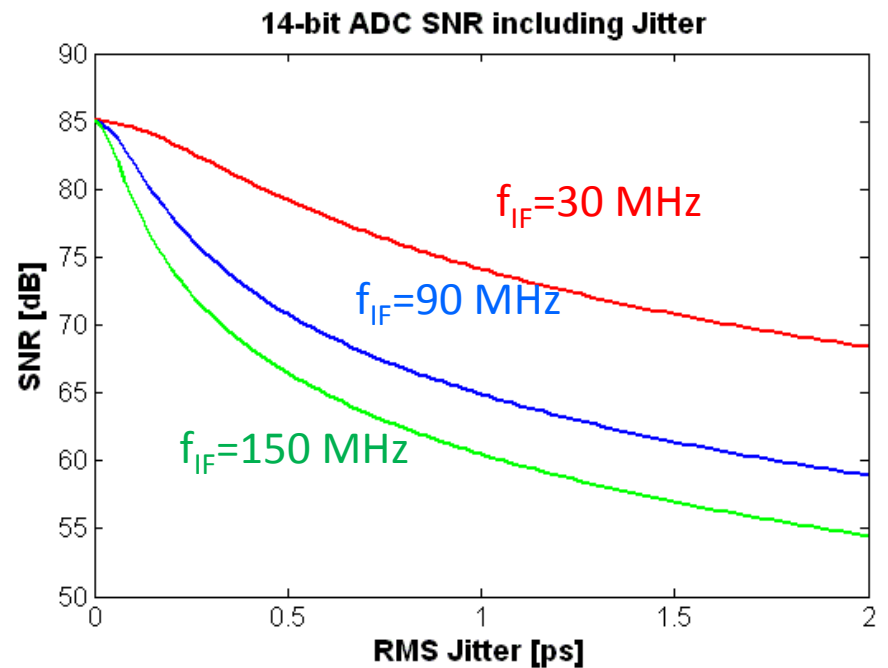
ADC Aperture Jitter

$$\cos(\omega_{IF}(t + \varepsilon)) = \cos(\omega_{IF}t + \omega_{IF}\varepsilon)$$

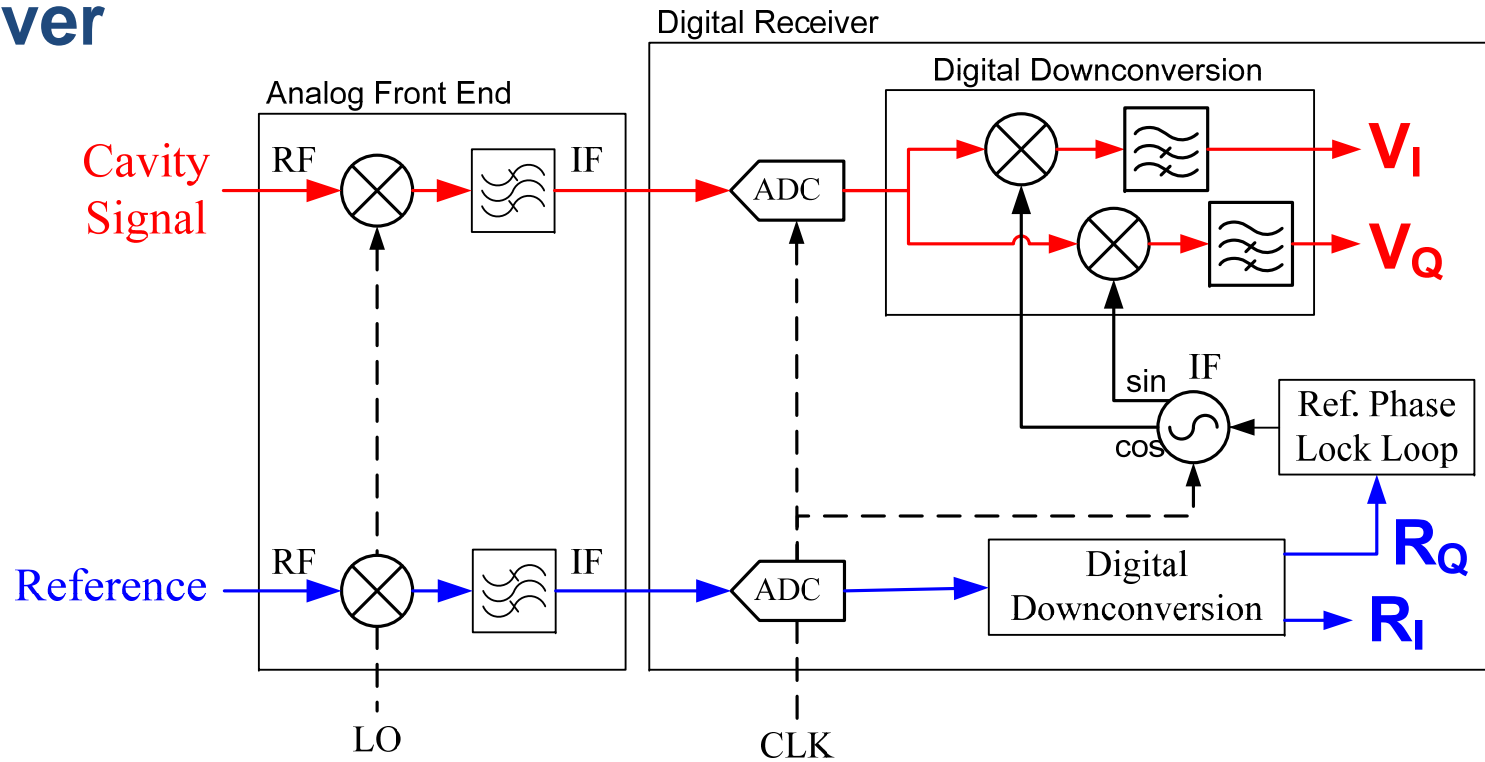
Phase noise

$$SNR_{jitter} = -20 \cdot \log(\omega_{IF} \cdot \sigma_{jitter}) \quad [\text{dB}]$$

σ_{jitter} rms aperture jitter



Receiver



ADC Aperture Jitter

phase noise variance

$$\sigma_\phi^2 = \int_0^{f_{\max}} S_\phi(f) df$$

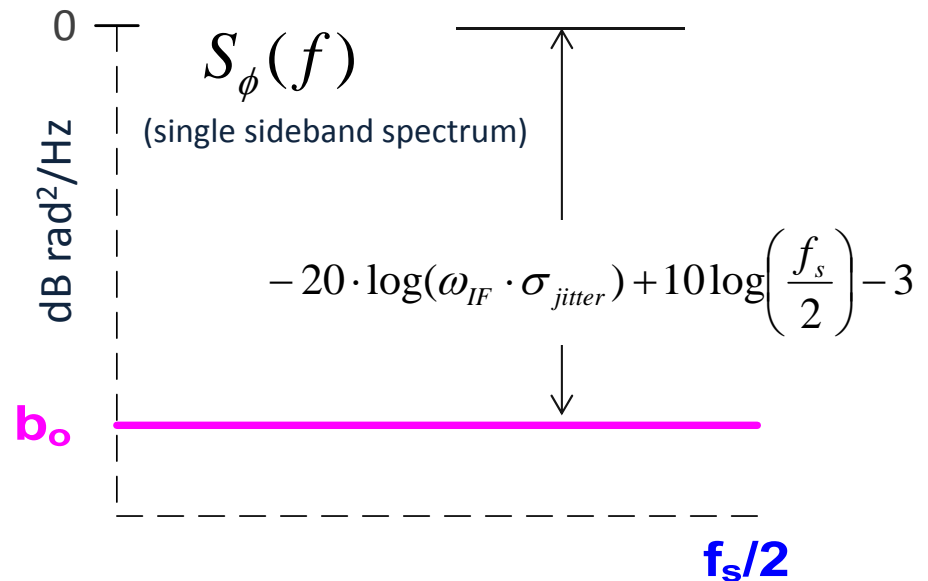
14 bit ADC, 0.5psec rms

30 MHz IF

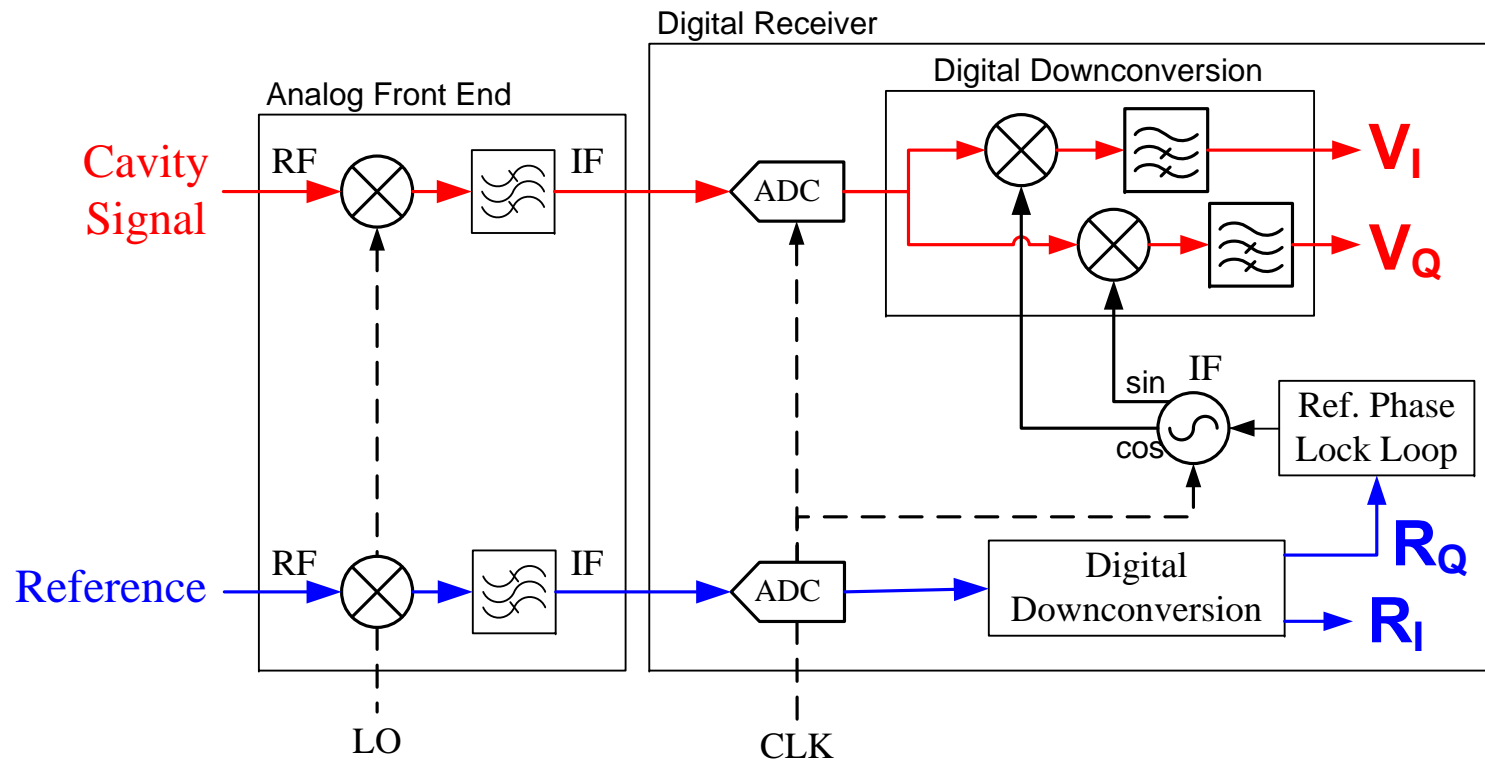
$$\sigma_\phi \approx 0.008 \text{ deg rms}$$

90 MHz IF

$$\sigma_\phi \approx 0.023 \text{ deg rms}$$



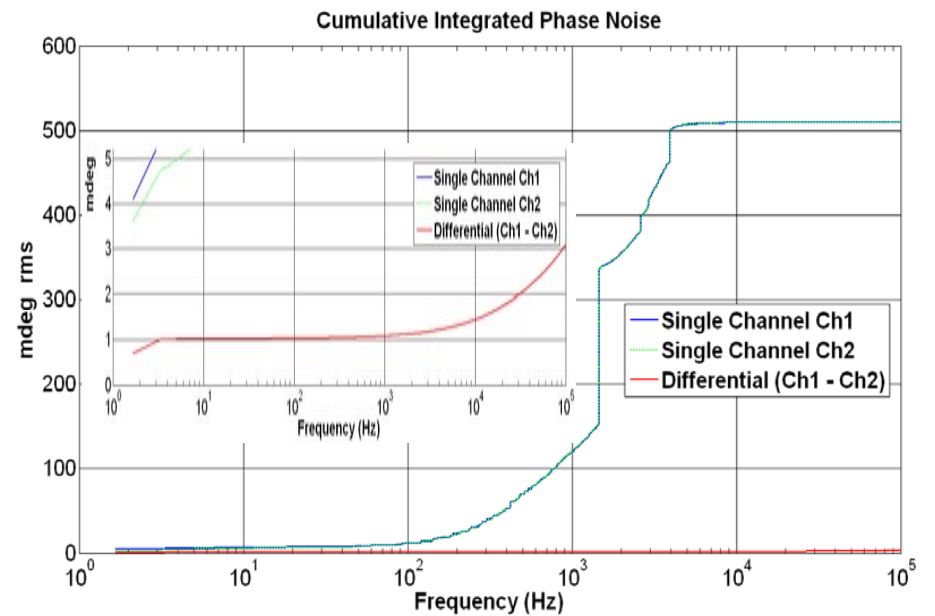
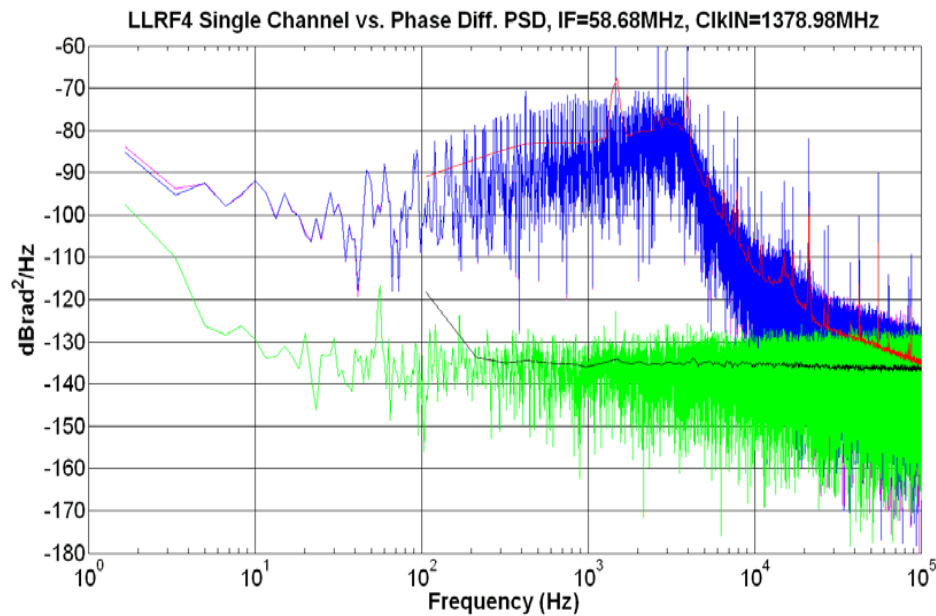
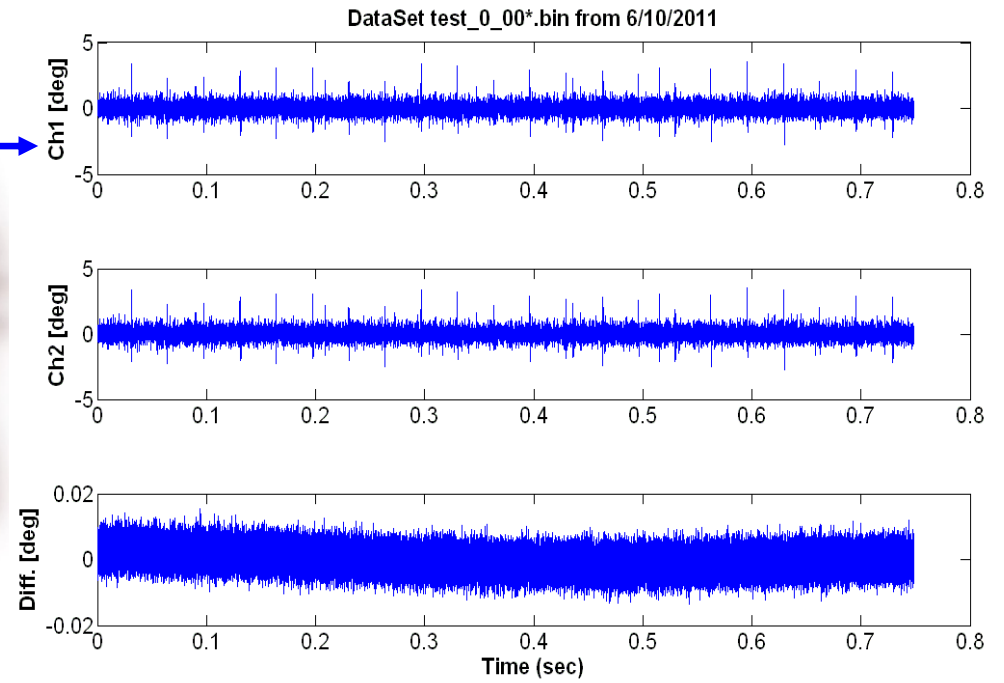
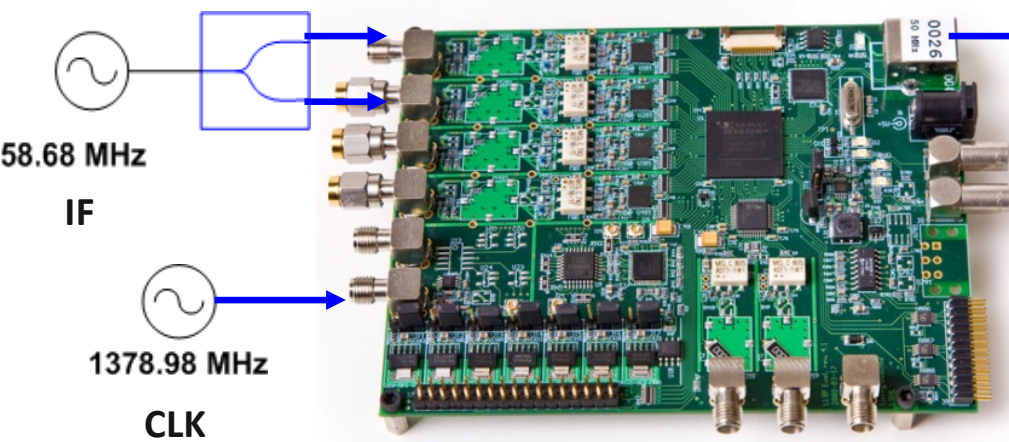
Receiver You can't regulate any better than your receiver



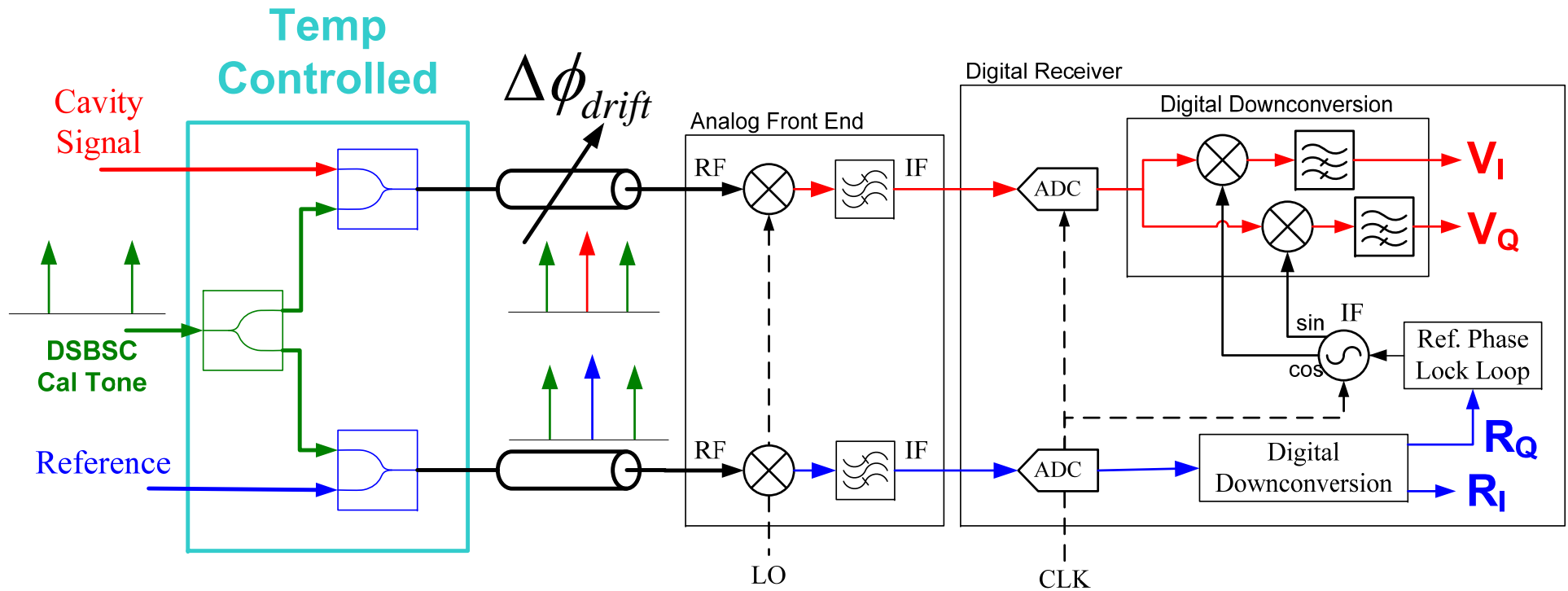
Regulate to a Designated Phase Reference

- Don't let the LO assume the role of the phase reference
- Phase is a Differential Measurement
- Mixers preserve phase information, x's and ÷'s preserve timing
- **In theory, common mode LO and clock noise cancels**

Receiver – Digital Receiver LLRF4 Board – Differential Phase Noise



Receiver - CW Drift Compensation⁴



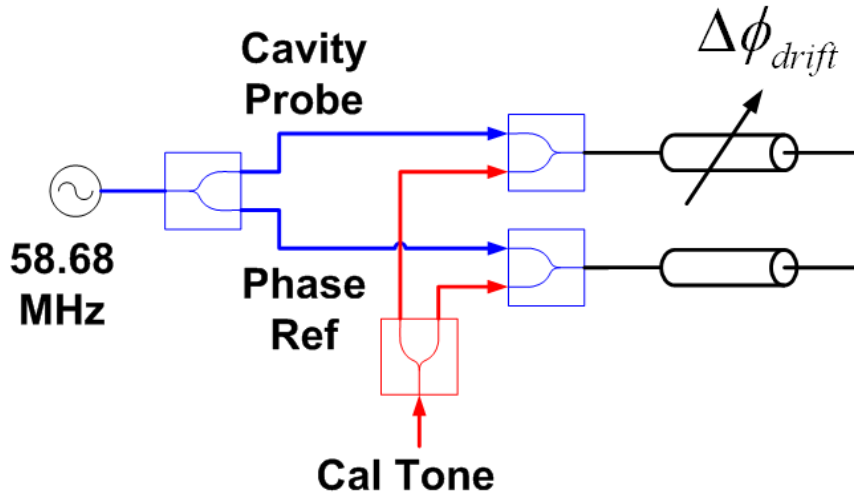
$$\Delta\phi_{meas} = (\phi_{cav} - \phi_{ref}) + \Delta\phi_{drift}$$

$$\Delta\phi_{calTone} = \Delta\phi_{drift}$$

$$\Delta\phi_{correct} = \Delta\phi_{meas} - \Delta\phi_{calTone}$$

⁴ "Signal Processing for High Precision Phase Measurements", G. Huang, L. Doolittle, J. Staples, R. Wilcox, J. Byrd, Proceedings of BIW10

Receiver - CW Drift Compensation Demonstration

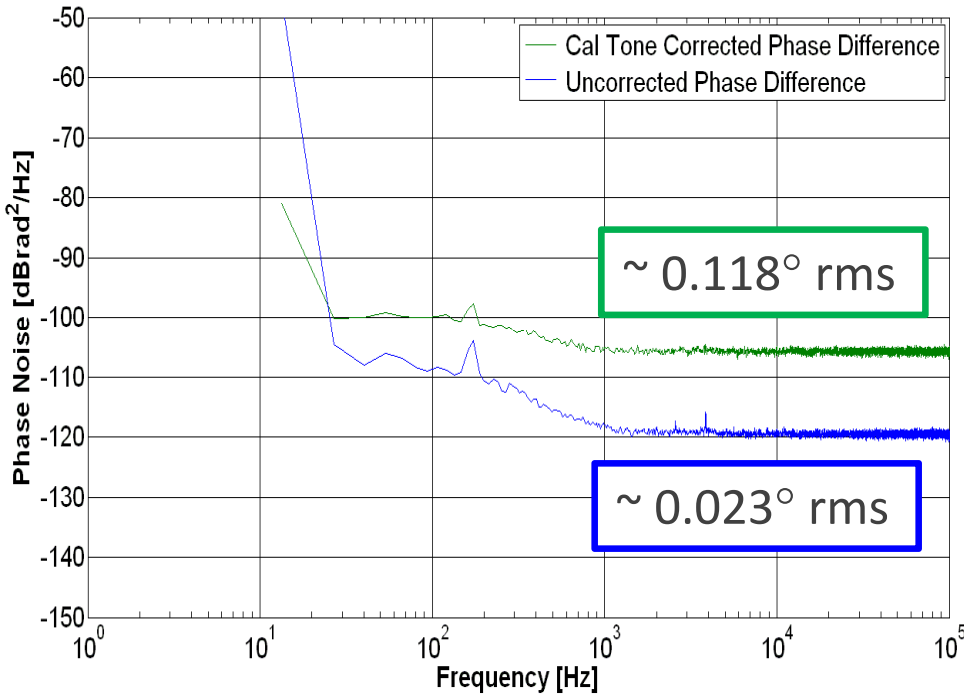


$$\Delta\phi_{meas} = (\phi_{cav} - \phi_{ref}) + \Delta\phi_{drift}$$

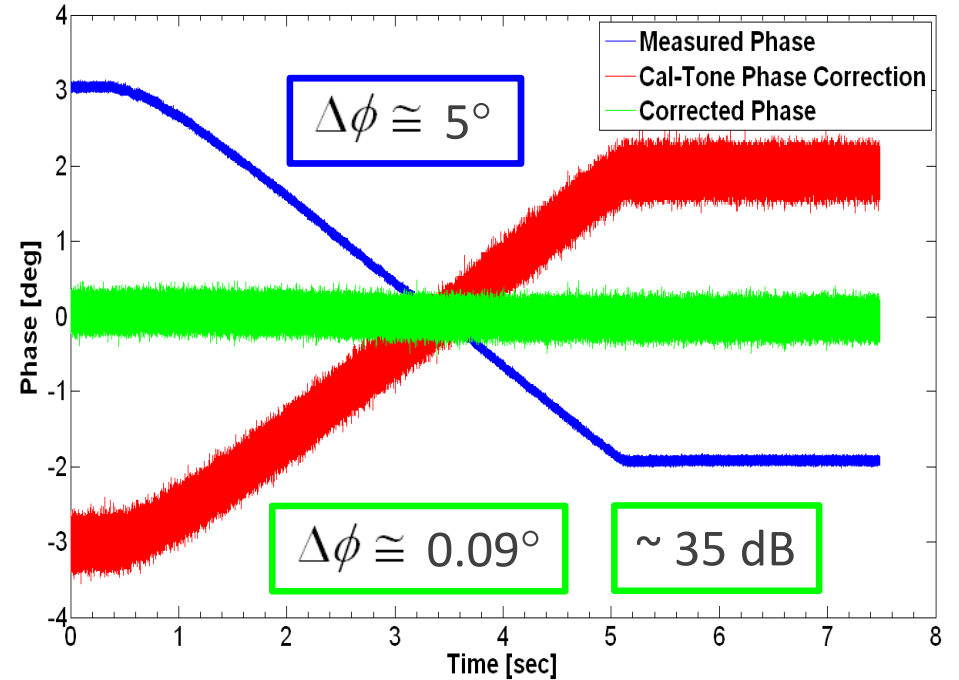
$$\Delta\phi_{calTone} = \Delta\phi_{drift}$$

$$\Delta\phi_{correct} = \Delta\phi_{meas} - \Delta\phi_{calTone}$$

LLRF4 Differential Phase Noise with & w/o Cal Tone Process

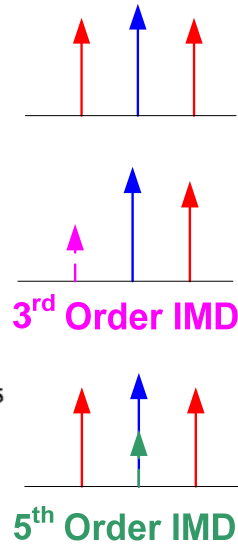
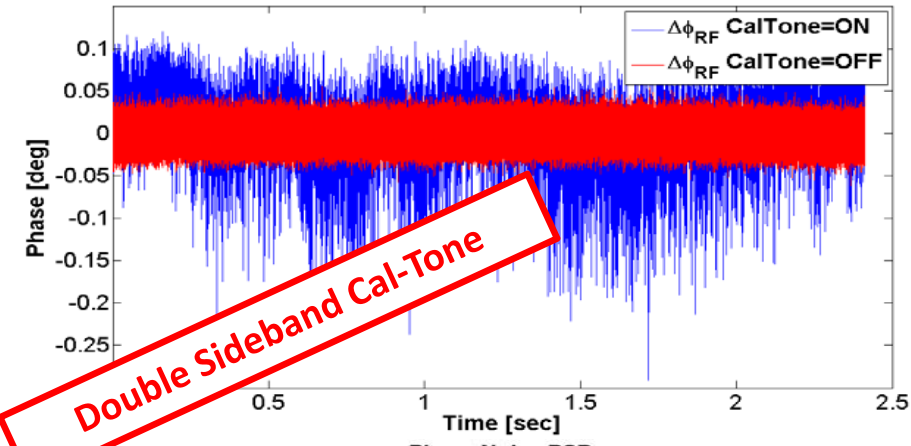


LLRF4 Cal-Tone Process Example Measurement at IF=58.68MHz

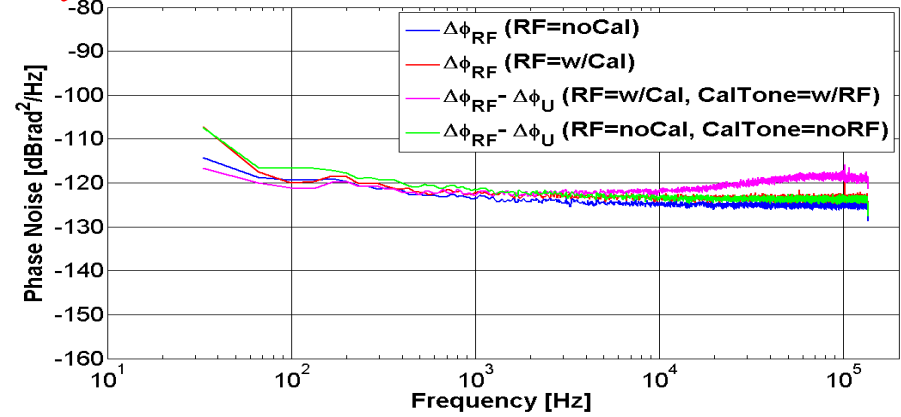
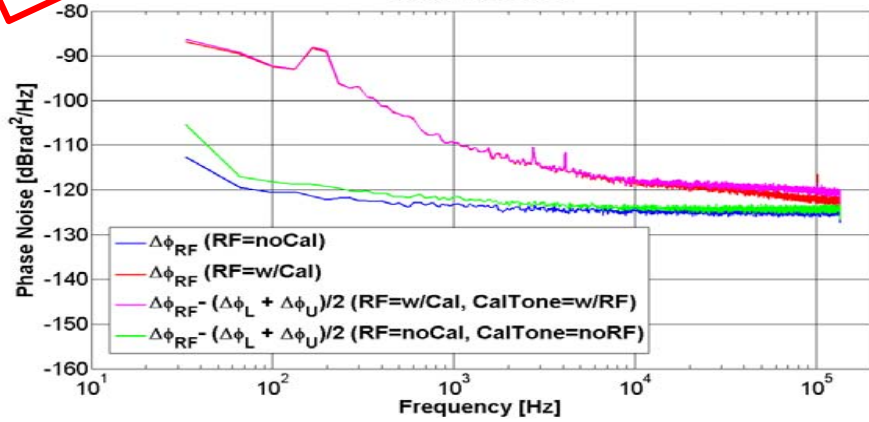
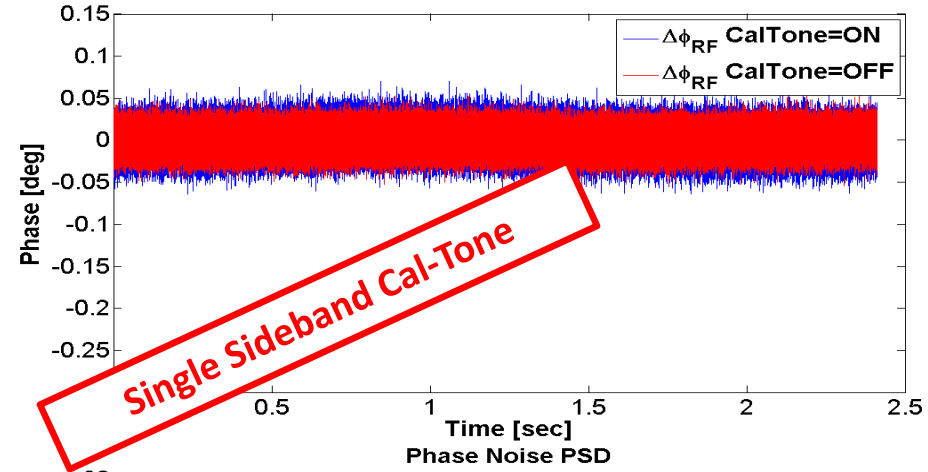


Receiver - Intermodulation Distortion

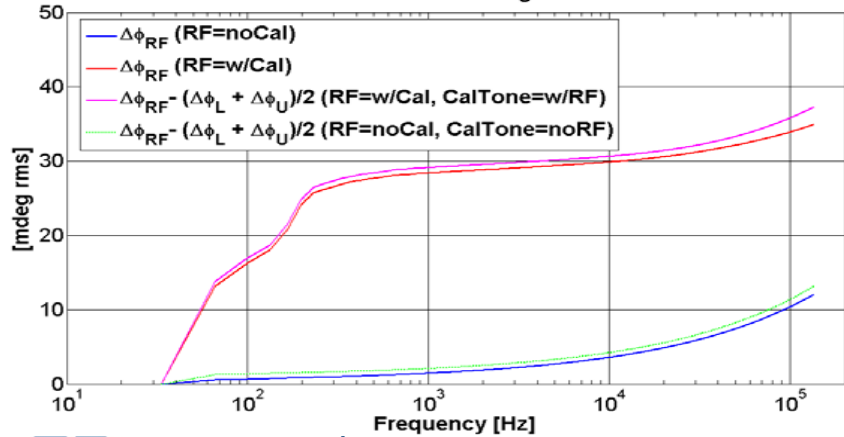
$\Delta\phi_{RF}$ Off-Line Calculation



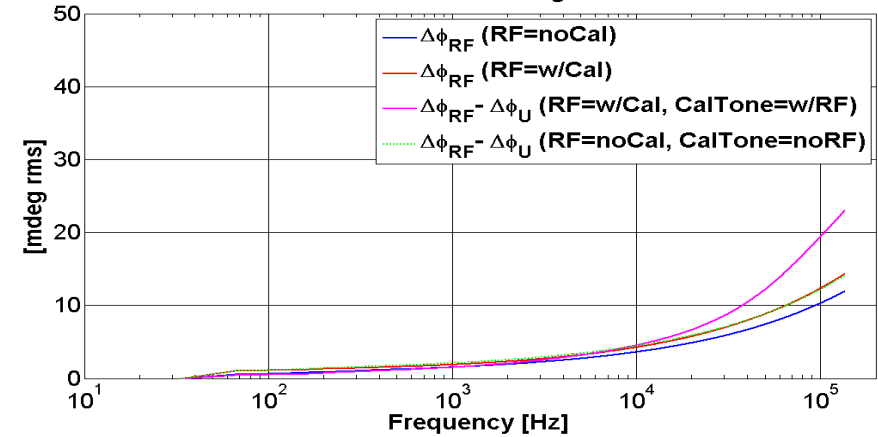
$\Delta\phi_{RF}$ Off-Line Calculation



Cumulative Integral



Cumulative Integral



Receiver - Intermodulation Distortion

For simplicity assume a Taylor series approximation (in general should use Volterra series)

$$v_o \cong a_o + a_1 v_i + a_2 v_i^2 + a_3 v_i^3$$

For a 3-tone input signal: ω_o : RF carrier ω_{LSB} : Lower side-band cal-tone
 ω_{USB} : Upper side-band cal-tone
 $\Delta \equiv \omega_o - \omega_{LSB} = \omega_{USB} - \omega_o$

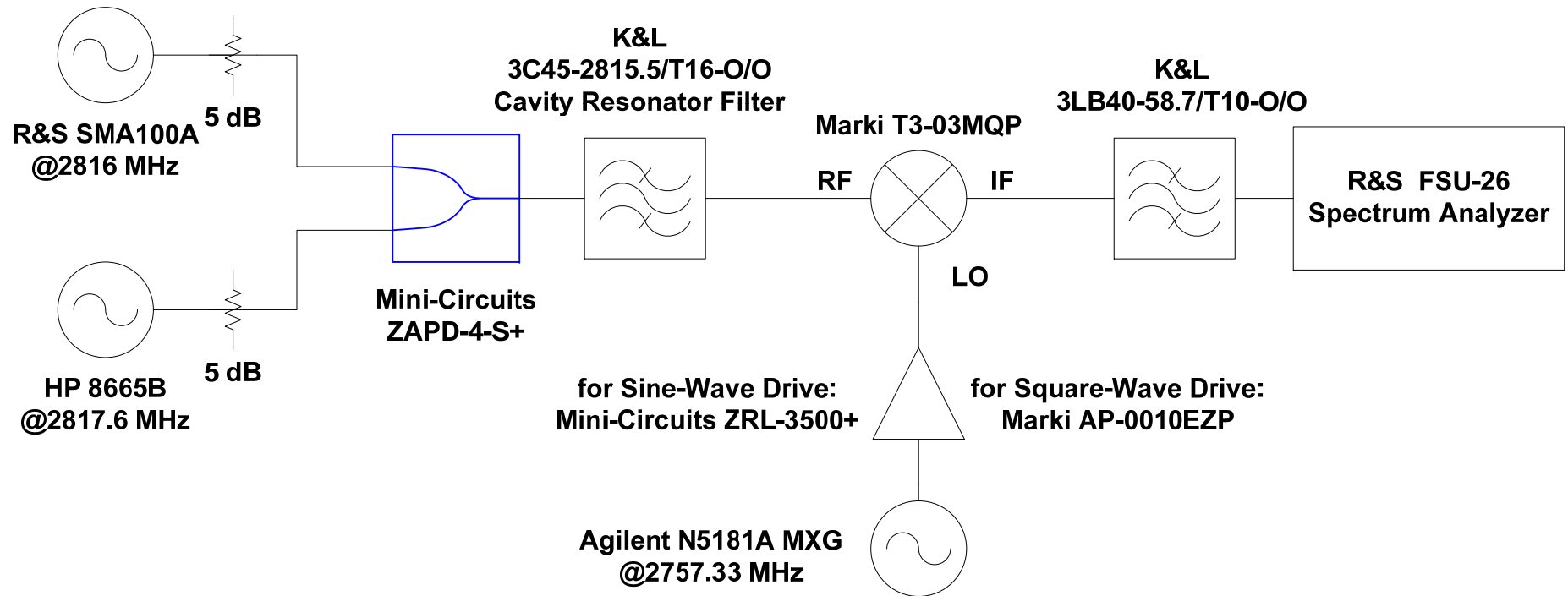
$$v_o \cong \left\{ a_1 V_{LSB} + a_3 \left[\frac{1}{2} V_{LSB} (V_{LSB}^2 + V_o^2 + V_{USB}^2) + \frac{1}{4} V_{LSB}^3 + \frac{3}{4} V_{USB} V_o^2 + V_{LSB} V_o^2 + V_{LSB} V_{USB}^2 \right] \right\} \cos \omega_{LSB} t$$

$$+ \left\{ a_1 V_o + a_3 \left[\frac{1}{2} V_o (V_{LSB}^2 + V_o^2 + V_{USB}^2) + \frac{1}{4} V_o^3 + \frac{3}{2} V_{LSB} V_o V_{USB} + V_o V_{LSB}^2 + V_o V_{USB}^2 \right] \right\} \cos \omega_o t$$

$$+ \left\{ a_1 V_{USB} + a_3 \left[\frac{1}{2} V_{USB} (V_{LSB}^2 + V_o^2 + V_{USB}^2) + \frac{1}{4} V_{USB}^3 + \frac{3}{4} V_{LSB} V_o^2 + V_{USB} V_o^2 + V_{USB} V_{LSB}^2 \right] \right\} \cos \omega_{USB} t$$

Receiver - Intermodulation Distortion

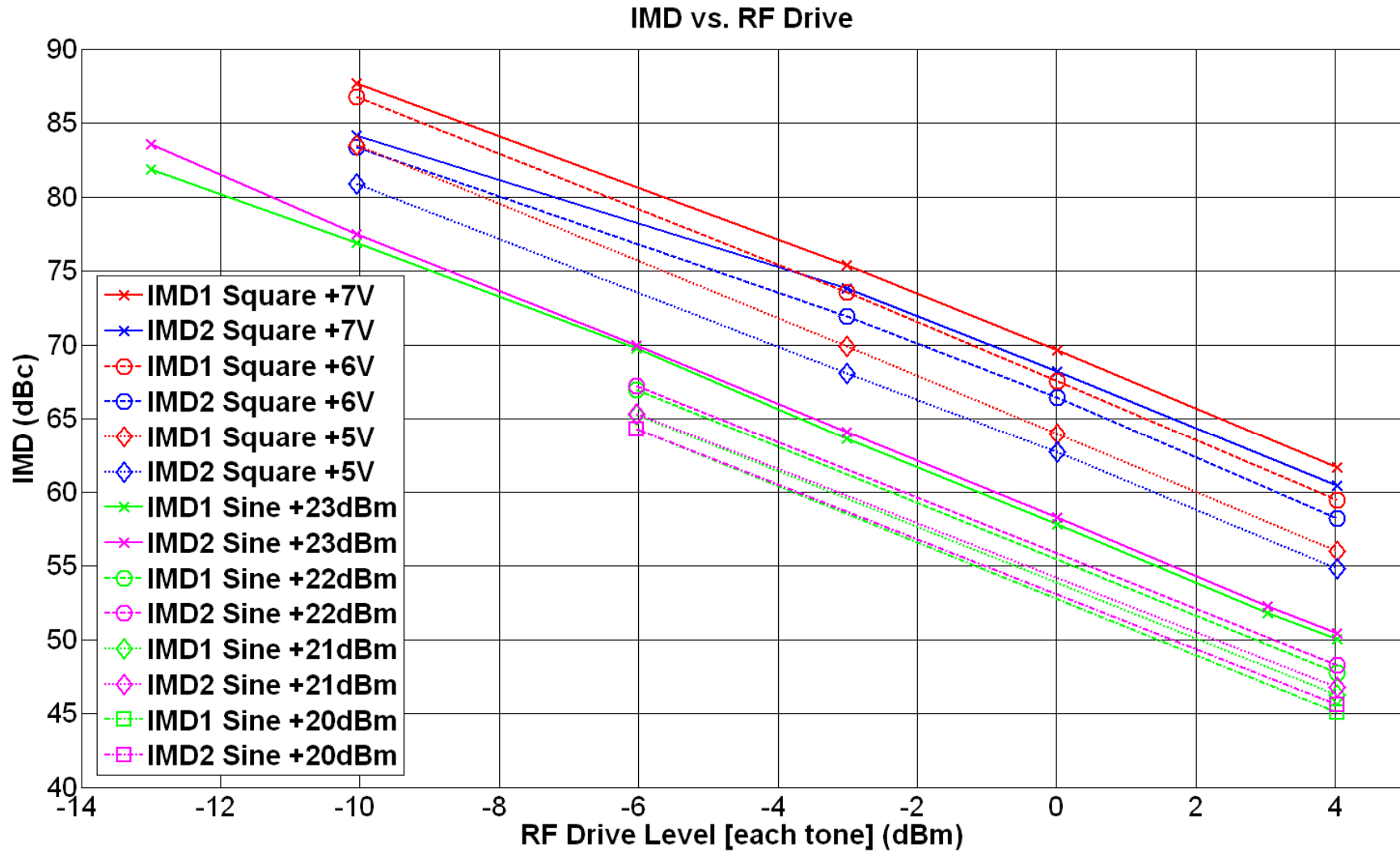
Marki T3-03MQP⁵ mixer measurements, Sine vs. Square Drive



⁵ "T3 Mixer Primer, A Mixer for the 21st Century", Ferenc Marki, Christopher Marki, http://www.markimicrowave.com/3436/T3_Mixer_Primer.aspx

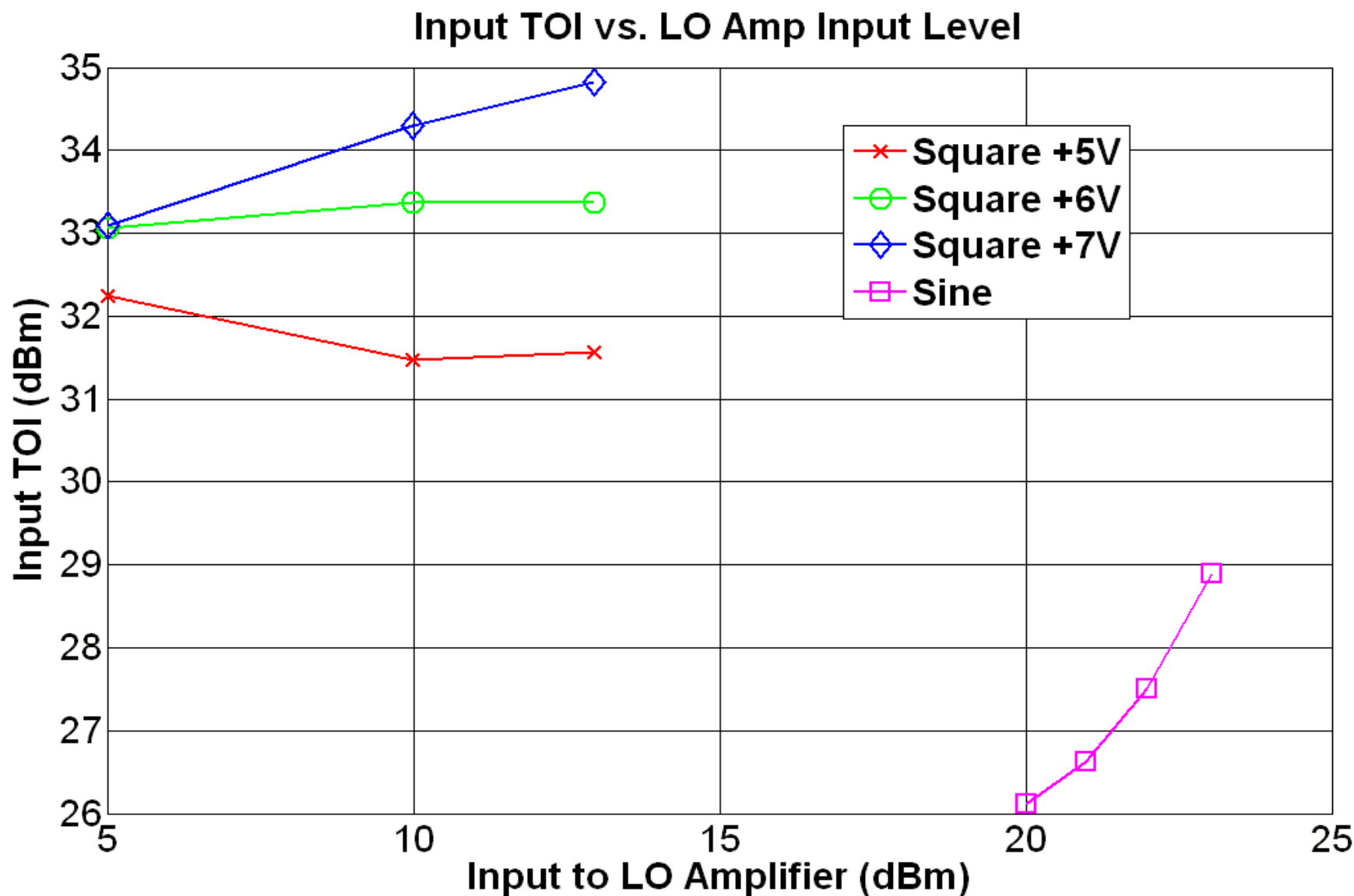
Receiver - Intermodulation Distortion

Marki T3-03MQP mixer measurements, Sine vs. Square Drive

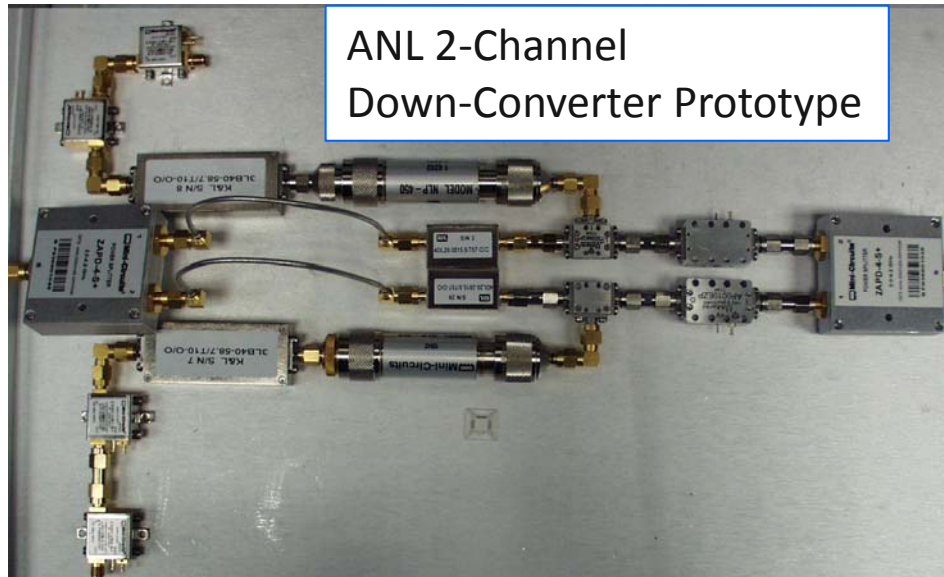
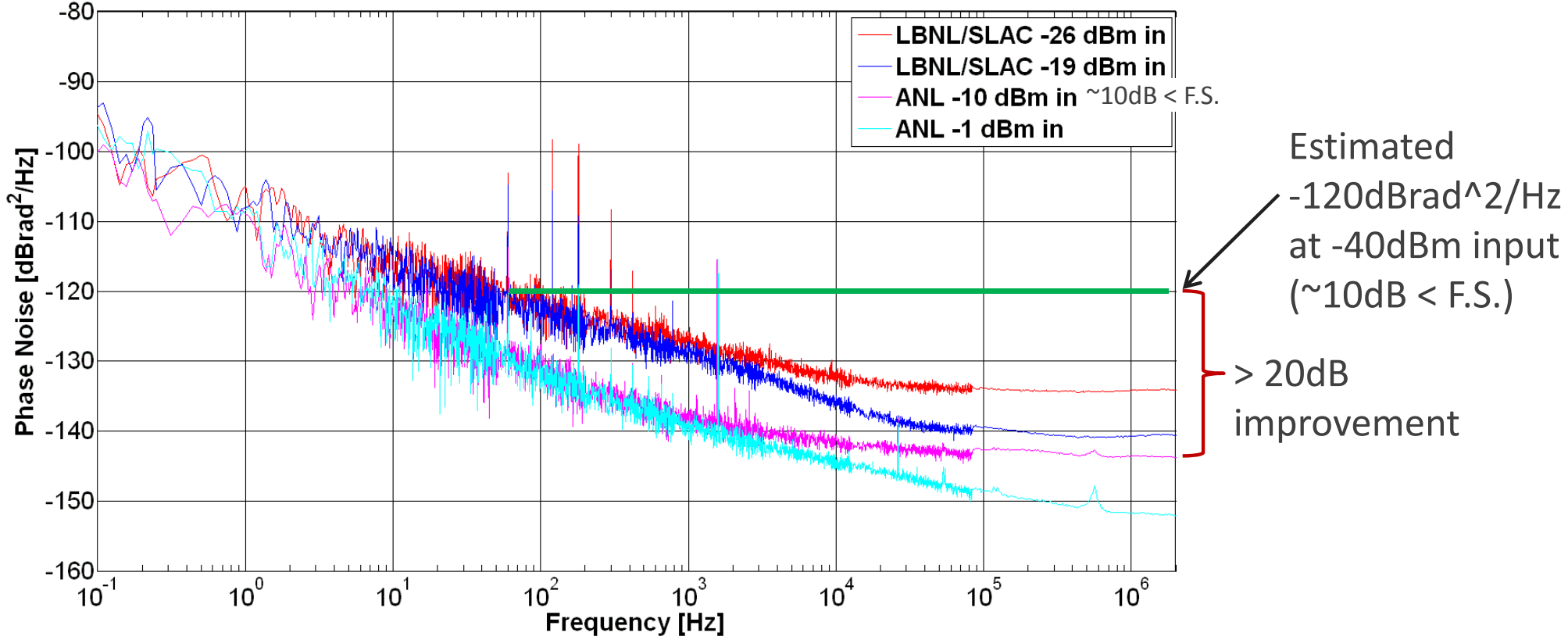


Receiver - Intermodulation Distortion

Marki T3-03MQP mixer measurements, Sine vs. Square Drive



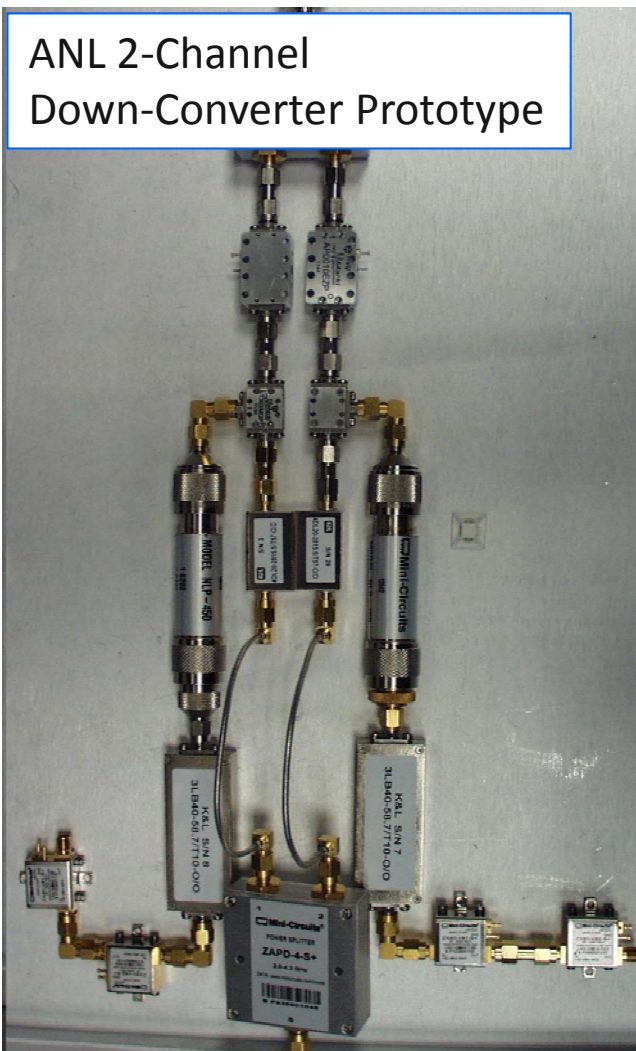
AFE Downconverter Comparison 2-Ch Differential Phase Noise



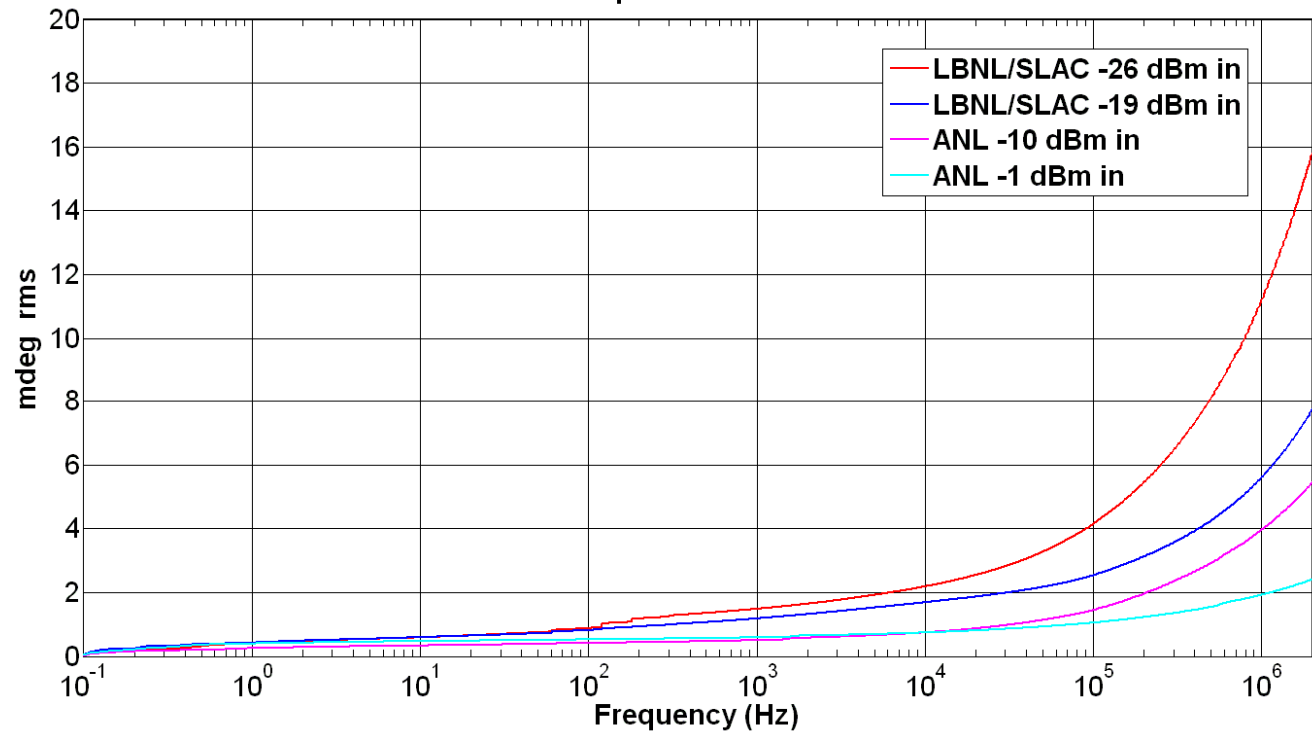
LBNL/SLAC AFE Ver.1



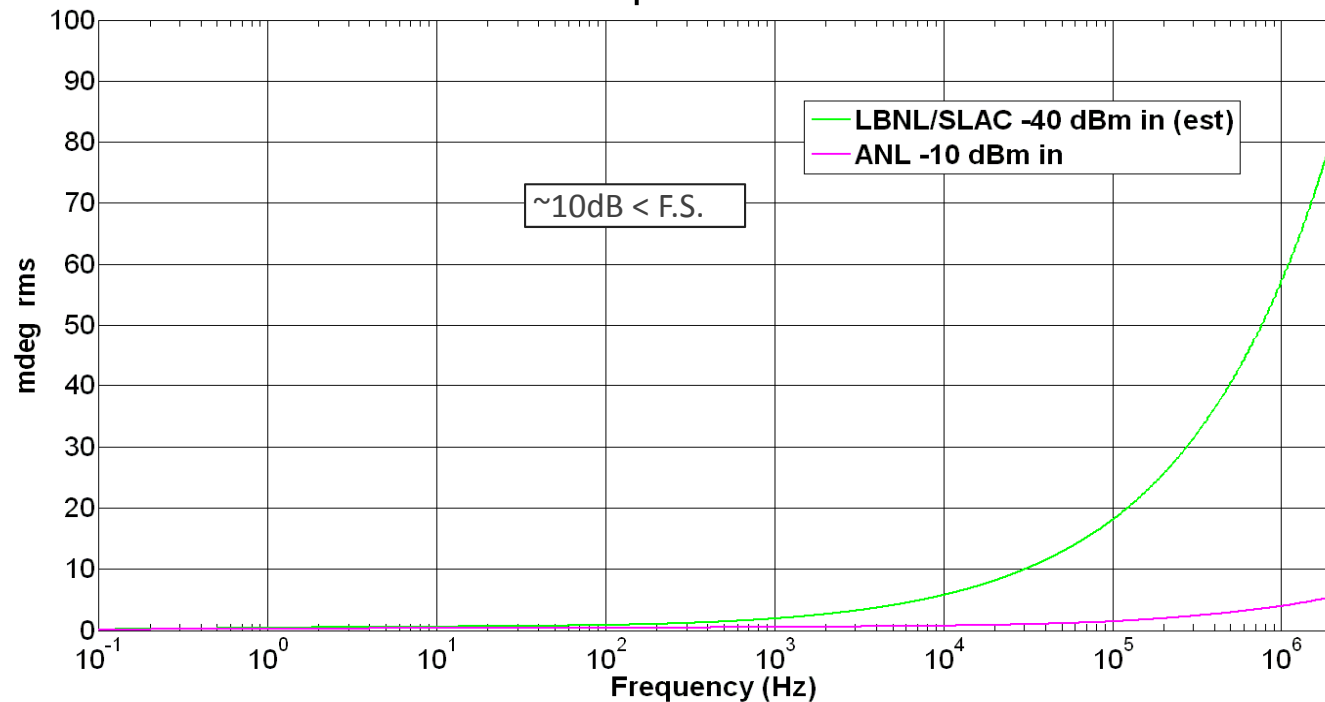
ANL 2-Channel Down-Converter Prototype



AFE Downconverter Comparison 2-Ch Differential Phase Noise



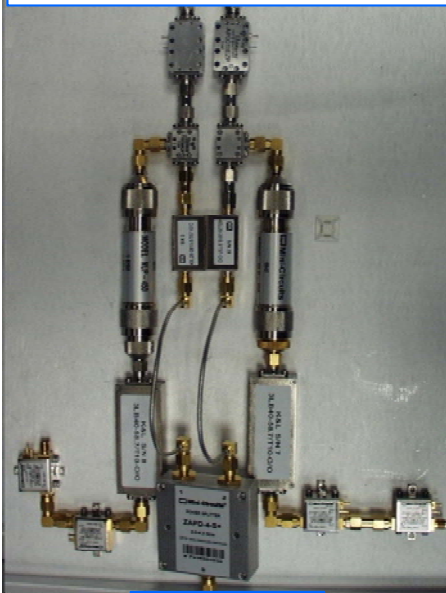
AFE Downconverter Comparison 2-Ch Differential Phase Noise



LBNL/SLAC AFE Ver.1



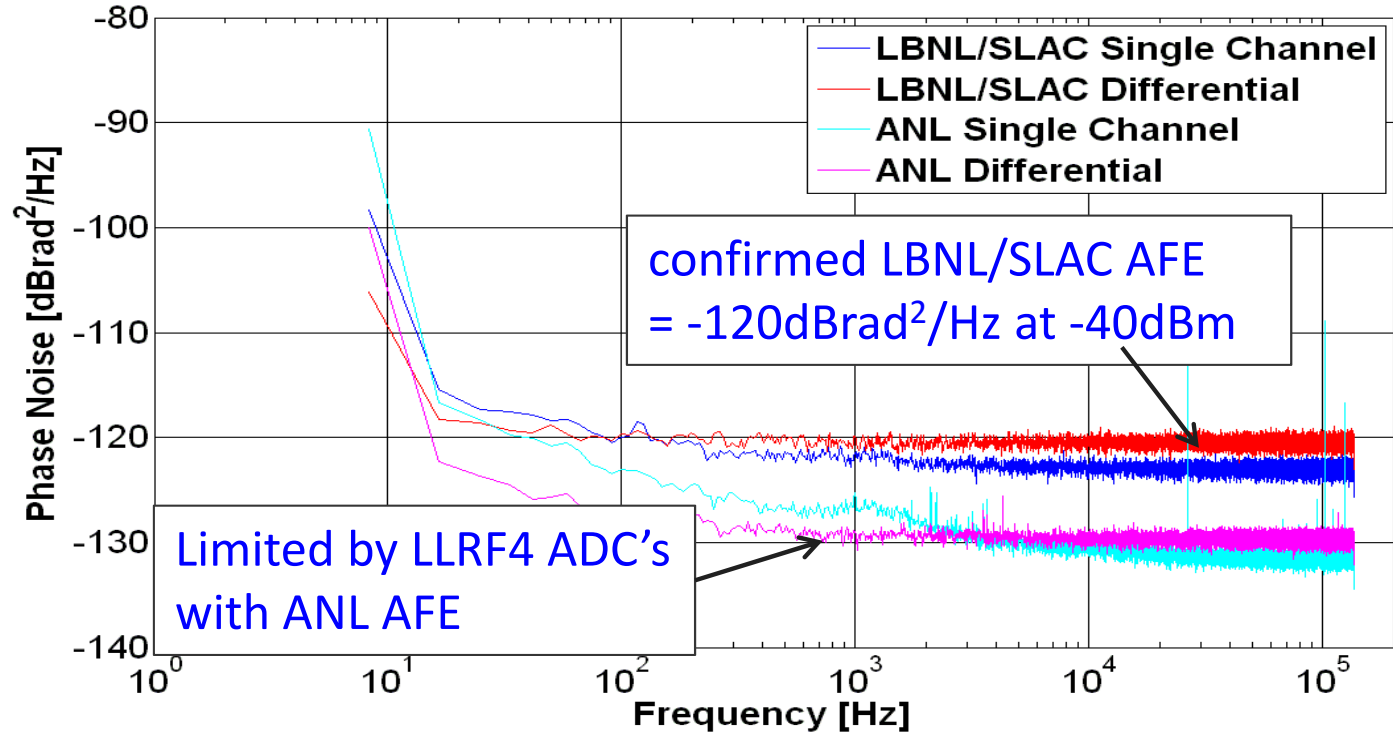
ANL 2-Channel
Down-Converter Prototype



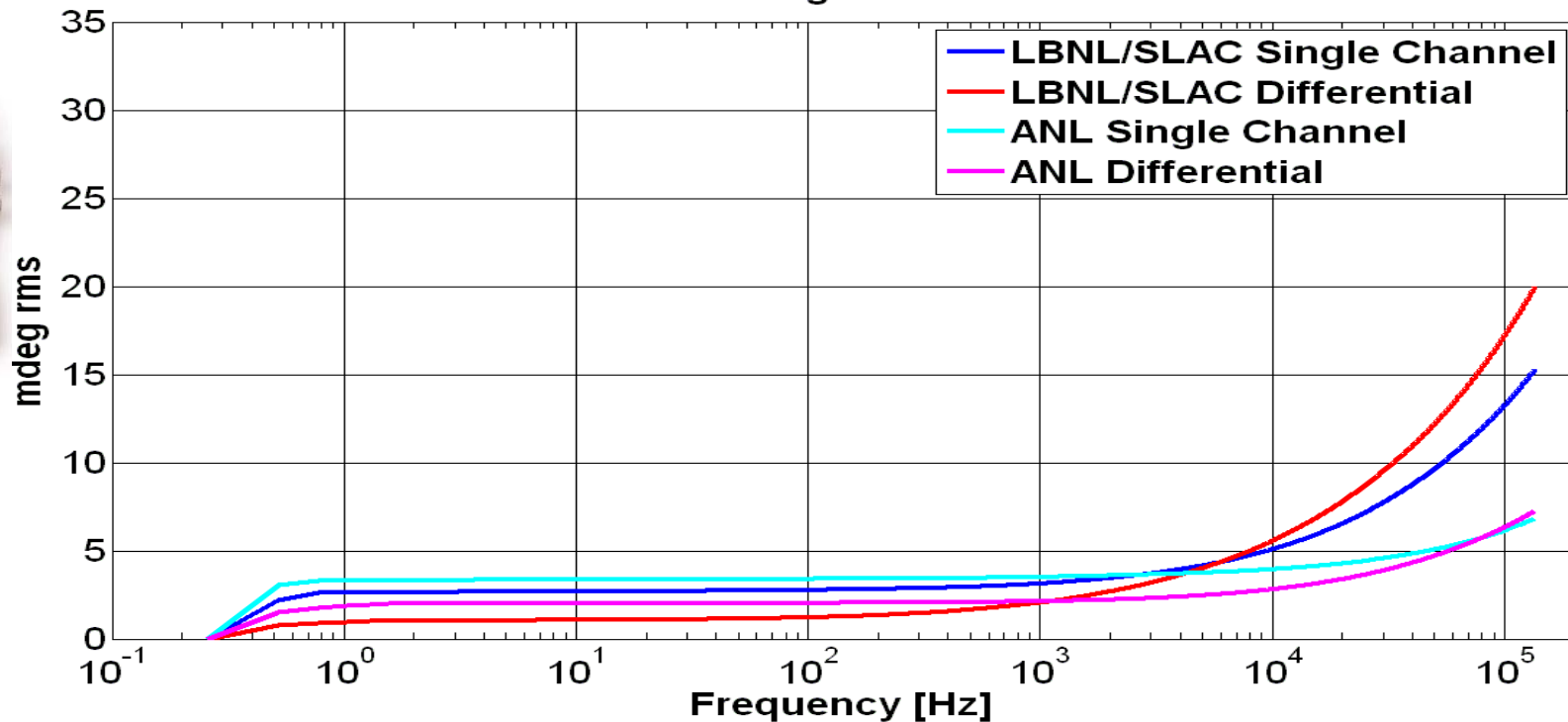
+
LLRF4



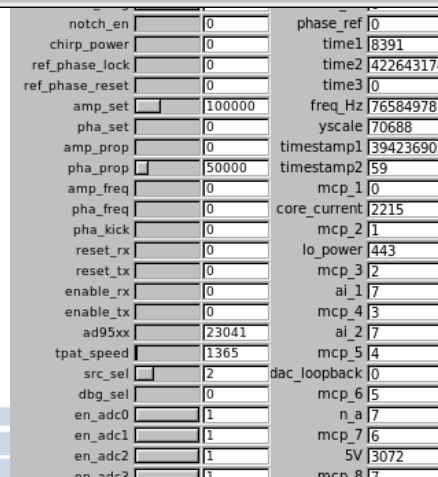
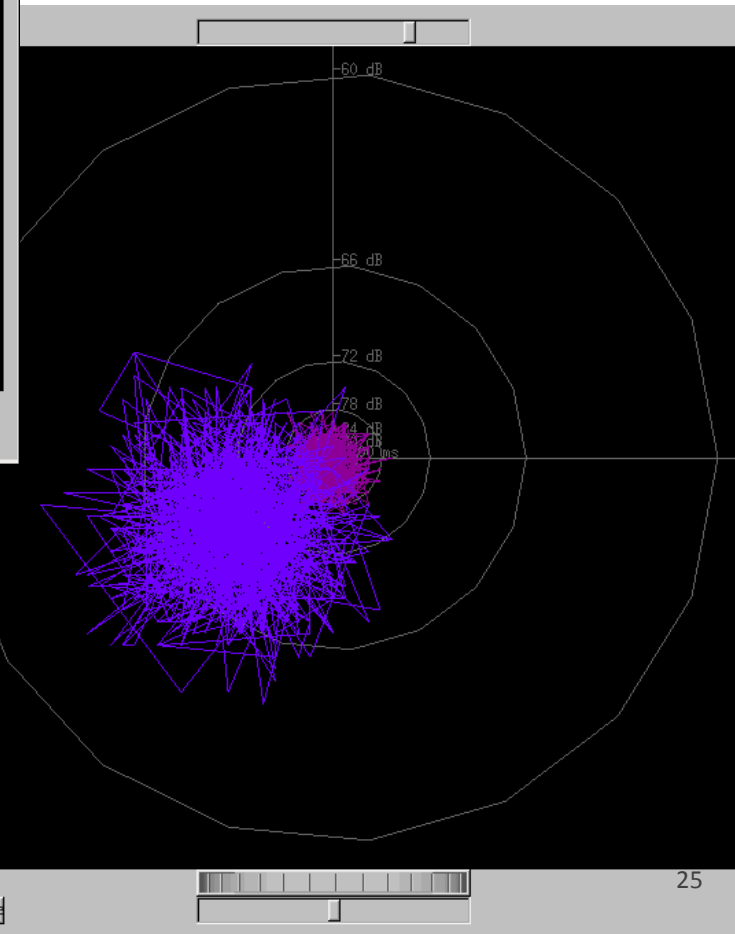
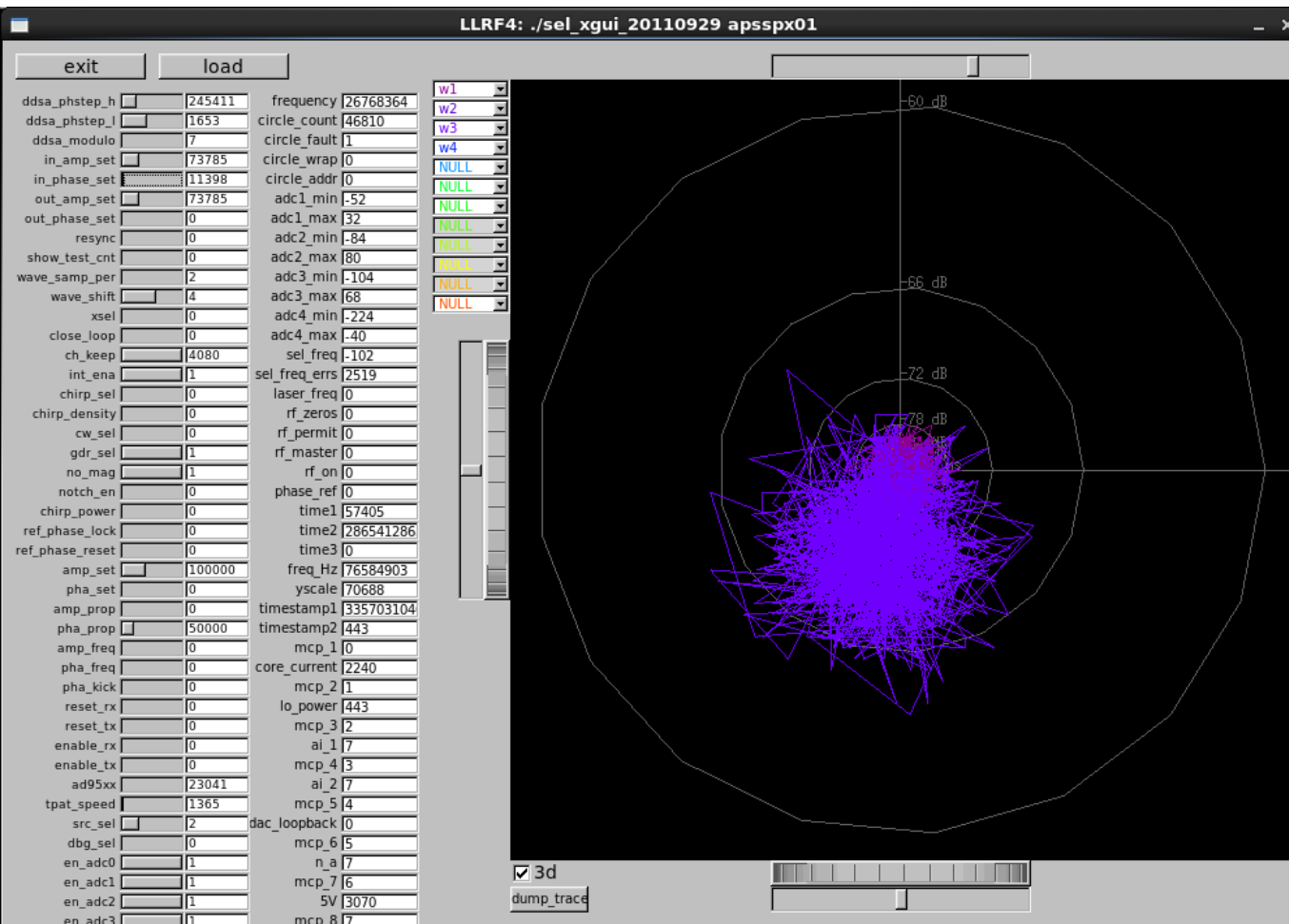
LLRF4 + AFE, Single Channel vs. Differential Phase Noise



Cumulative Integrated Phase Noise

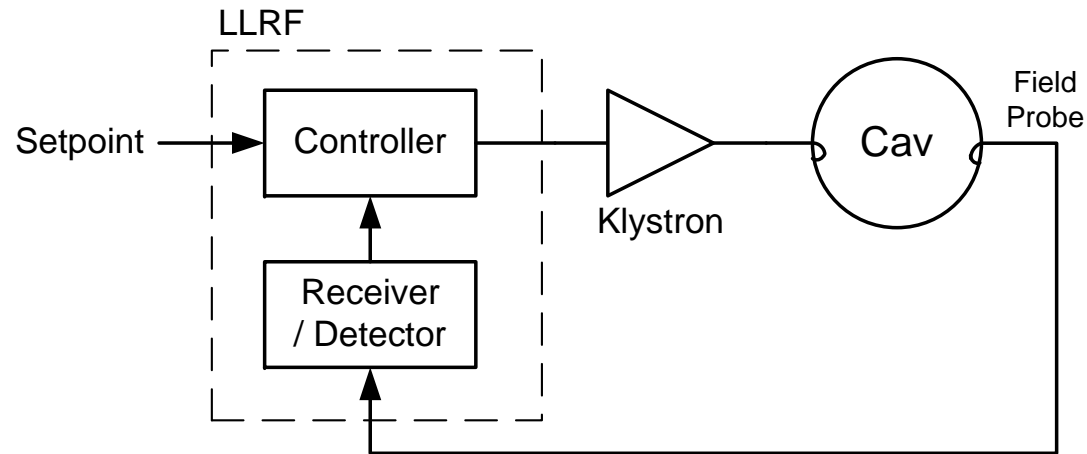


Receiver - comparison (Susceptibility to Interference)



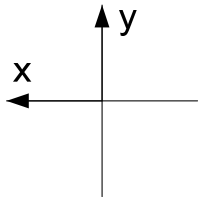
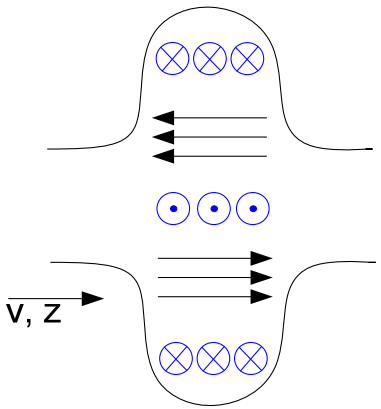
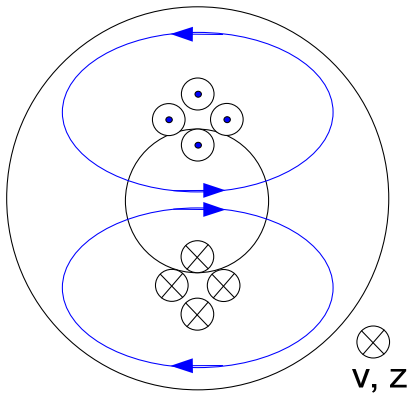
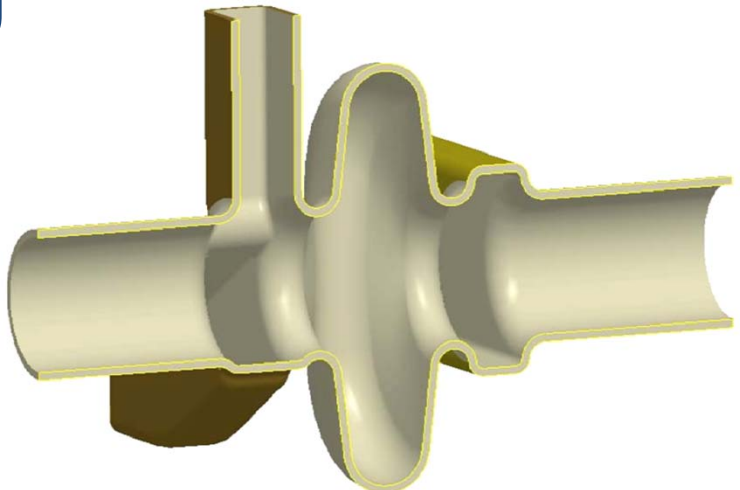
Low Level Radio Frequency (LLRF) System

Primary responsibility is to regulate the cavity field



Get to know the plant you are controlling – the cavity (**deflecting not accelerating**)

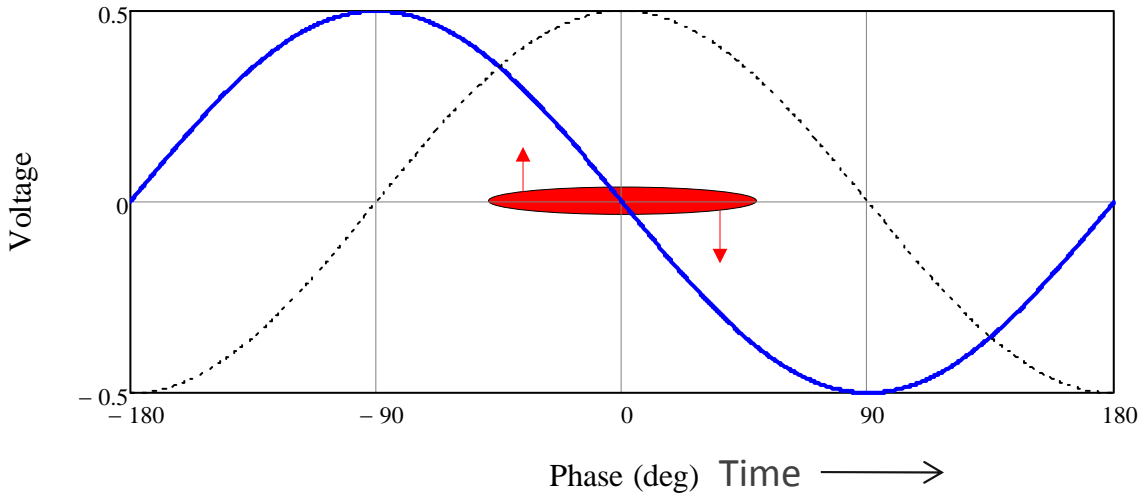
Deflecting Cavity - Beam Loading



— Magnetic Field
— Electric Field

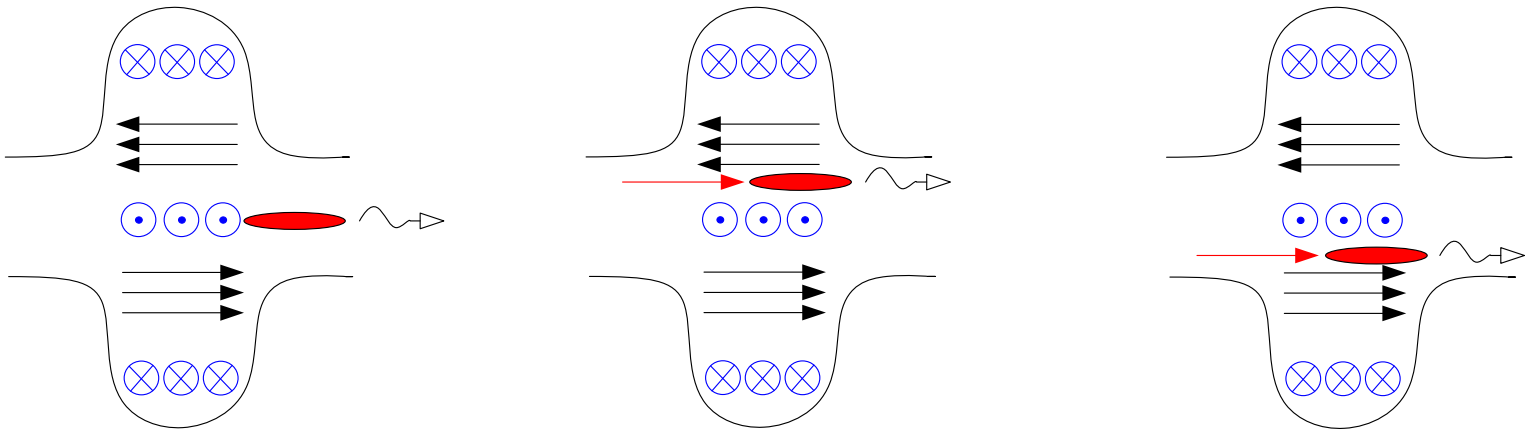
$$V_z(y) = V_m \cdot y \quad \text{Longitudinal voltage}$$

$$V_t = j \frac{V_m}{K_o} \quad \text{Vertical deflecting voltage}$$



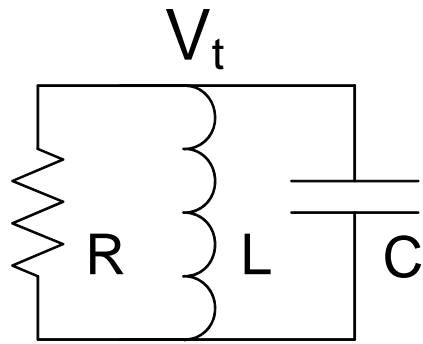
— Cavity Transverse Voltage
- - - Cavity Longitudinal Voltage / κ_o ($y > 0$)

Deflecting Cavity - Beam Loading



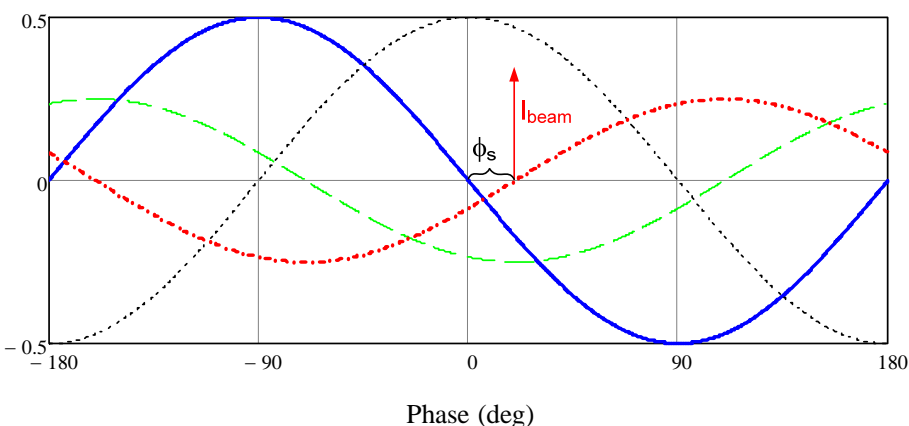
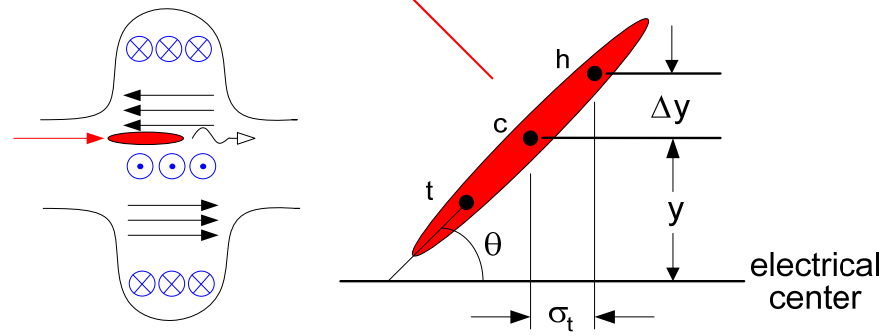
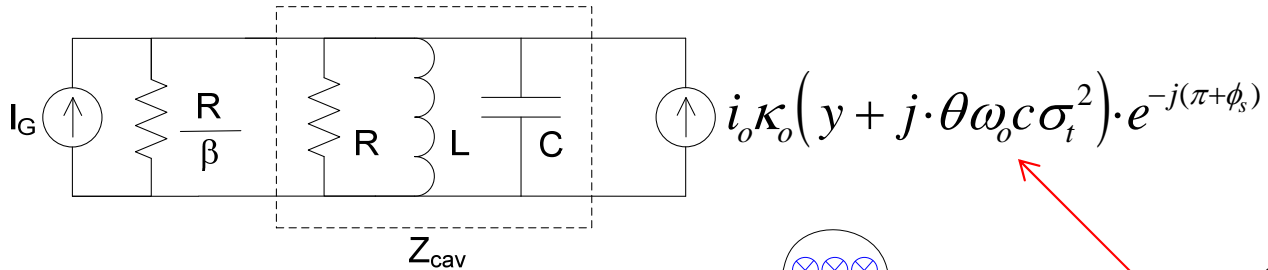
Dipole loss factor: $k_{\perp} \equiv \frac{U_{loss}}{q^2} = \frac{|V_Z(y)|^2}{4U} = \frac{\omega_r}{2} \left(\frac{R}{Q} \right)' (\kappa_o y)^2$

Circuit definition R/Q: $\left(\frac{R}{Q} \right)' = \frac{V_t^2}{2\omega_r U} = 17.8 \Omega$

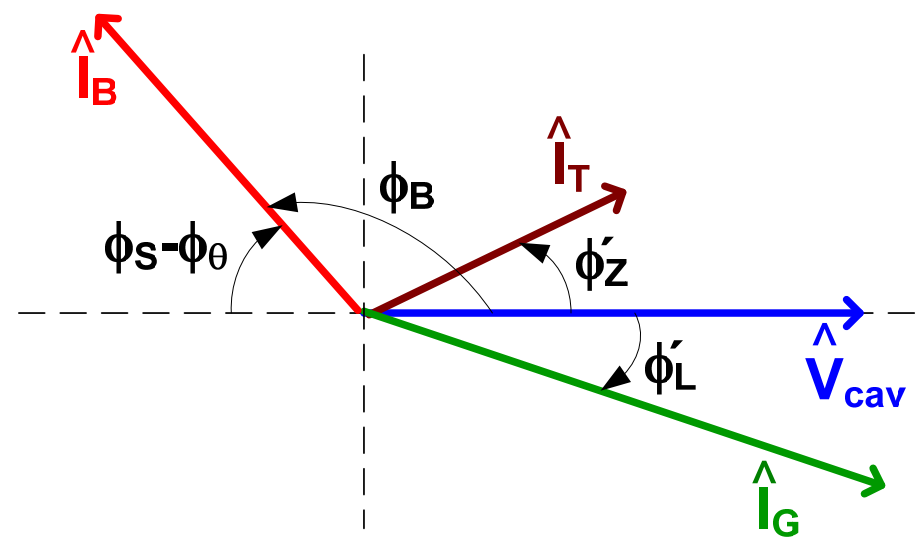


$$U_{loss} = q^2 k_{\perp} = \frac{1}{2} C V_t^2 \quad \Rightarrow V_t^2 = \left(\frac{q \cdot \kappa_o y}{C} \right)^2 \quad \Rightarrow q_{eq} = |q \cdot \kappa_o y|$$

Deflecting Cavity - Beam Loading^{5,6}

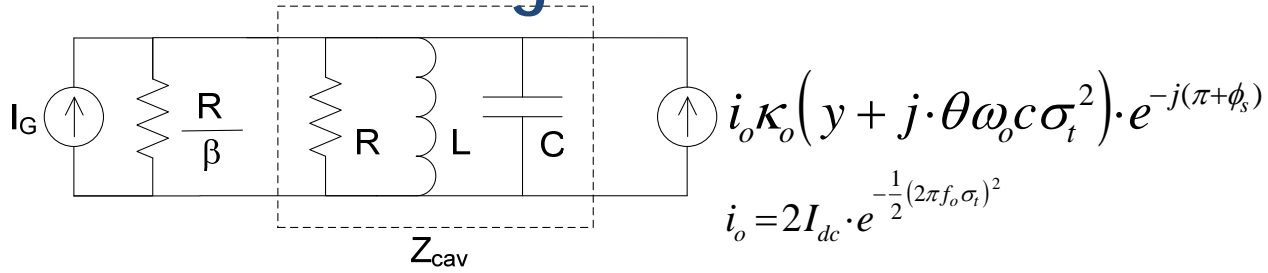


- Cavity Transverse Voltage
- - - Cavity Longitudinal Voltage
- · - Beam Induced Longitudinal Voltage ($y > 0$)
- · · Beam Induced Transverse Voltage ($y > 0$)



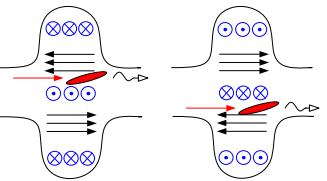
⁵ Berenc, "An Equivalent Circuit Model ..", ICMS# APS_1405978
⁶ Decker, "..Tilt Monitor", DIAG-TN-2010-10, ICMS# APS_1417048

Deflecting Cavity - Beam Loading



$$P_g^+ = \frac{V_t^2}{8\beta(R/Q)'Q_o} \cdot \left[\left(\beta + 1 + \frac{P_B}{P_{cav}} \right)^2 + \left(2Q_o \frac{(\Delta f + \delta f_m)}{f_r} + \frac{P_B}{P_{cav}} \tan \phi_s \right)^2 \right]$$

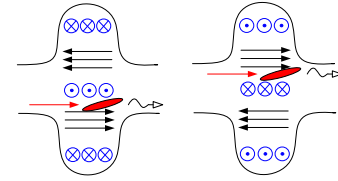
$$P_B = -\frac{1}{2} V_t \hat{I}_B \cos \phi_B$$



$V_t \cdot y > 0$

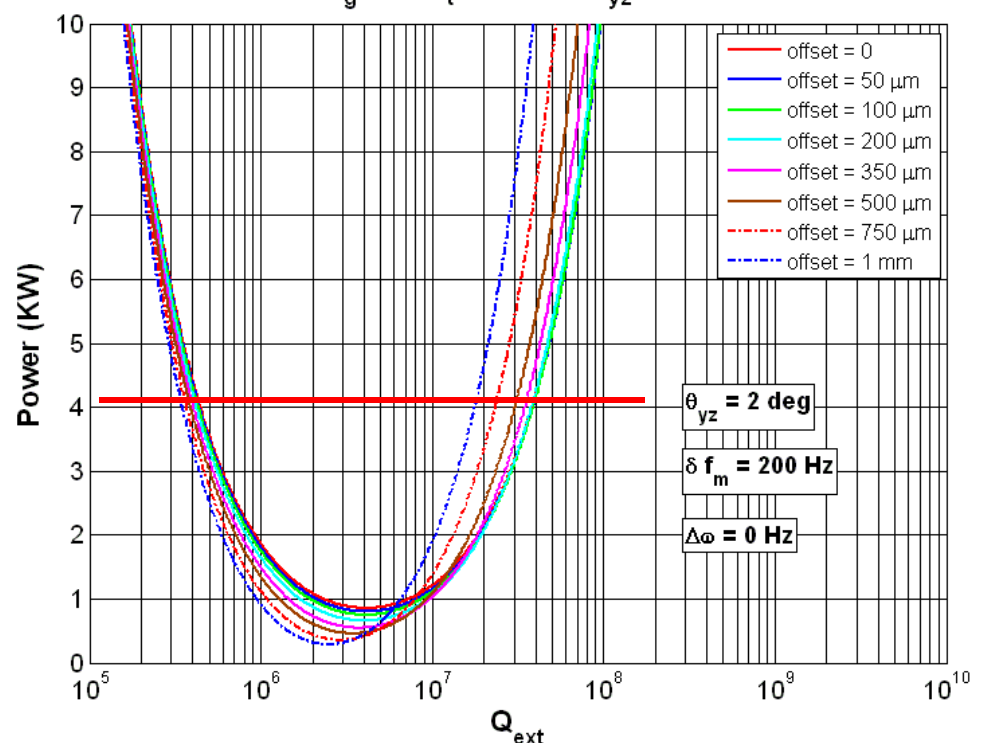
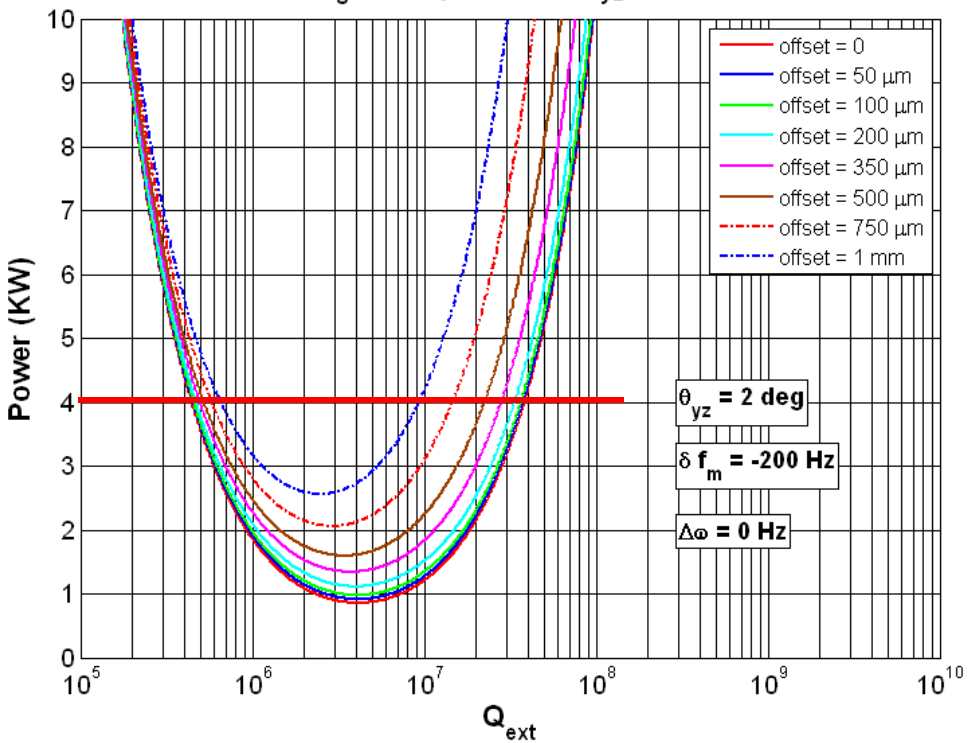
$I_{DC} = 100mA$, $V_{cav} = 0.5MV$

$V_t \cdot y < 0$

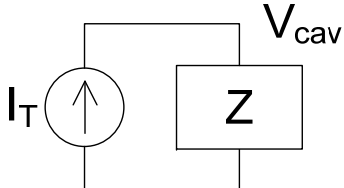


P_g^+ for $V_t y > 0$ and $\theta_{yz} = 2deg$

P_g^+ for $V_t y < 0$ and $\theta_{yz} = 2deg$



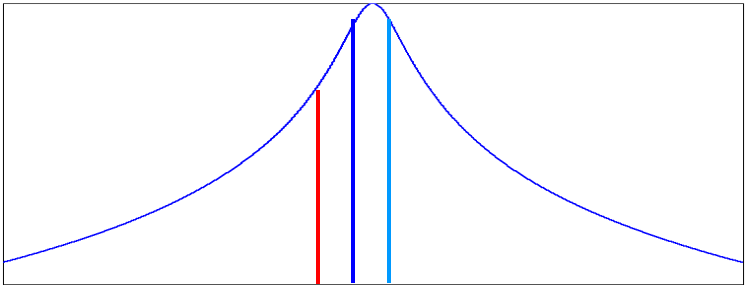
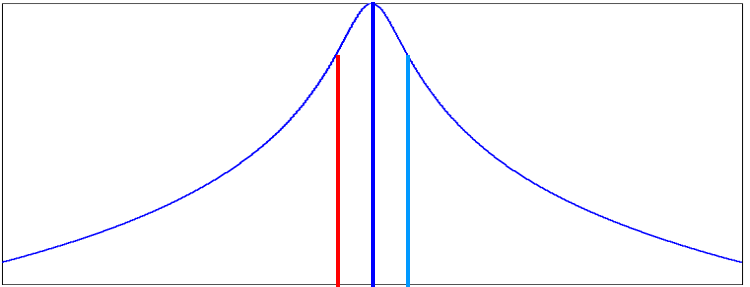
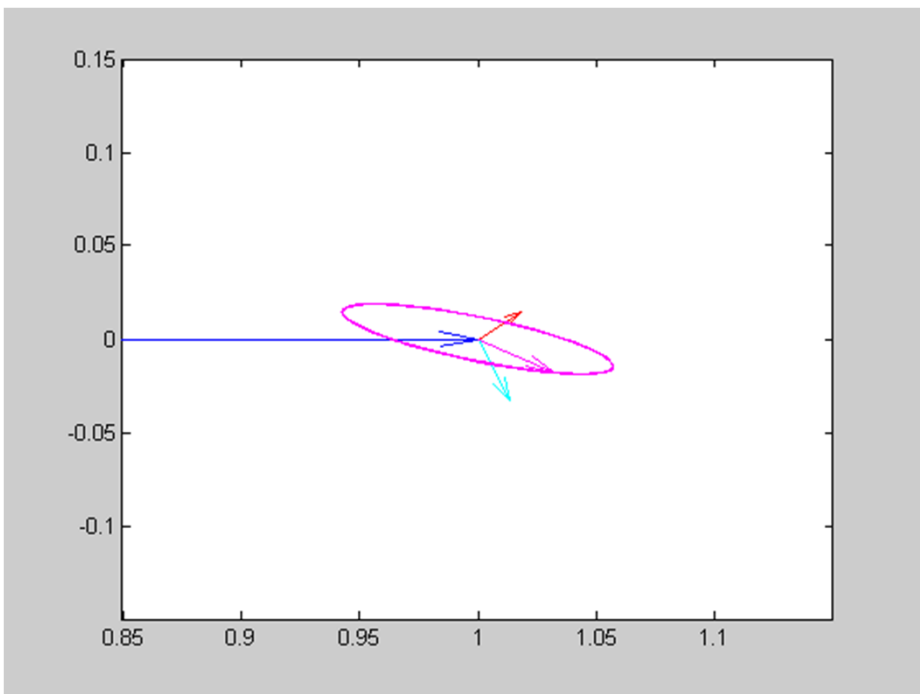
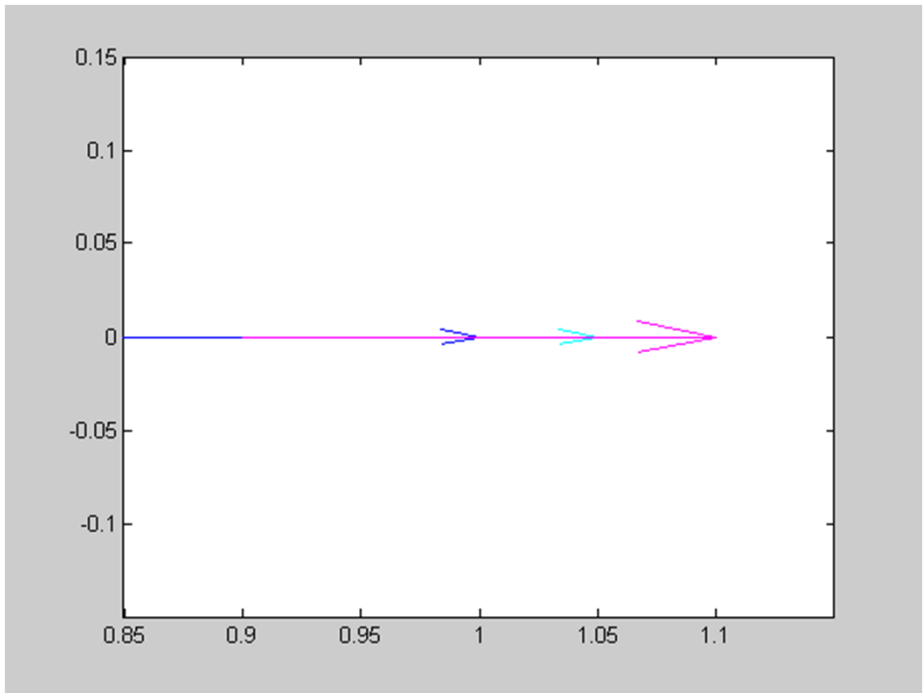
Deflecting Cavity - Dynamic Behavior



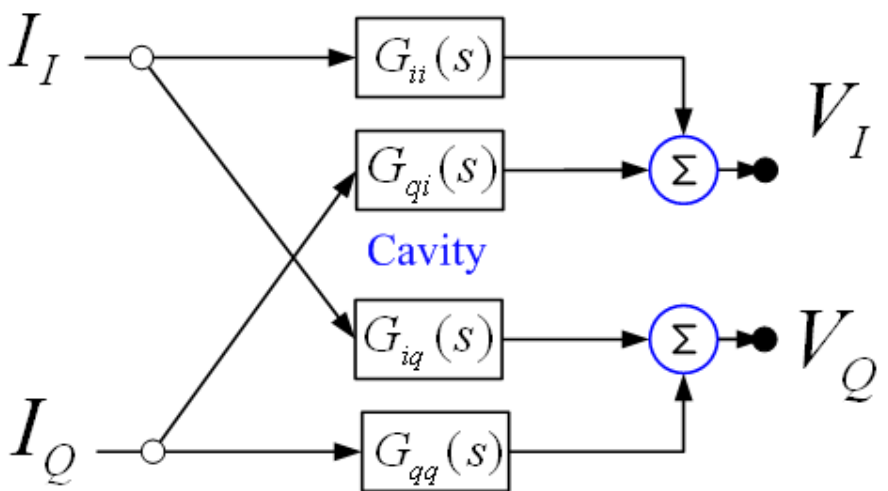
$$I_T(t) = I_r \cos \omega_{RF} t + i_I(t) \cos \omega_{RF} t - i_Q(t) \sin \omega_{RF} t$$

$$V_{cav}(t) = V_r \cos(\omega_{RF} t + \phi_Z) + v_I(t) \cos(\omega_{RF} t + \phi_Z) - v_Q(t) \sin(\omega_{RF} t + \phi_Z)$$

In-general I/Q modulations of I_T each cause both I/Q modulations of V_{cav}



Deflecting Cavity - Dynamic Behavior



$$G_{ii}(s) = G_{qq}(s) = \frac{1}{2} \left[\frac{Z(j\omega_{RF} + s)}{N} + \frac{Z^*(j\omega_{RF} - s)}{N^*} \right]$$

$$G_{iq}(s) = -G_{qi}(s) = -\frac{j}{2} \left[\frac{Z(j\omega_{RF} + s)}{N} - \frac{Z^*(j\omega_{RF} - s)}{N^*} \right]$$

Polar Coordinates

$$I_T(t) = I_r \cos \omega_{RF} t + \alpha_I(t) I_r \cos \omega_{RF} t - \phi_I(t) I_r \sin \omega_{RF} t$$

$$N_{polar} = |Z(j\omega_{RF})| e^{+j\phi_Z} = Z(j\omega_{RF})$$

$$G_{\alpha\alpha}(s) = G_{\phi\phi}(s) = \frac{\sigma(s + \sigma(1 + \tan^2 \phi_Z))}{s^2 + 2\sigma s + \sigma^2(1 + \tan^2 \phi_Z)}$$

$$G_{\alpha\phi}(s) = -G_{\phi\alpha}(s) = \frac{-\sigma \tan \phi_Z s}{s^2 + 2\sigma s + \sigma^2(1 + \tan^2 \phi_Z)}$$

classical "Pedersen/Boussard Equations"

Cartesian Coordinates

$$I_T(t) = I_r \cos \omega_{RF} t + i_I(t) \cos \omega_{RF} t - i_Q(t) \sin \omega_{RF} t$$

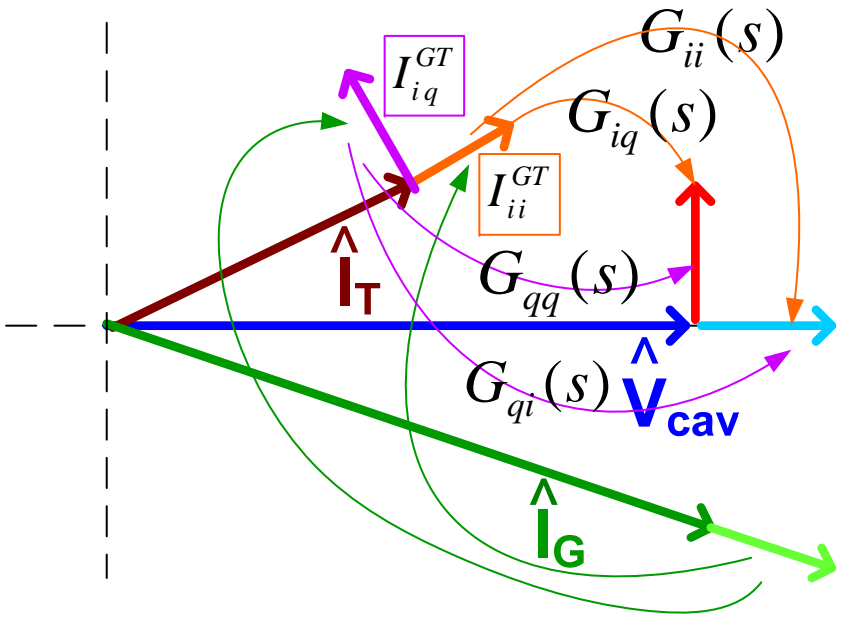
$$N_{Cartesian} = e^{+j\phi_Z}$$

$$G_{ii}(s) = G_{qq}(s) = \frac{\sigma R \cos \phi_Z (s + \sigma(1 + \tan^2 \phi_Z))}{s^2 + 2\sigma s + \sigma^2(1 + \tan^2 \phi_Z)}$$

$$G_{iq}(s) = -G_{qi}(s) = \frac{-\sigma R \sin \phi_Z}{s^2 + 2\sigma s + \sigma^2(1 + \tan^2 \phi_Z)}$$

Modern I/Q Equations

Deflecting Cavity - Dynamic Behavior



$$\begin{bmatrix} V_I^G(s) \\ V_Q^G(s) \end{bmatrix} = \begin{bmatrix} G_{ii}^G(s) & G_{qi}^G(s) \\ G_{iq}^G(s) & G_{qq}^G(s) \end{bmatrix} \begin{bmatrix} I_I^G(s) \\ I_Q^G(s) \end{bmatrix}$$

Use vector projection techniques to find the transfer functions from generator current and beam current modulations. Generator Current in-phase modulation is shown here. Total of 15 transfer functions describe the cavity.

Polar Coordinates

for discussion "NO DETUNING"

$$G_{\alpha\phi}^G(s) = -G_{\phi\alpha}^G(s) = 0$$

$$G_{\alpha\alpha}^G(s) = G_{\phi\phi}^G(s) = (1+Y) \frac{\sigma}{s + \sigma}$$

Cartesian Coordinates

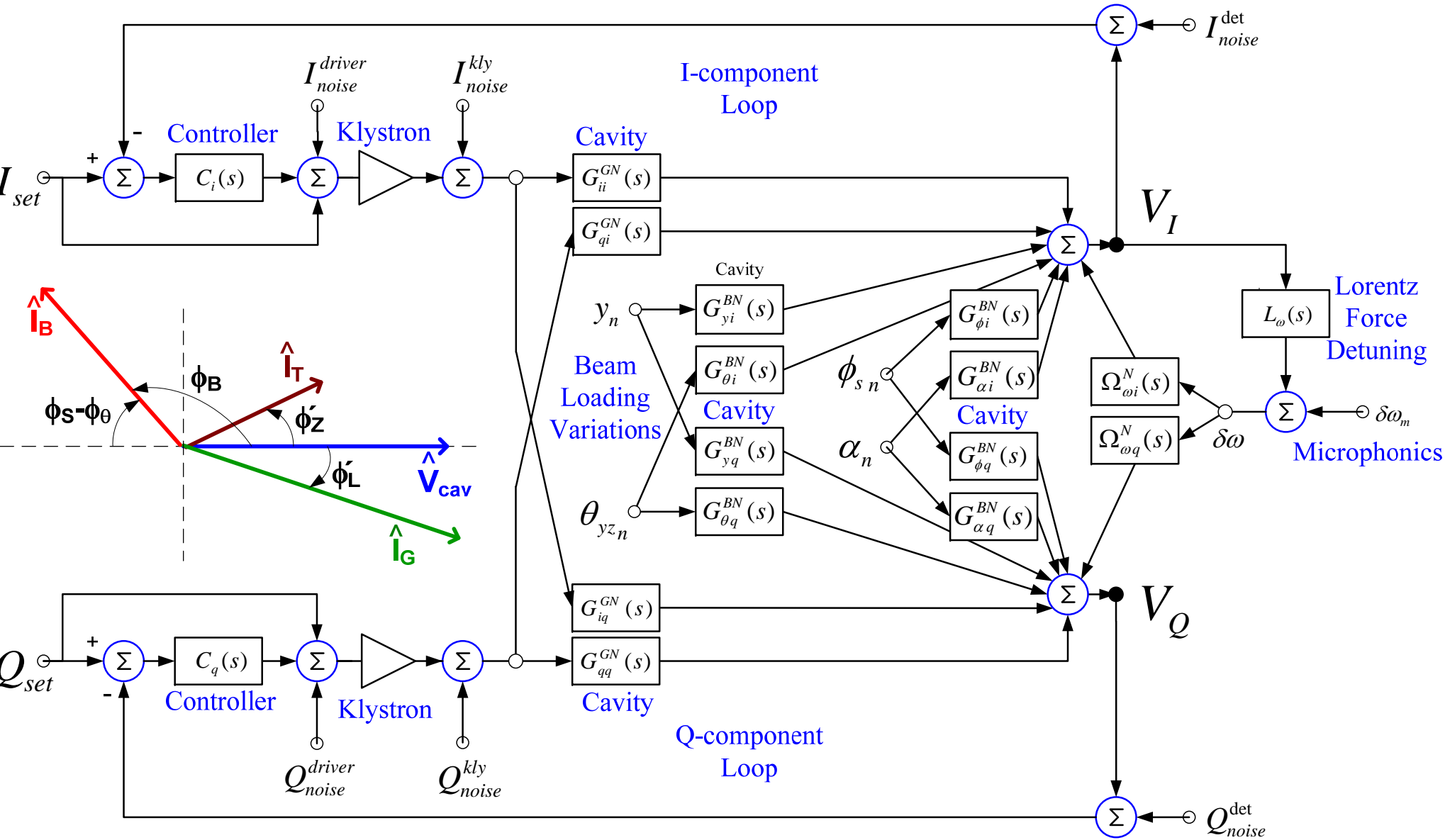
for discussion "NO DETUNING"

$$G_{iq}^G(s) = -G_{qi}^G(s) = 0$$

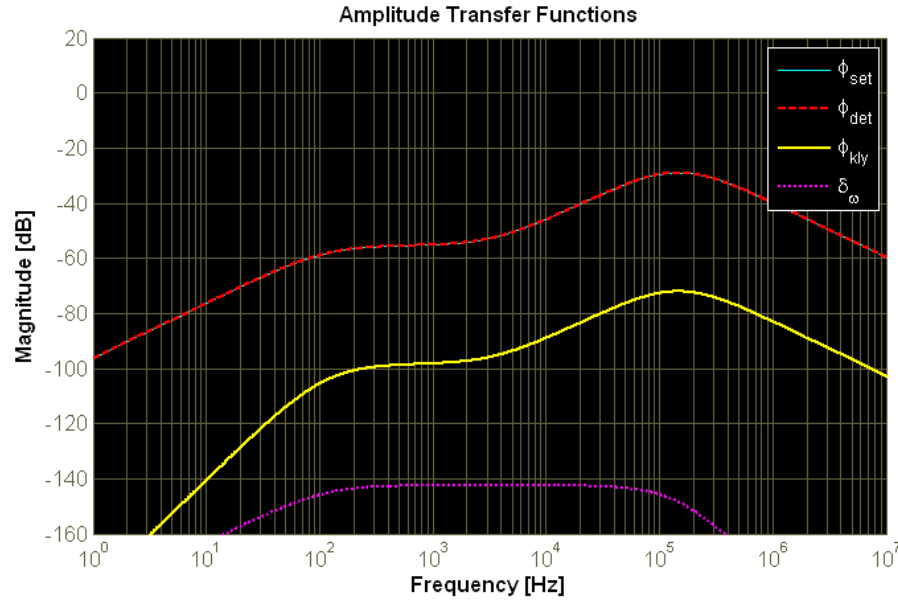
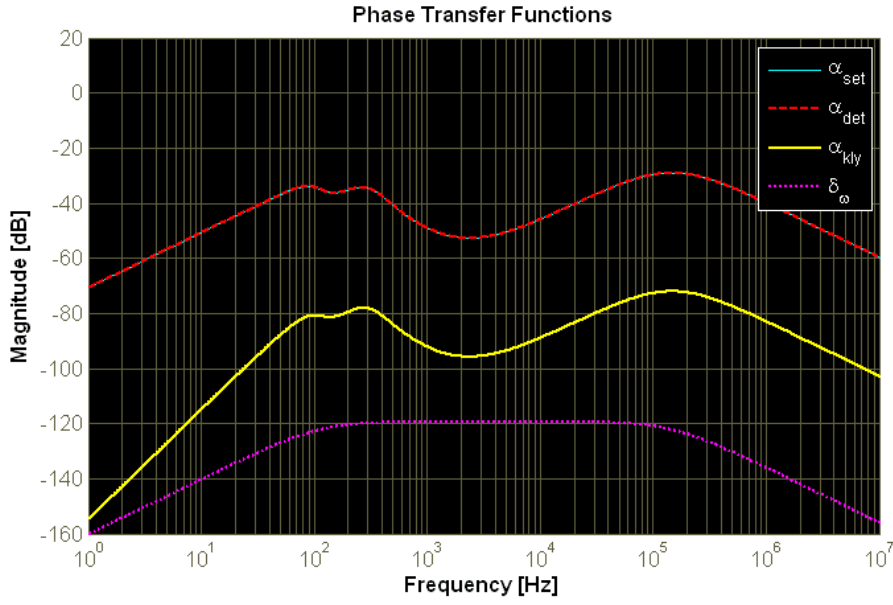
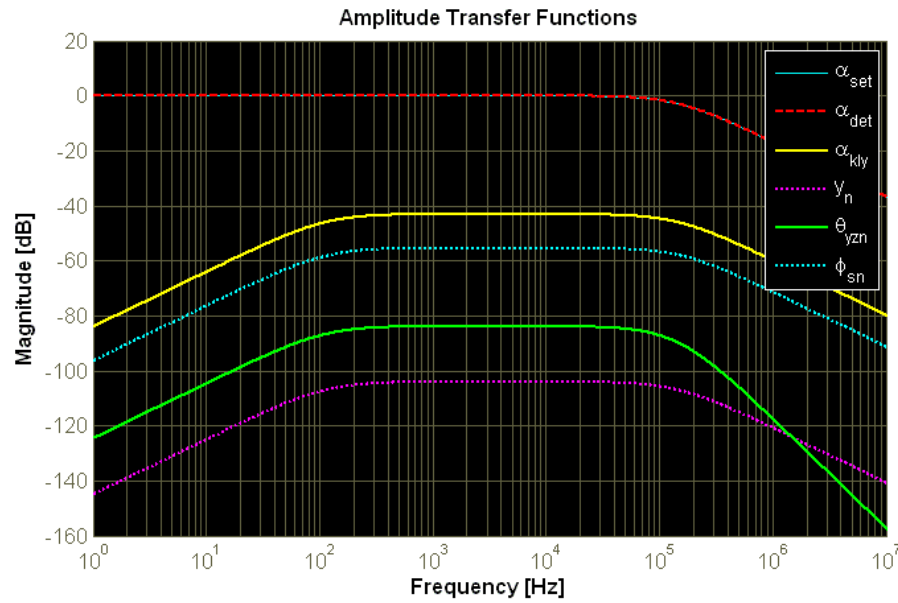
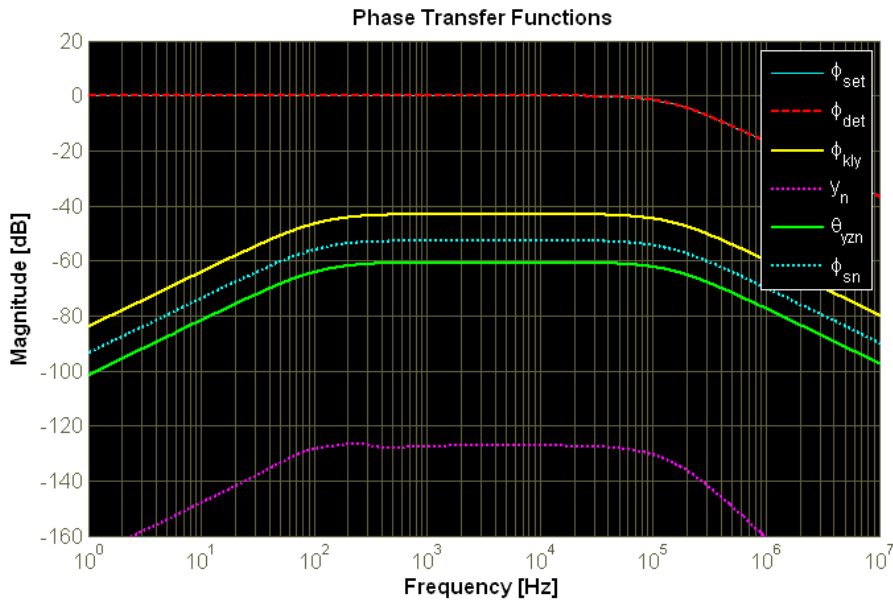
$$G_{ii}^G(s) = G_{qq}^G(s) = \frac{\sigma R}{s + \sigma}$$

Y = Beam Loading Factor which can be negative for deflecting cavities. Amp/Phase control can be lost when beam offset drives the cavities to full field (there is no drive carrier). This doesn't happen for I/Q control.

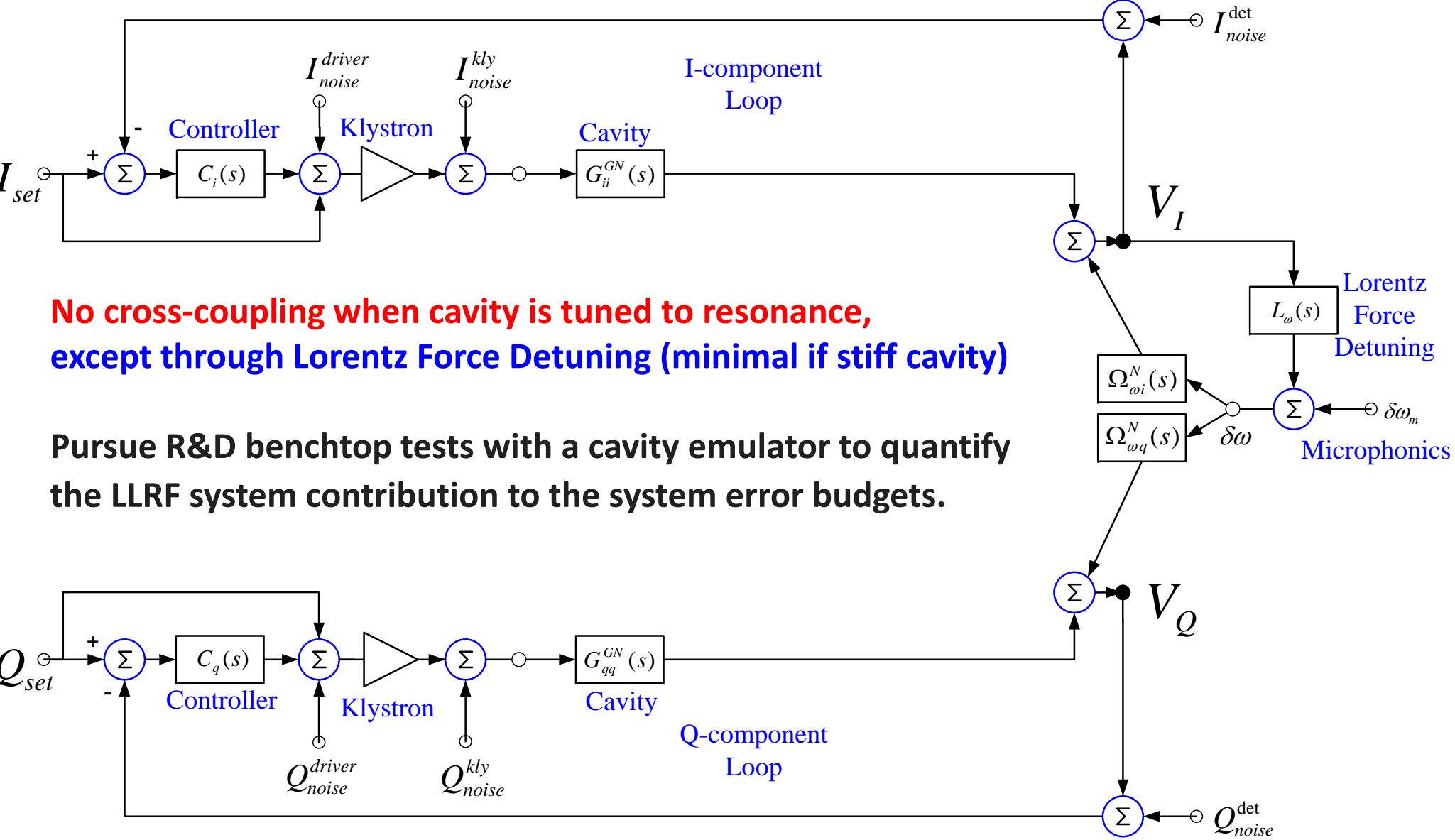
Deflecting Cavity - Dynamic Behavior



Deflecting Cavity - Dynamic Behavior



Deflecting Cavity - Dynamic Behavior



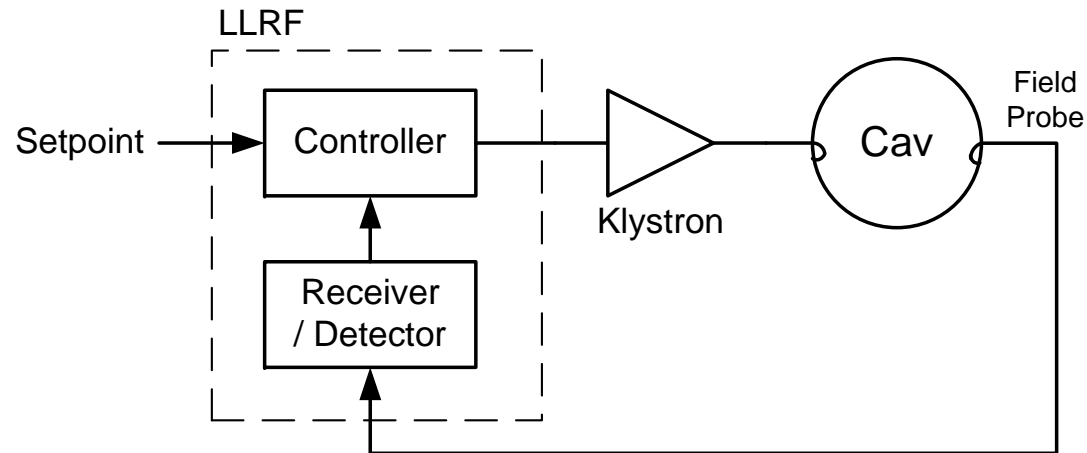
No cross-coupling when cavity is tuned to resonance, except through Lorentz Force Detuning (minimal if stiff cavity)

Pursue R&D benchtop tests with a cavity emulator to quantify the LLRF system contribution to the system error budgets.



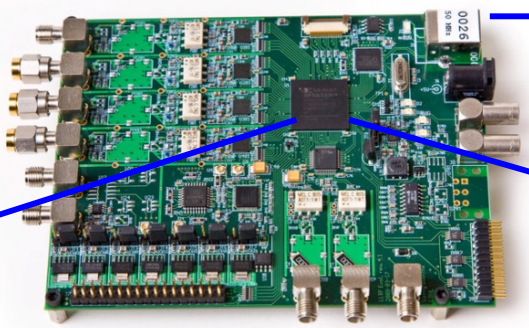
Low Level Radio Frequency (LLRF) System

Primary responsibility is to regulate the cavity field



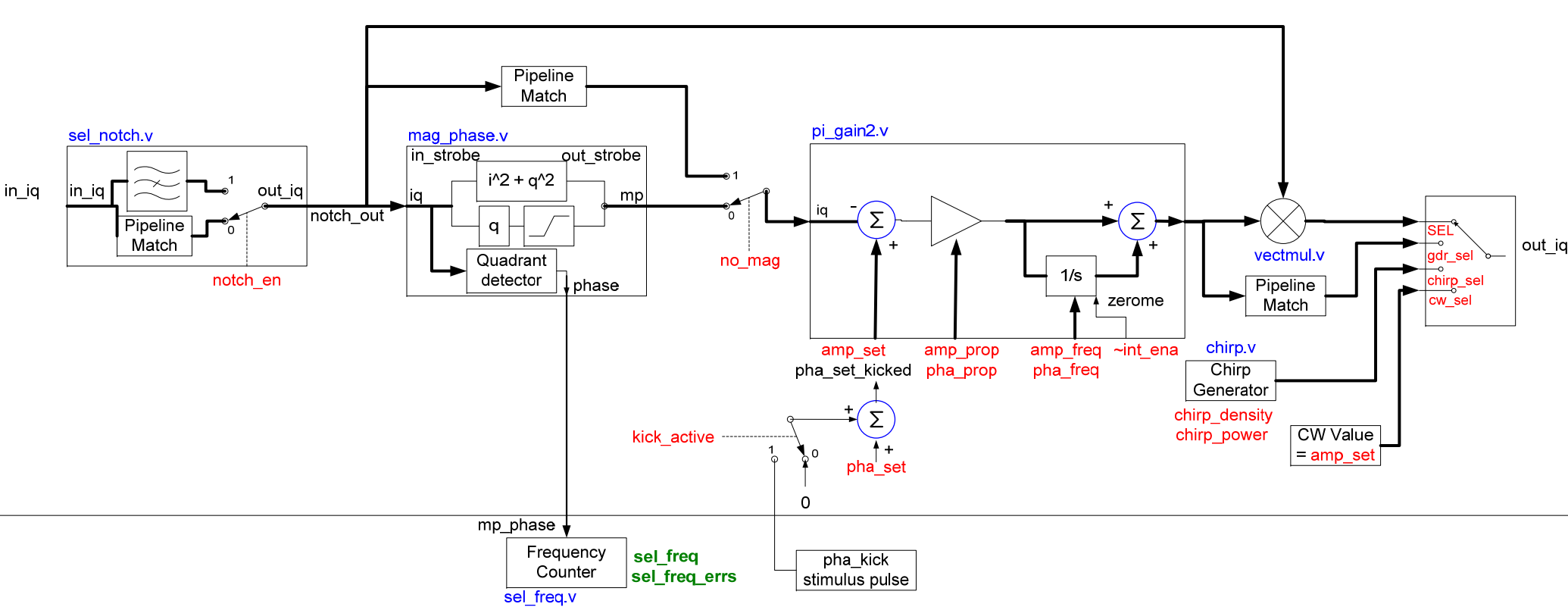
The Controller....

Controller



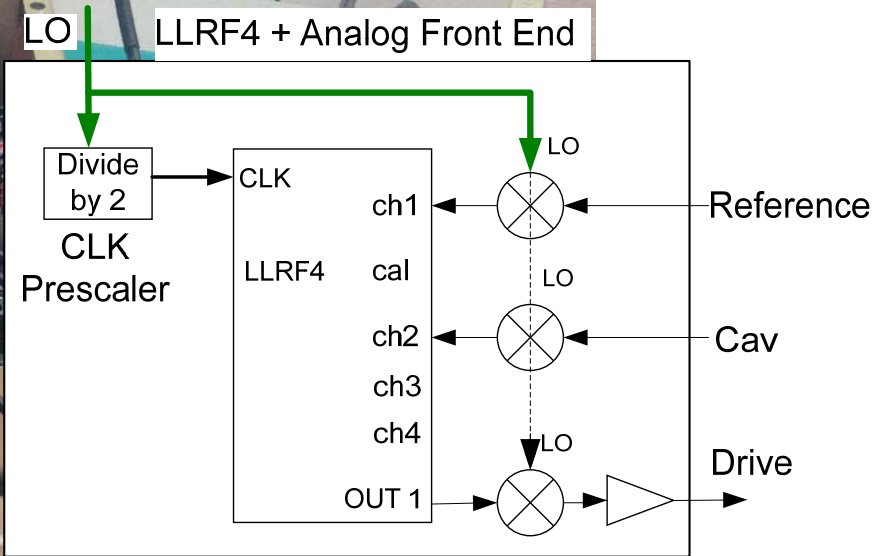
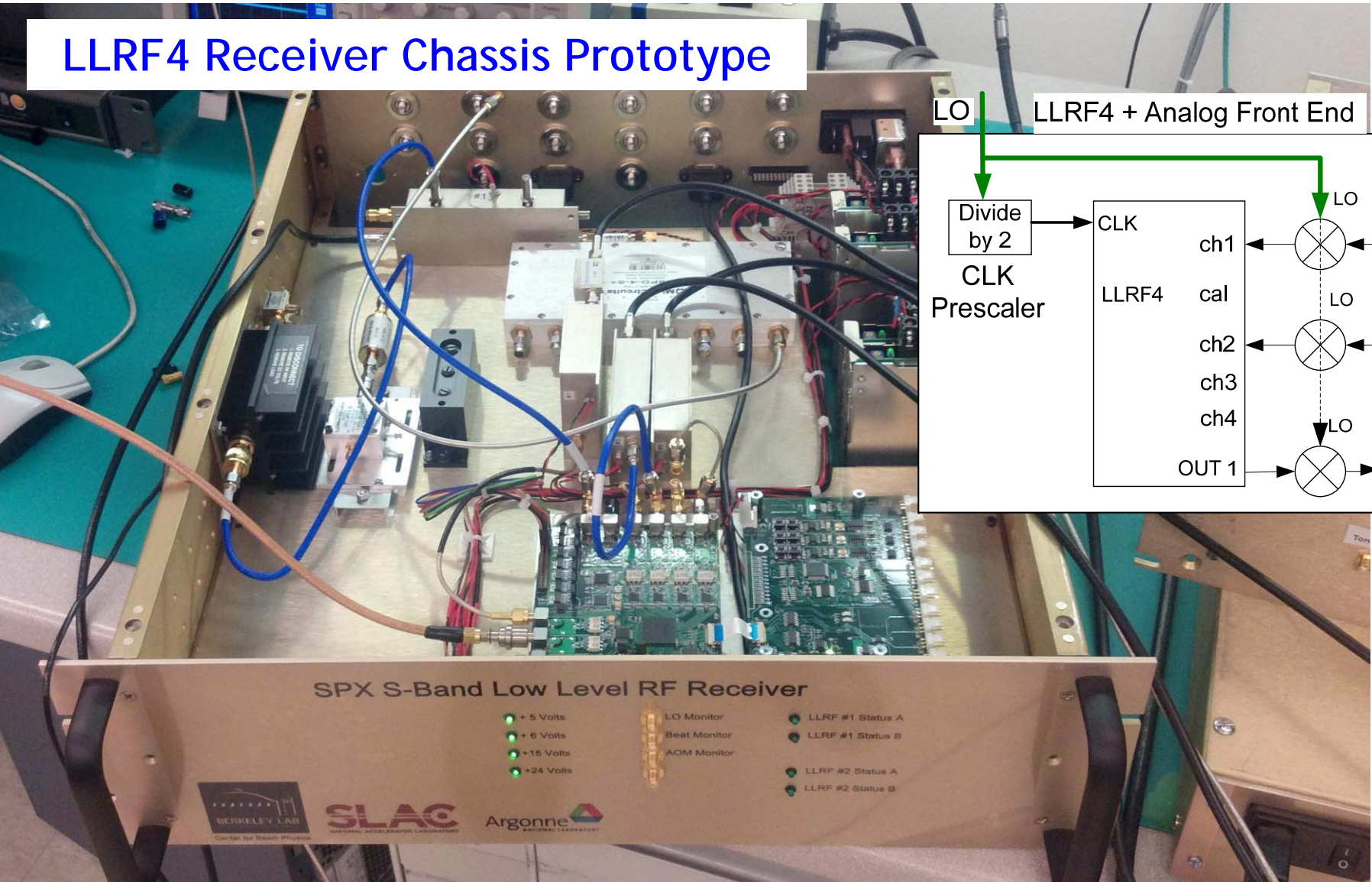
USB interface to host computer

sel_baseband.v



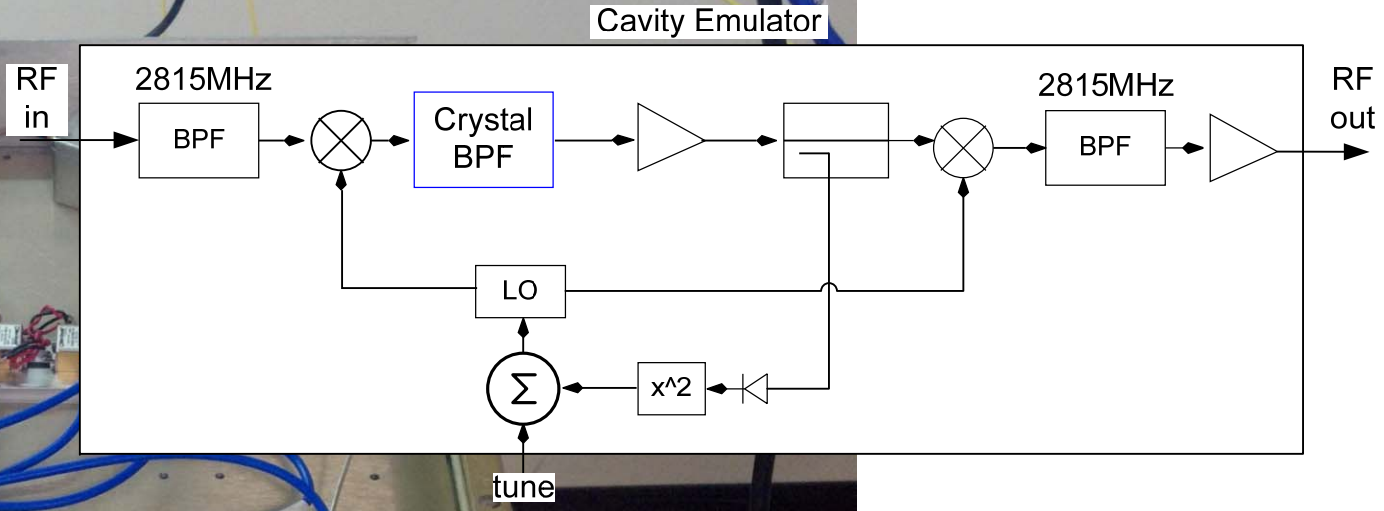
Controller – Benchtop Tests

LLRF4 Receiver Chassis Prototype

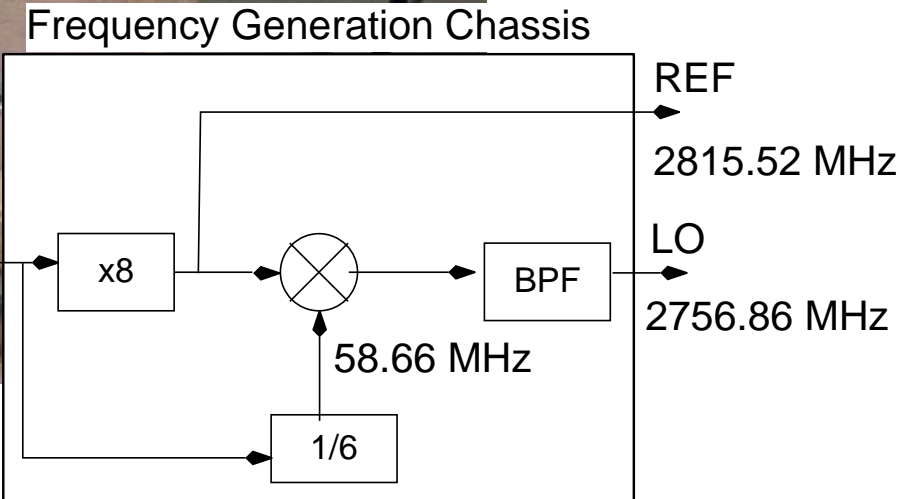


Controller – Benchtop Tests

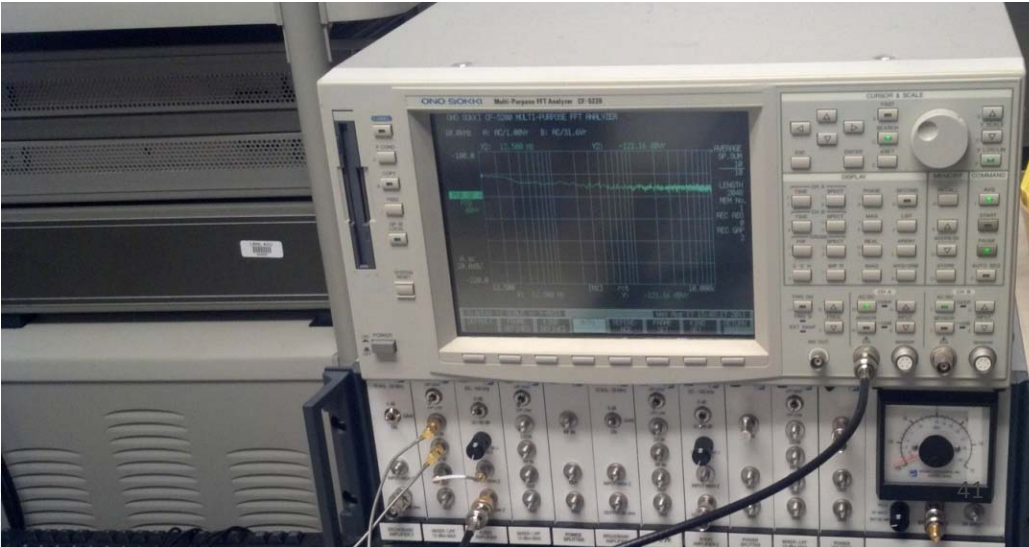
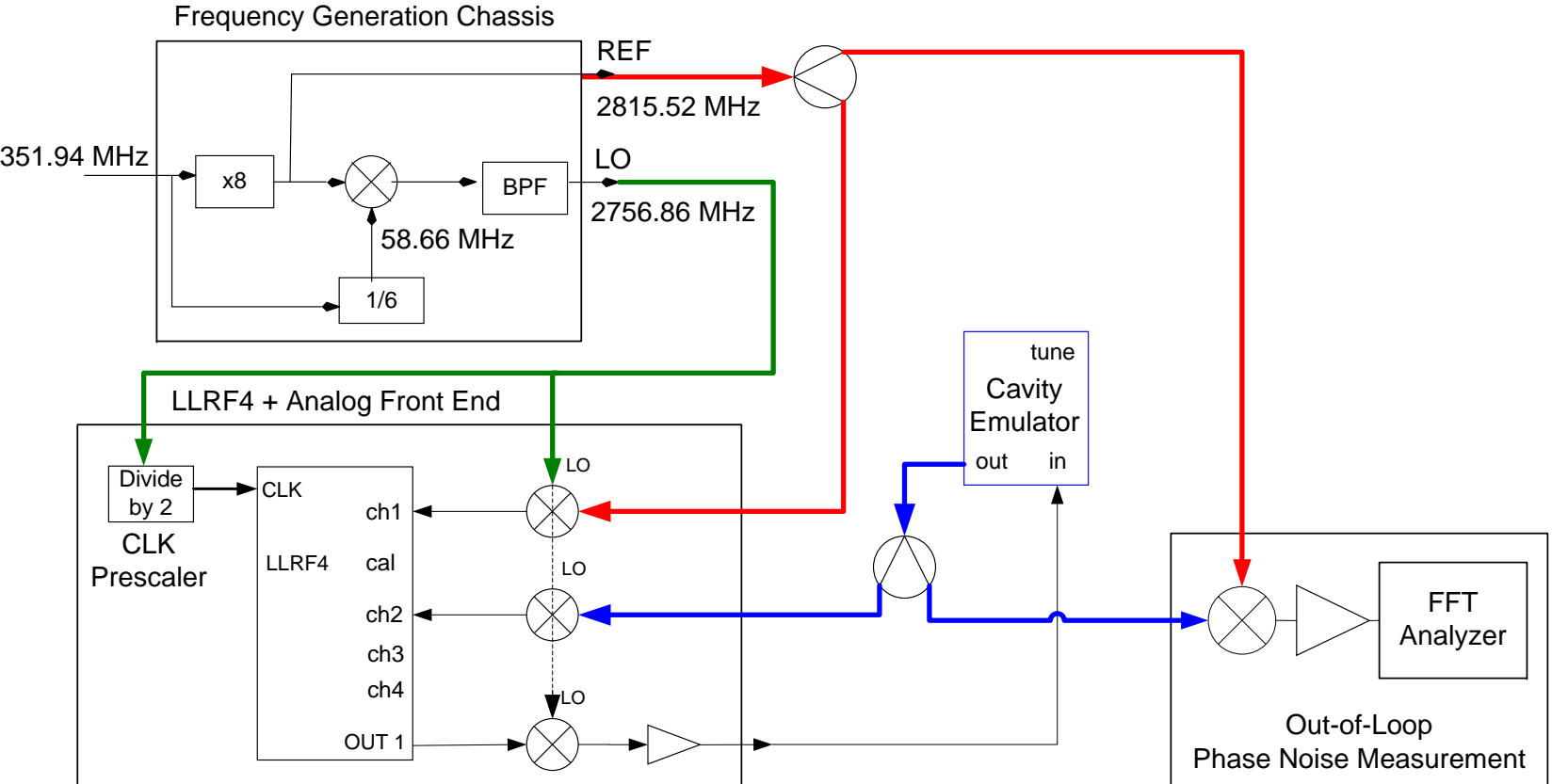
Cavity Emulator



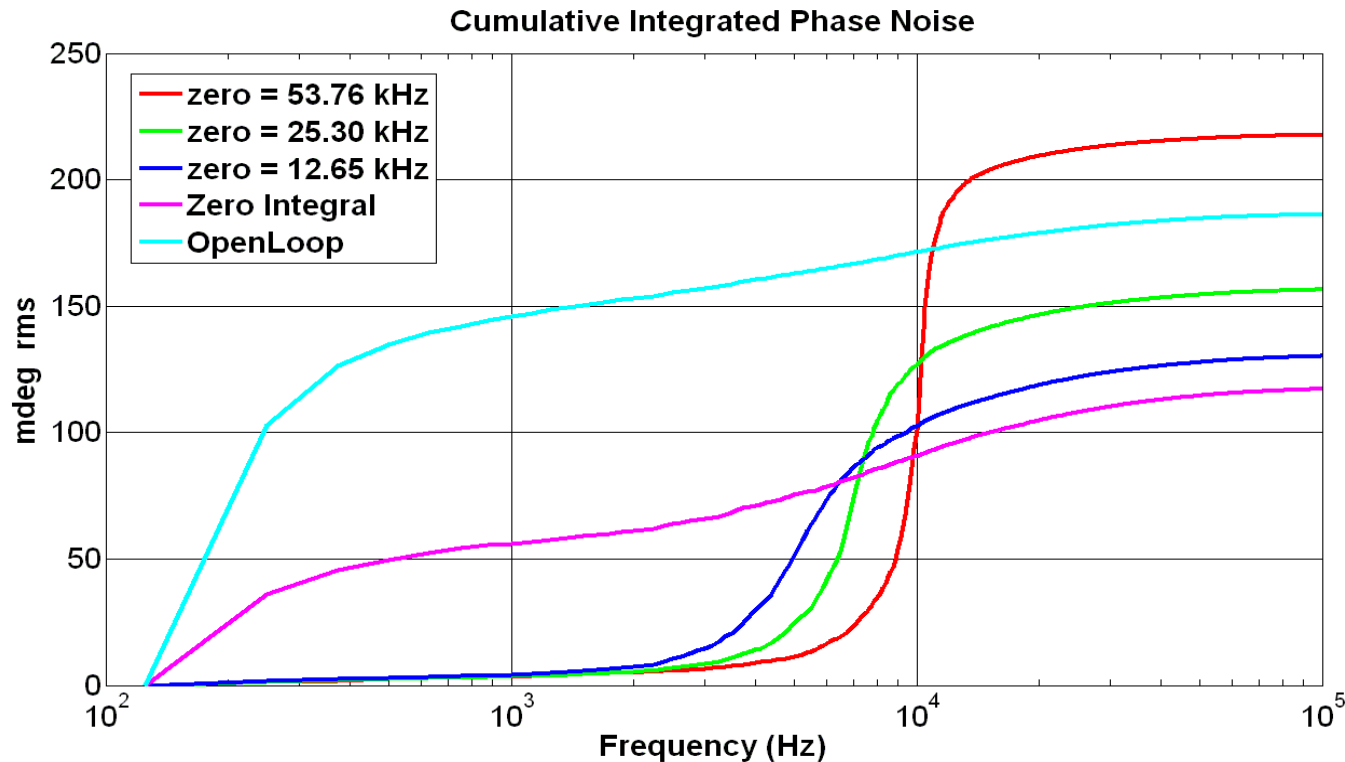
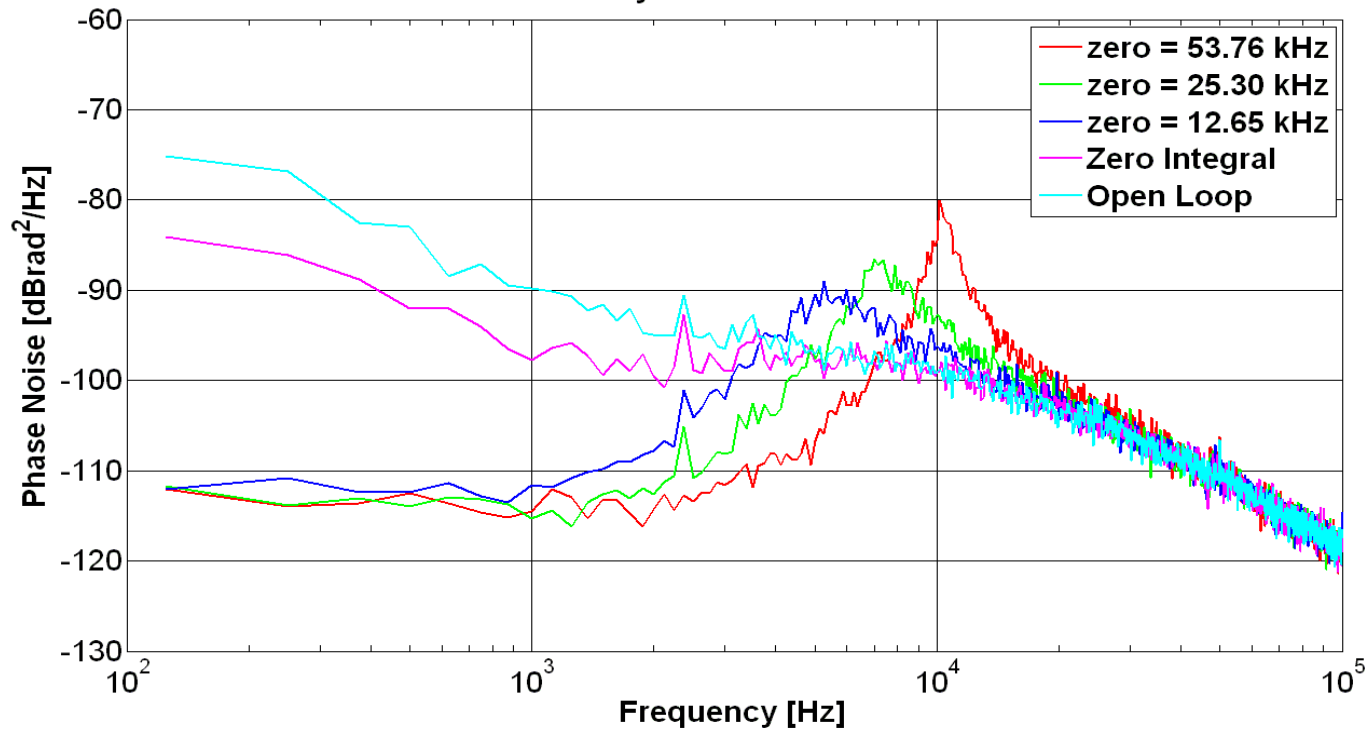
Frequency Generation Chassis



Controller – Single System Benchtop Test



LLRF4 Cavity Emulator Test 8/19/2011

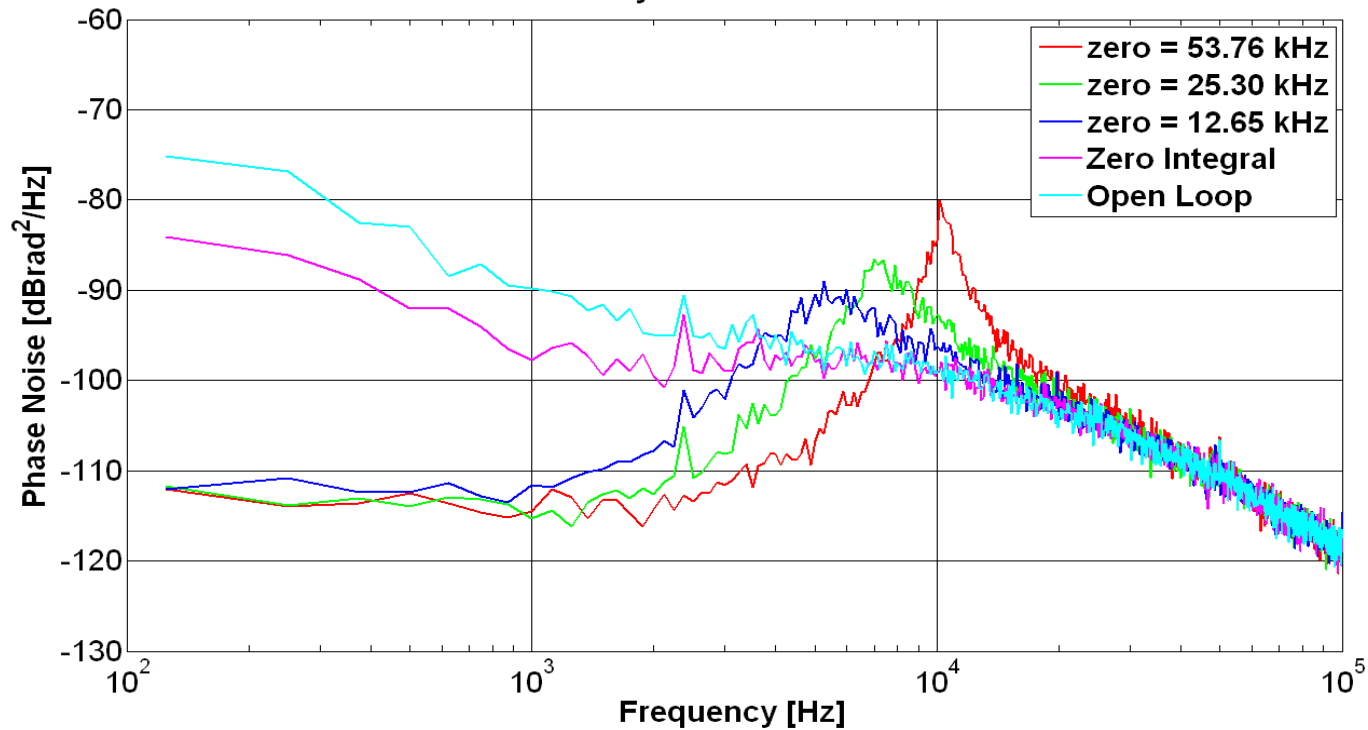


Noise sources include an independent LO generator used for cavity emulator. This is not something that exists in the 'real' system.

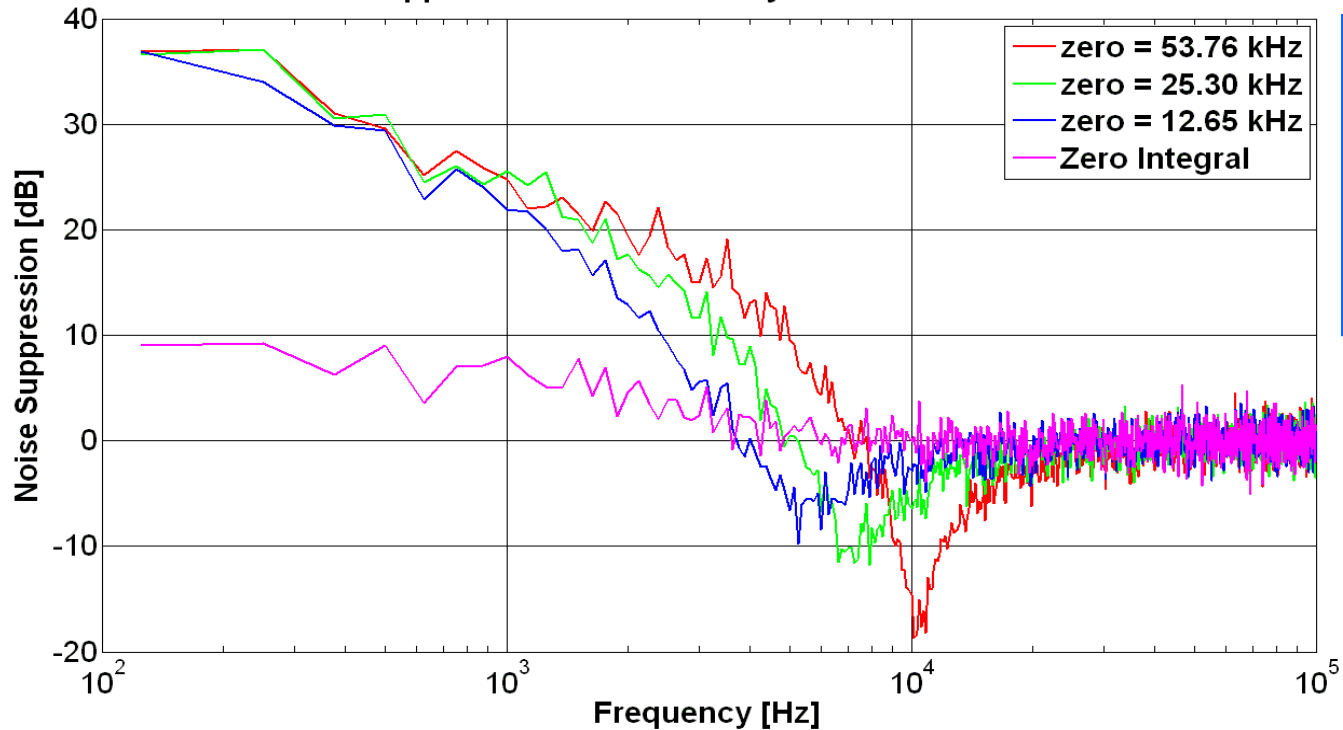
What matters is the noise suppression capability in combination with our expected noise sources.



LLRF4 Cavity Emulator Test 8/19/2011



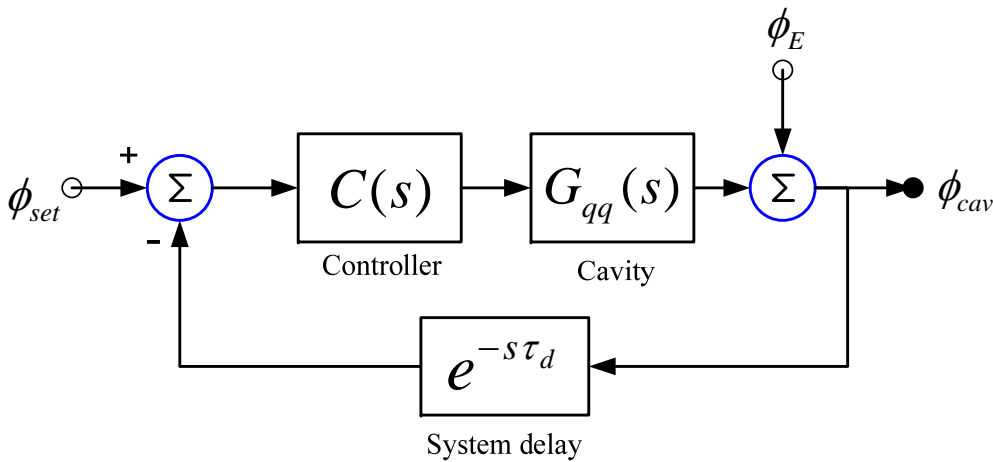
Noise Suppression - LLRF4 Cavity Emulator Test 8/19/2011



What matters is the noise suppression capability in combination with our expected noise sources.



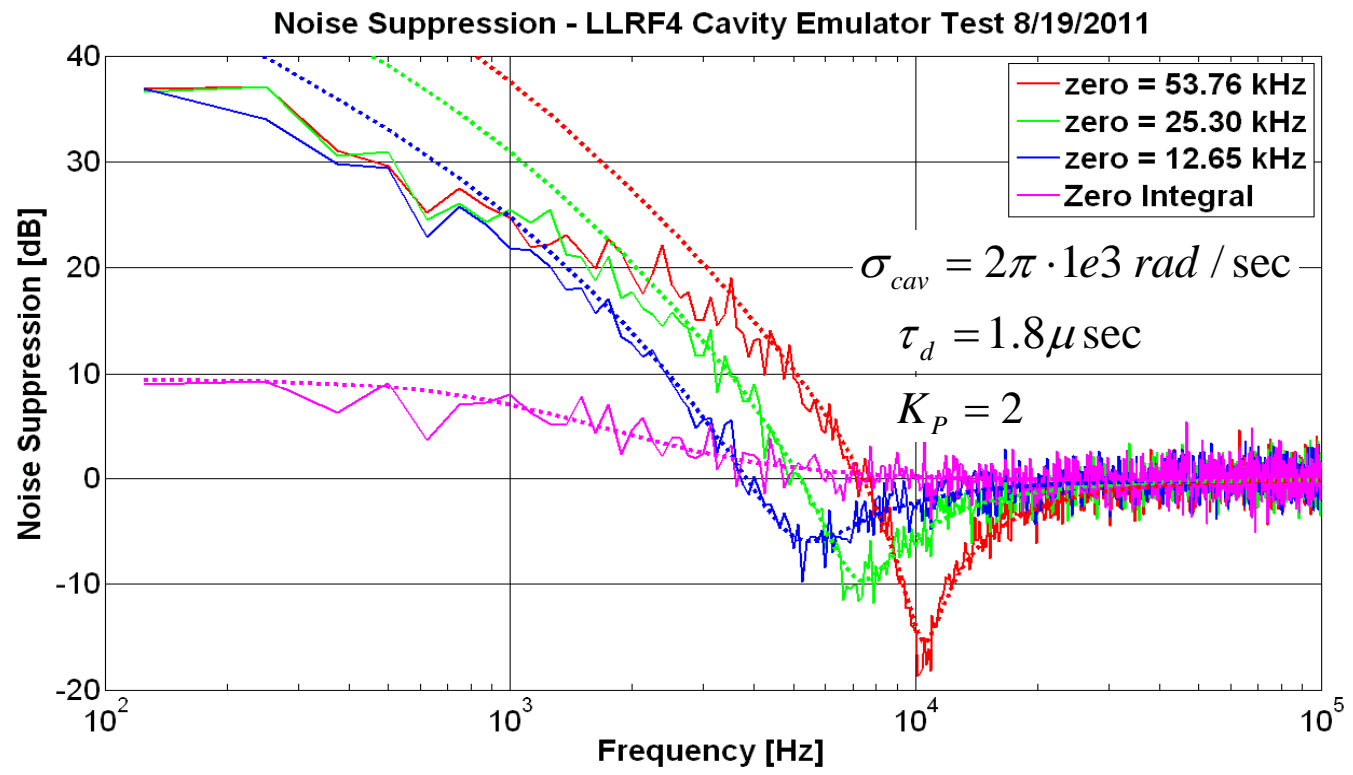
Controller – Noise Suppression Model



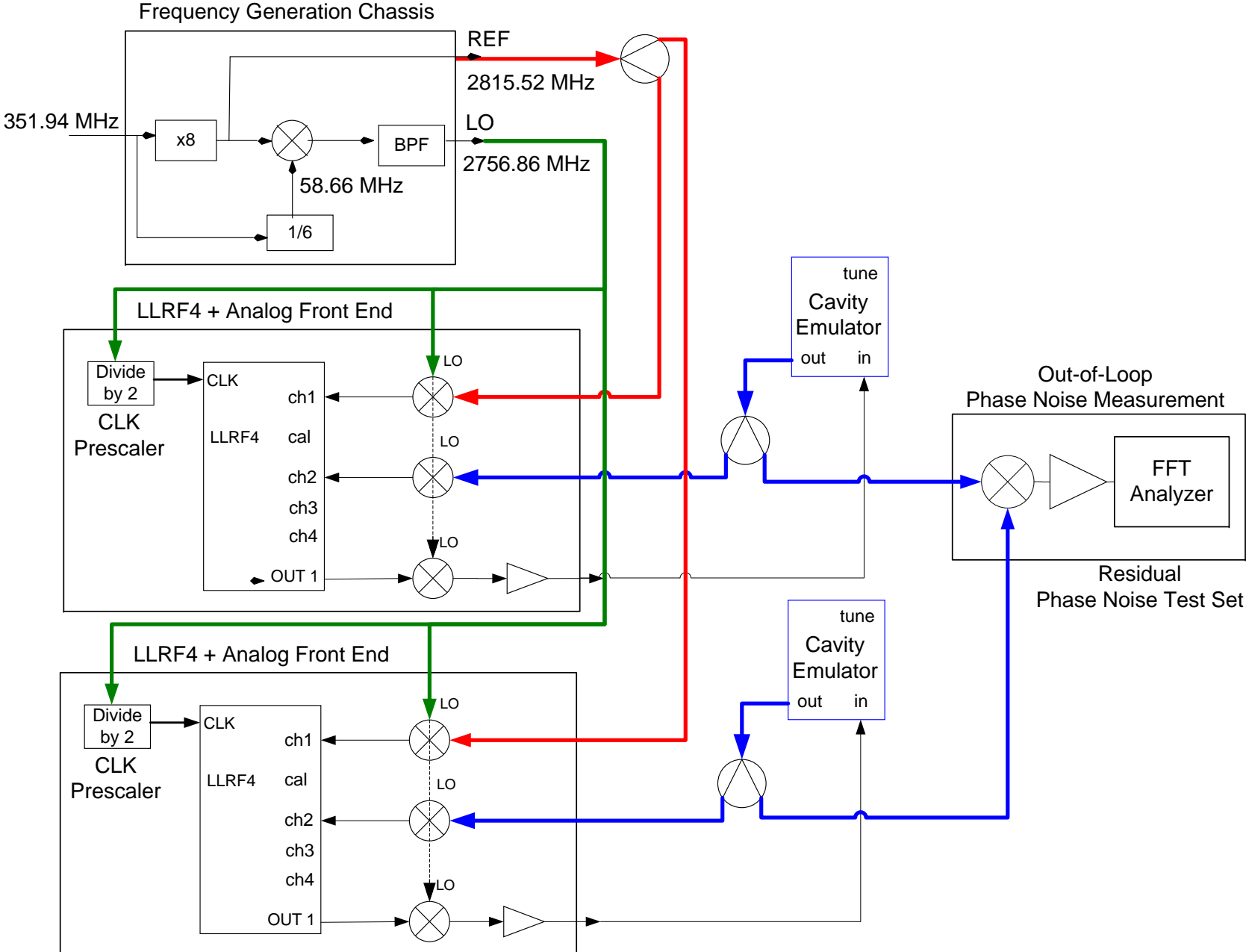
$$C(s) = K_P \left(1 + \frac{\sigma_Z}{s} \right) = K_P \left(\frac{s + \sigma_Z}{s} \right)$$

$$G_{qq}(s) = \frac{\sigma_{cav}}{s + \sigma_{cav}}$$

$$\frac{\phi_{cav}}{\phi_E} = \frac{1}{1 + C(s) G_{qq}(s) e^{-s\tau_d}}$$



Controller – 2 System Benchtop Test



Controller – 2 System Benchtop Test



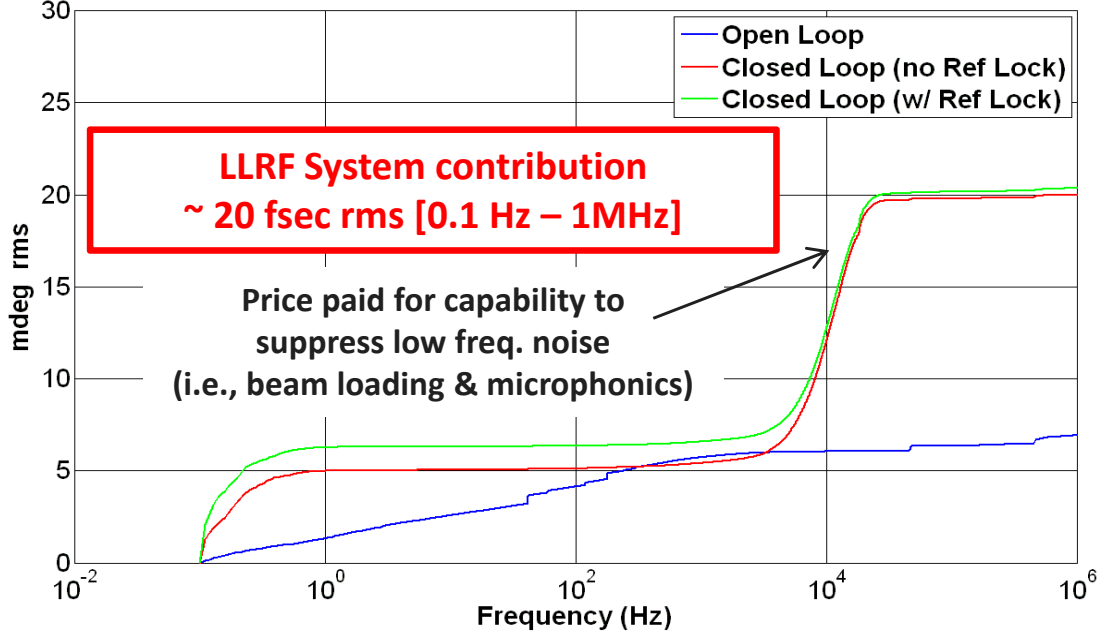
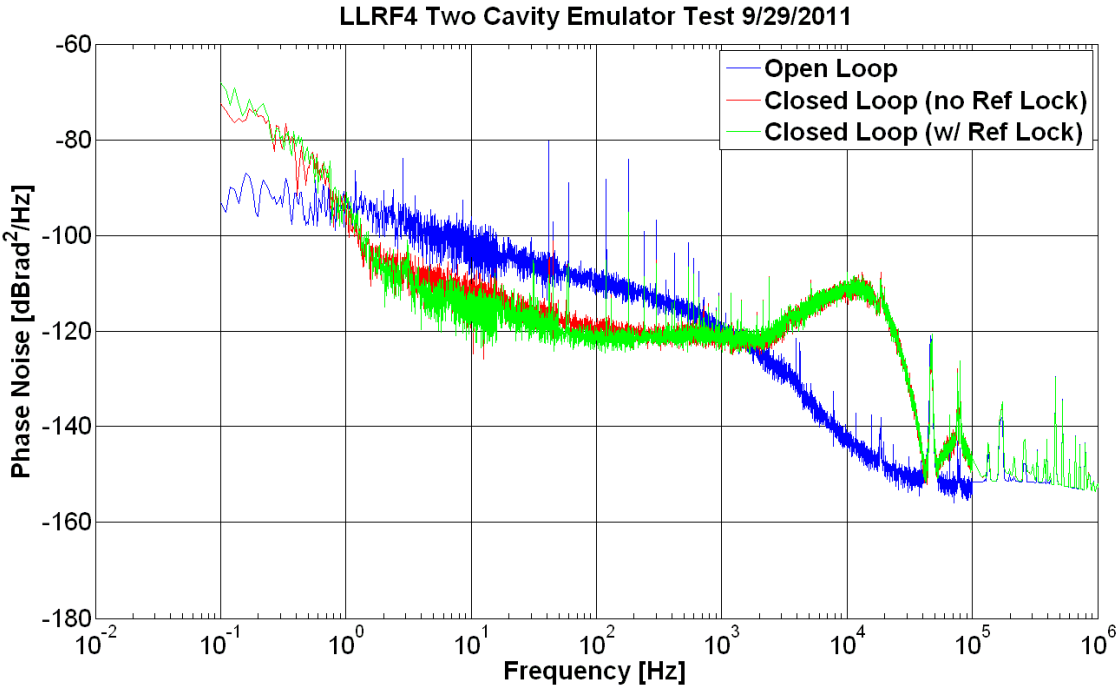
**Residual
Phase Noise
Test Set**
(measure noise
between cavity
emulators)

**Cavity
Emulators
#1 and #2**

**LLRF Receiver
#1**

**Freq.
Generation
Chassis**

**LLRF Receiver
#2**



LLRF R&D Outlook (**overly simplified**)

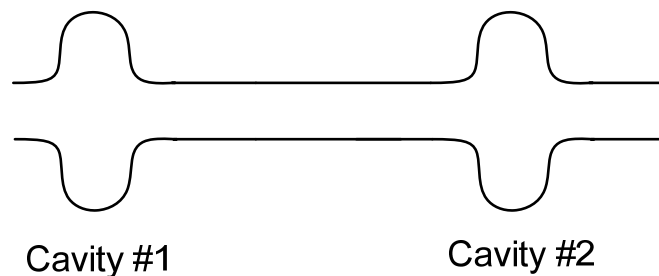
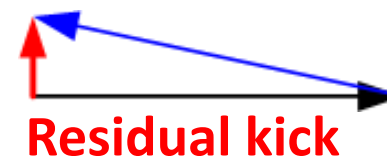
- Adding the calibration tone scheme into the cavity control gateway. Currently these are 2 separate code bases, parts need to be merged.
- Preparing for real single cavity testing to begin ~ June 2012
- **Modifications to Storage Ring RF System ...**

SPX0 System Performance Requirements ⁷

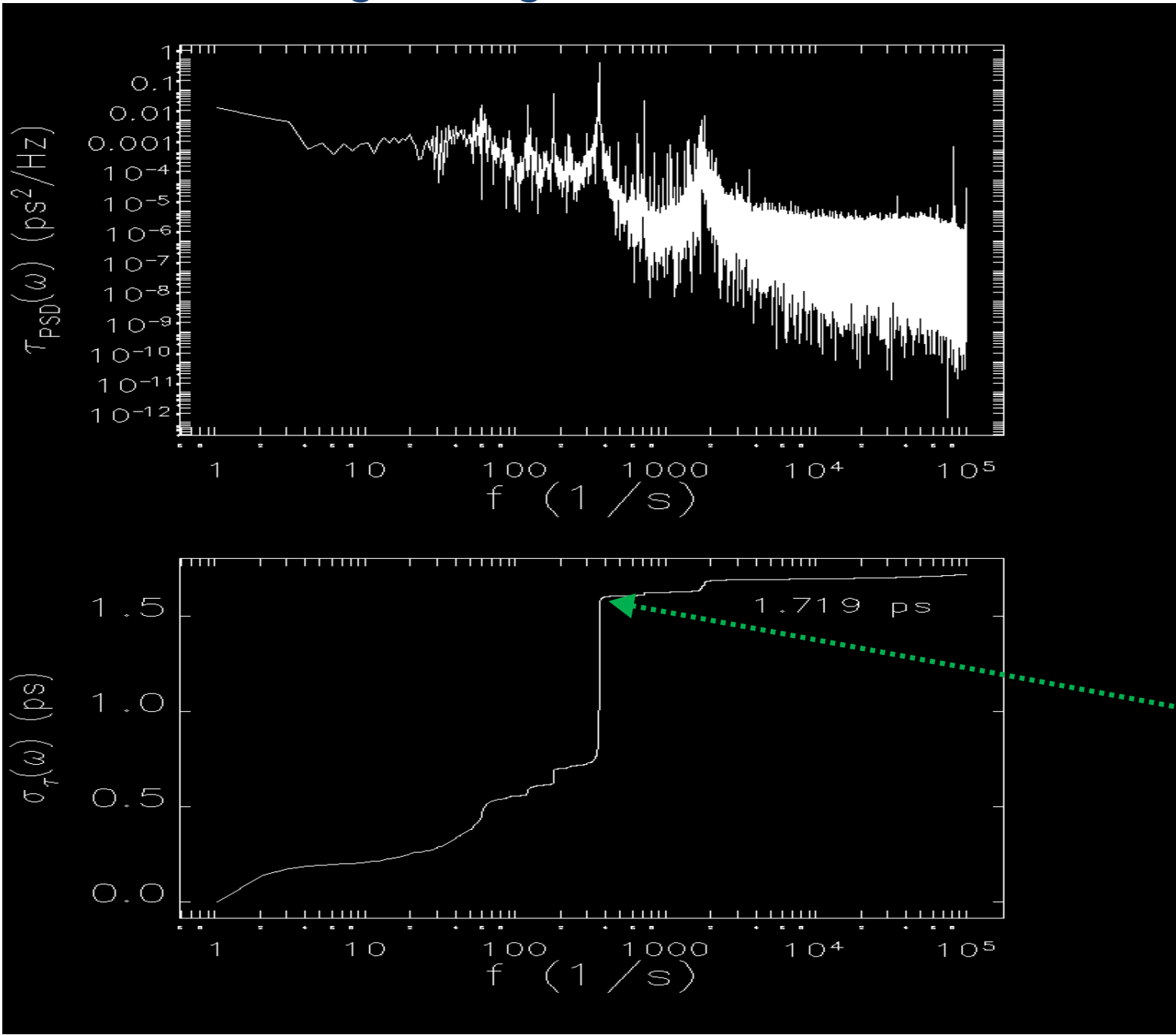
Specification name	Rms Value	Bandwidth	Driving requirement
Common-mode voltage amplitude variation	< 7%	0.1Hz – 271kHz	Keep beam emittance variation distinguishable from the differential voltage effect for SPX0
Common-mode phase variation	< 1.0 deg	0.1Hz – 1kHz	Keep global orbit motion distinguishable from differential phase for SPX0
	< 3.6 deg	1kHz – 271kHz	Keep rms emittance variation distinguishable from differential phase for SPX0
Differential mode voltage variation	< 1%	0.1Hz – 1kHz	Keep rms emittance variation outside of SPX under 10 % of nominal 35 pm
	< 0.77%	1kHz – 271kHz	Effective emittance growth under 1.5 pm for SPX
Differential mode phase variation	< 0.077 deg	0.1Hz – 1kHz	Keep global rms orbit motion under 10% of the beam size/divergence for SPX
	< 0.28 deg	1kHz – 271kHz	Keep emittance growth outside of SPX under 10 % of nominal 35 pm

Common Mode

Differential



Present Storage Ring Beam Jitter ⁸



$$\sim 1.65 = \sqrt{0.7^2 + 1.5^2}$$

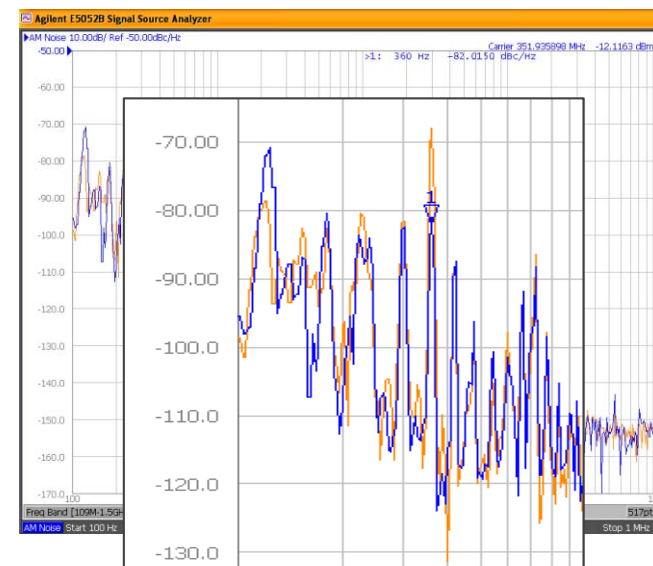
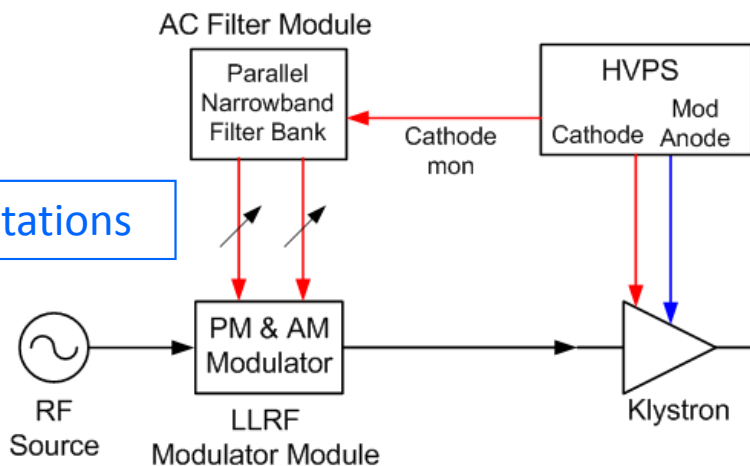
$$0.86 = \sqrt{0.7^2 + 0.5^2}$$

$$0.72 = \sqrt{0.7^2 + 0.15^2}$$

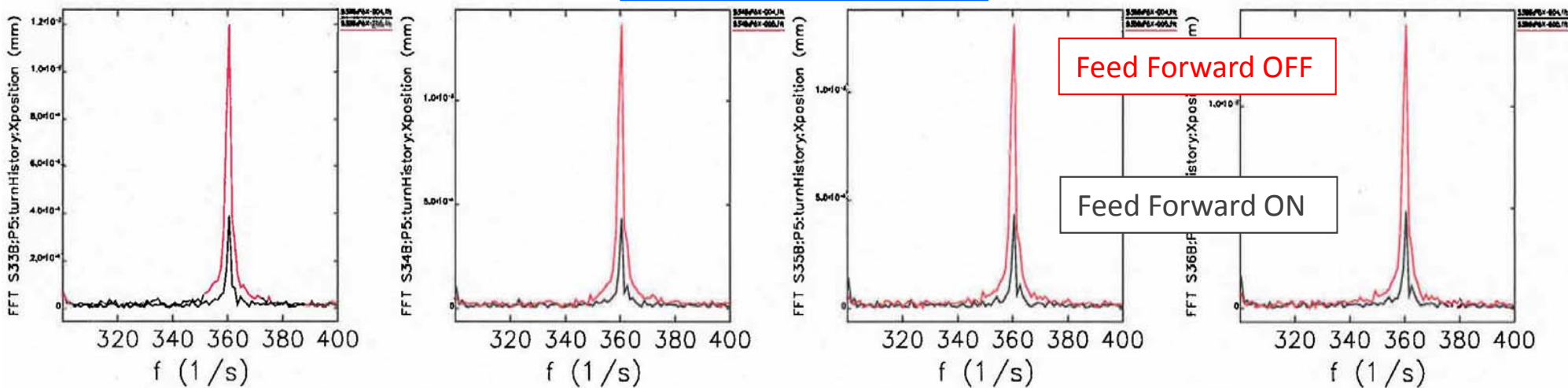
Proof of Principle Feed Forward Experiment

Experiment with 360Hz Feed-Forward correction of Storage Ring Klystron High-Voltage Power Supply (HVPS) induced noise

AM & PM suppression at Both Stations



Horizontal BPM Data



Adaptive Noise Cancellation Concept ⁹

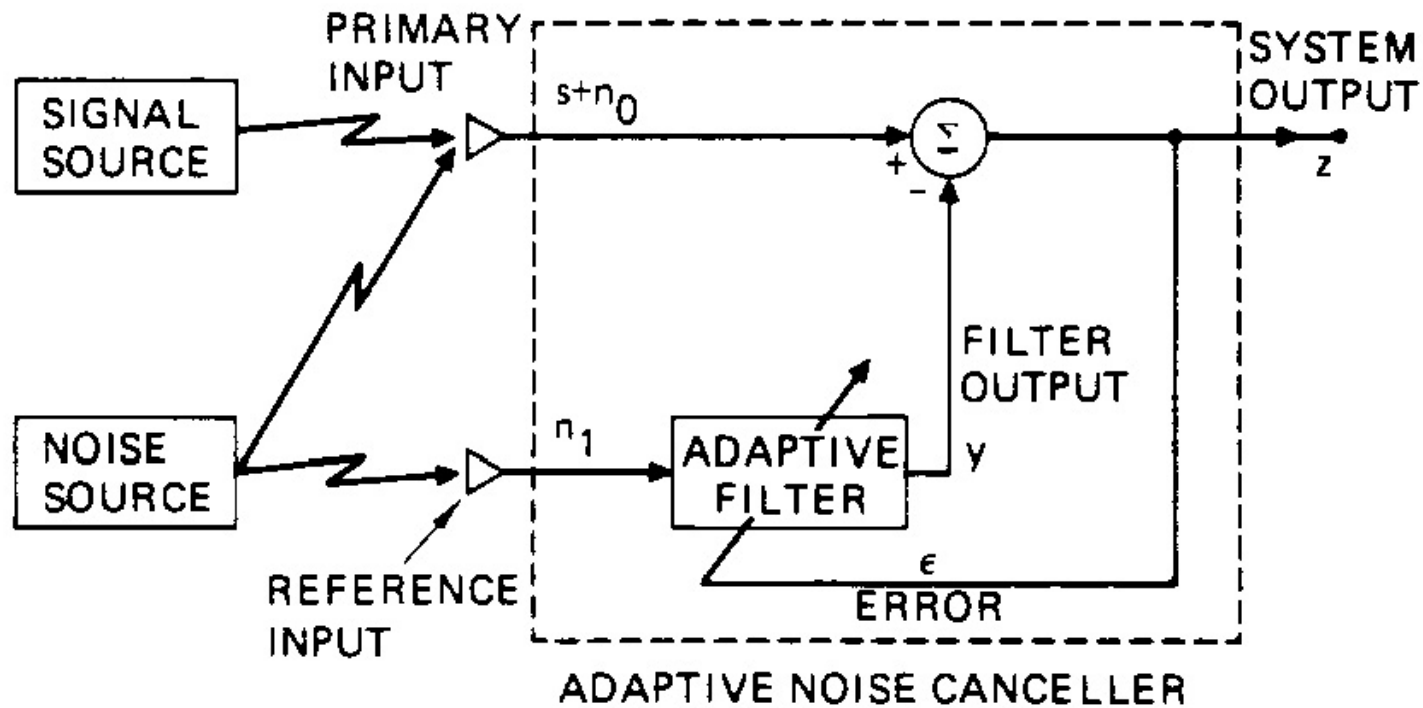
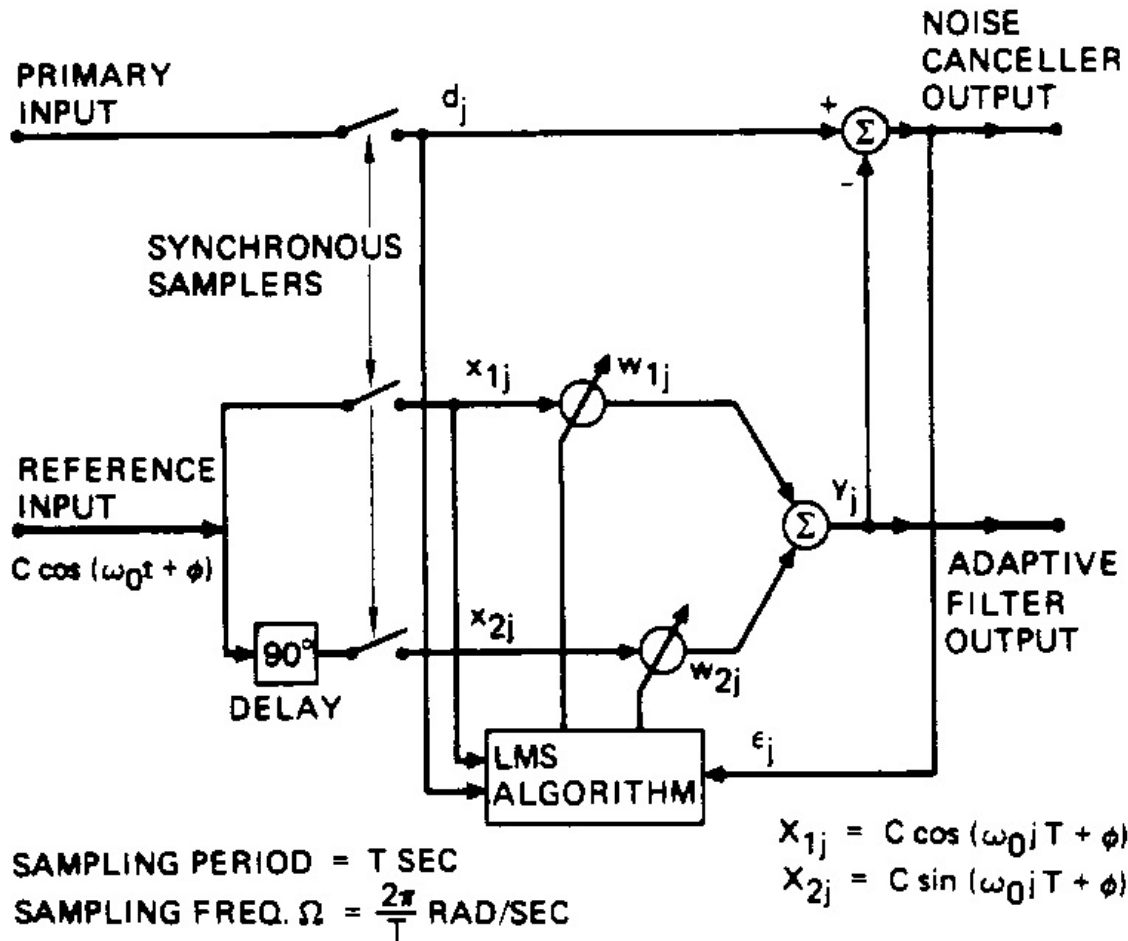


Fig. 1. The adaptive noise cancelling concept.

From [9]

Adaptive Noise Cancellation Concept ⁹



$$N_I \cos \omega_N t - N_Q \sin \omega_N t$$

$$(Y_I - N_I)^2 + (Y_Q - N_Q)^2$$

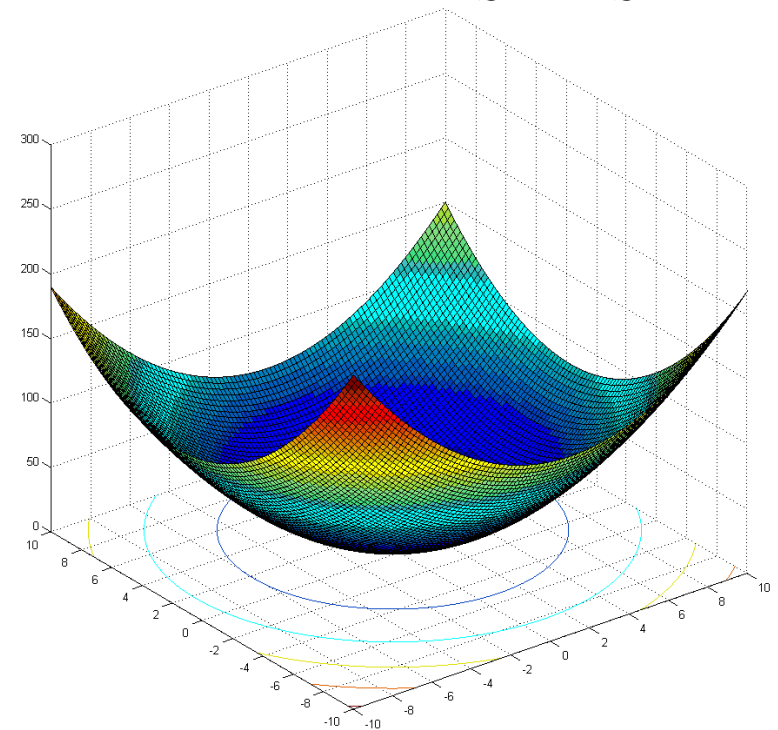
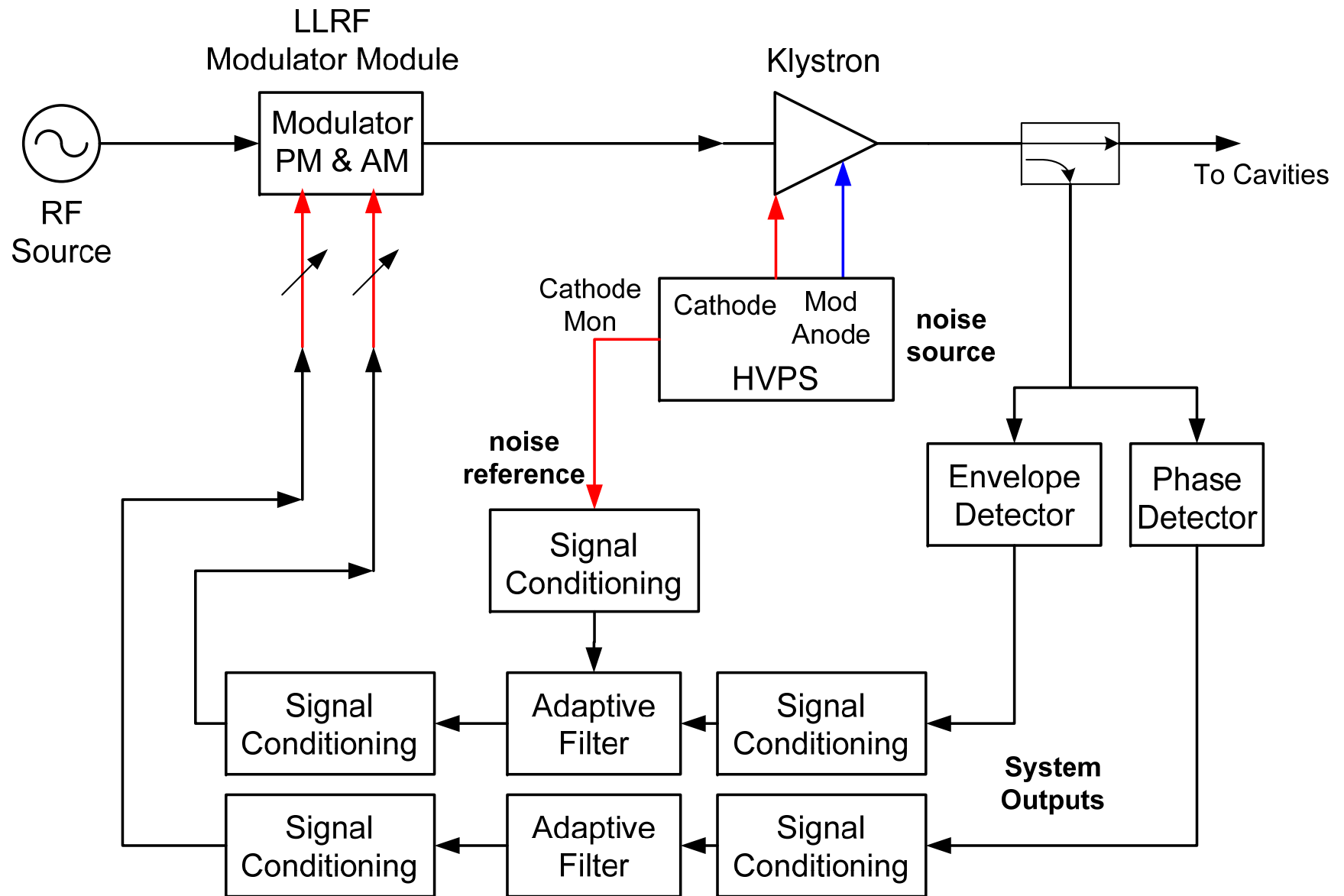


Fig. 6. Single-frequency adaptive noise canceller.

From [9]

Storage Ring RF AM/PM Noise Suppression Concept



Summary

- Digital LLRF system shows promise of femto-second level synchronization [0.1 Hz – 1MHz] with proper attention to common source distribution
- Great design improvement demonstrated for Analog Front End with T3 mixers
- New I/Q small-signal baseband model developed for SRF Deflecting Cavities
- Adaptive noise cancellation of Storage Ring main 352MHz RF system AM/PM noise is being pursued to reduce present beam jitter